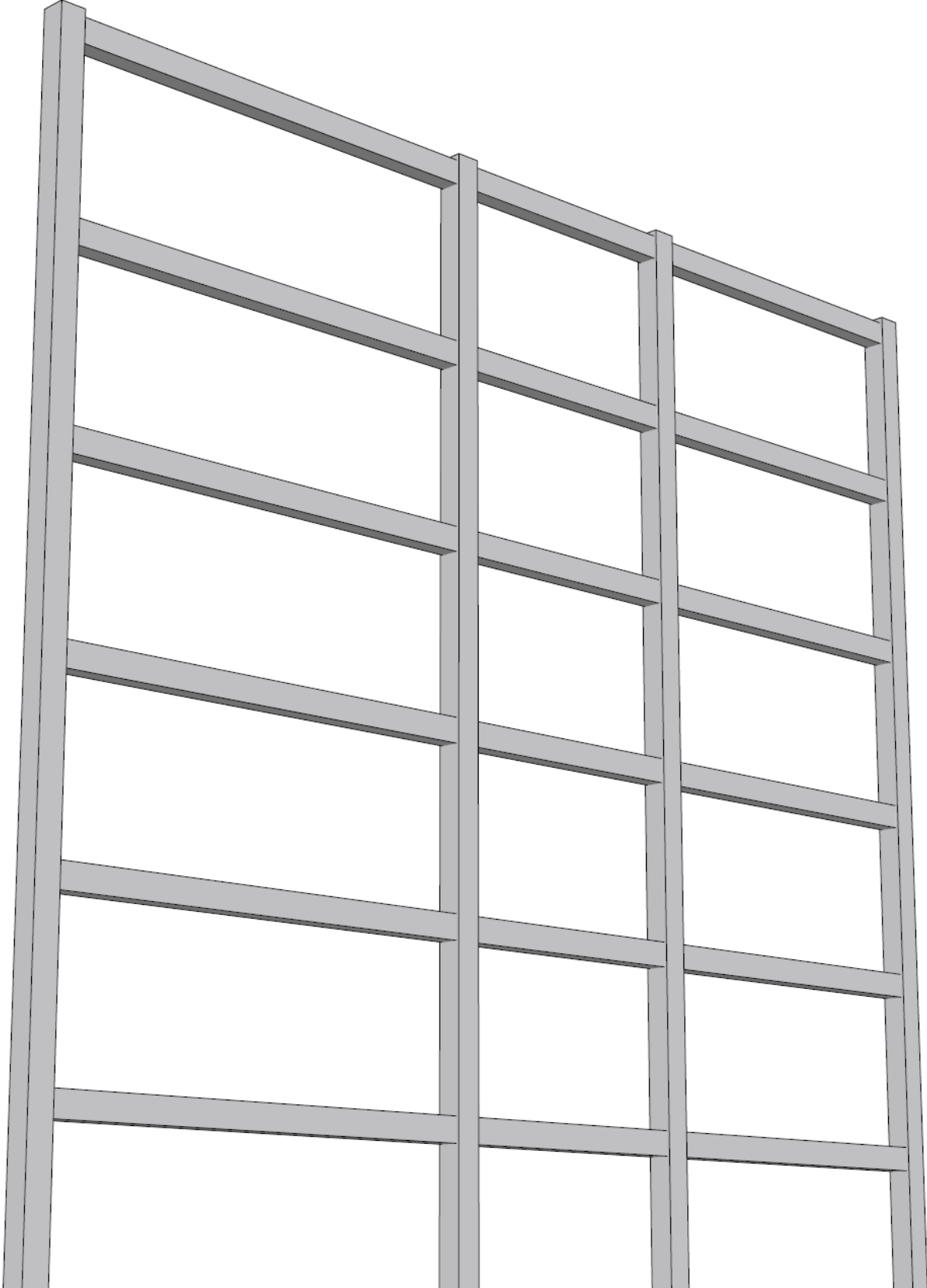


Continuous Beam Design with Moment Redistribution (ACI 318-14)



Continuous Beam Design with Moment Redistribution (ACI 318-14)

A structural reinforced concrete continuous beam at an intermediate floor level in an exterior frame (spandrel Beam) provides gravity load resistance for the applied dead and live loads.

The required reinforcement areas are determined for this continuous beam after analysis are adjusted and optimized using moment redistribution provisions from ACI 318 standard. The results of hand calculations are then compared with numerical analysis results obtained from the [spBeam](#) engineering software program.

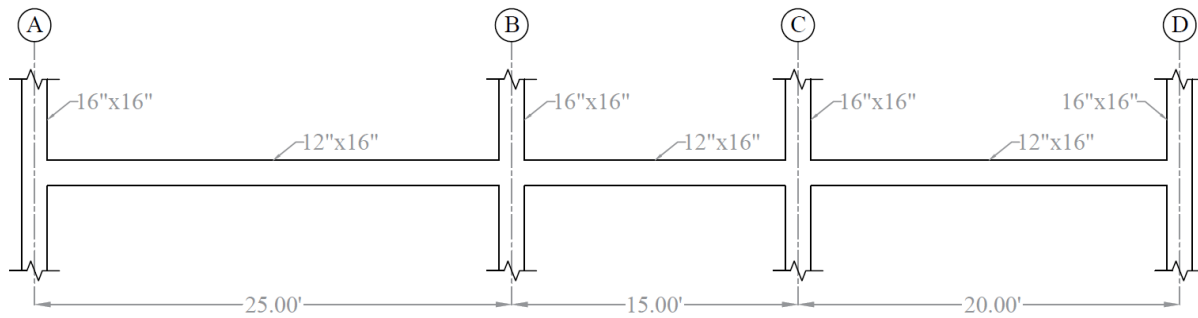


Figure 1 – Reinforced Concrete Continuous Beam at intermediate floor level

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Code

Building Code Requirements for Structural Concrete (ACI 318-14) and Commentary (ACI 318R-14)

Reference

PCA Notes on ACI 318-11 Building Code Requirements for Structural Concrete, Twelfth Edition, 2013 Portland Cement Association, Example 8.2 (In this example ACI 318-14 is used instead of ACI 318-11)

[spBeam](#) Engineering Software Program Manual v5.00, STRUCTUREPOINT, 2015

Design Data

$f_c' = 4,000$ psi normal weight concrete ($w_c = 150$ pcf)

$f_y = 60,000$ psi

Story height = 10 ft

Columns = 16 in. x 16 in.

Spandrel beam = 12 in. x 16 in.

Dead Loads (DL) = 1,167 lb/ft

Live Loads (LL) = 450 lb/ft

Solution

Continuous beams are frequently analyzed and designed using simplified methods such as the approximate coefficients provided in ACI 318 to approximate the bending moments and shear forces. There are many important limitations to allow the use of coefficients. The factored moment and shear can be determined using the simplified method if the requirements are satisfied: [ACI 318-14 \(6.5.1\)](#)

- ✓ Members are prismatic.
- ✓ Loads are uniformly distributed.
- ✓ $L \leq 3D$
- ✓ There are at least two spans.
- X The longer of two adjacent spans does not exceed the shorter by more than 20 percent.

In this example the ratio of the two adjacent spans lengths exceeds 1.2 and coefficients can't be used. Therefore, the analysis of the continuous beam framing into columns must use traditional analysis methods and will be performed using the following steps:

1. Determine the factored loads.
2. Perform the structural analysis using the moment distribution method.
3. Repeat the analysis for each live load pattern to arrive at the enveloped maximum design moments.
4. Apply moment redistribution provisions to get adjusted (reduced) design moments.
5. Determine the required area of steel optimized to the adjusted design moments.

It is important in this example to distinguish between the two terms: **moment distribution** and **moment redistribution**. **Moment distribution** is a structural analysis method for statically indeterminate beams and frames, while **moment redistribution** refers to the behavior of statically indeterminate structures that are not completely elastic, but have some reserve plastic capacity. When one location first yields, further application of load to the structure causes the bending moment to redistribute differently from what a purely elastic analysis would suggest.

Moment redistribution is not commonly used primarily due to the extensive additional and tedious calculations required involving many live load patterns and the iterative nature of the procedure that lends itself to automation as is provided by [spBeam](#) engineering software program from [StructurePoint](#).

When permitted, **moment redistribution** is used to reduce total reinforcement required and this example will illustrate the extent of redistribution of bending moments and the corresponding reduction of steel area achievable. Typically, negative moments over supports governs the design of reinforcement and any reduction in the required area of steel at the supports is favorable due to savings in materials, labor, and construction time and effort.

1. Continuous Beam Analysis – Moment Distribution Method

Determine moment distribution factors and fixed-end moments for the frame members. The moment distribution procedure will be used to analyze the frame. Stiffness factors, carry over factors, and fixed-end moment factors for the beams and columns are determined as follows:

Determine the elastic bending moment diagrams for each of the load patterns per ACI and the maximum moment envelope values for all patterns as shown in Table 1. ACI 318-14 (6.4)

1.1. Load combination

$$U = 1.2D + 1.6L \quad \text{ACI 318-14 (Eq. 5.3.1b)}$$

$$w_d = 1.2 \times 1.167 = 1.4 \text{ kips/ft}$$

$$w_l = 1.6 \times 0.45 = 0.72 \text{ kips/ft}$$

$$w_u = 0.72 + 1.4 = 2.12 \text{ kips/ft}$$

1.2. Flexural stiffness of beams and columns ends, K

$$K = \frac{4 \times E_c \times I}{l}$$

Where K is referred to as stiffness factor at beam or column end and can be defined as the amount of moment required to rotate the end of the beam or column 1 rad.

$$I = \frac{b \times h^3}{12}$$

$$E = w_c^{1.5} \times 33 \times \sqrt{f_c'} \quad \text{ACI 318-14 (Eq. 19.2.2.1.a)}$$

For member AB:

$$l = 25 \text{ ft}$$

$$I = \frac{12 \times 16^3}{12} = 4,096 \text{ in.}^2$$

$$E = \frac{(150)^{1.5} \times 33 \times \sqrt{4000}}{1000} = 3,834 \text{ ksi}$$

$$K_{AB} = \frac{4 \times 3,834 \times 4,096}{25 \times 12} = 209.4 \times 10^6 \text{ in.-lb}$$

1.3. Distribution factor, DF

$$DF = \frac{K}{\sum K}$$

The distribution factor for a member that is connected to a fixed joint is defined as the fraction of the total resisting moment supplied by this member.

For member AB:

$$DF_{AB} = \frac{209.4 \times 10^6}{209.4 \times 10^6 + 698.0 \times 10^6 + 698.0 \times 10^6} = 0.130$$

1.4. Flexural stiffness of beams and columns ends, COF

$$\text{COF} = 0.5$$

Where COF is the Carry-Over Factor that represents the fraction of the moment that is “carried over” from the joint to the beam end when the beam far end is fixed.

1.5. Fixed-end moments, FEMs

For a beam with uniformly distributed load and fixed ends, *FEM* can be found using the following equation:

$$FEM = \frac{w \times l^2}{12}$$

For member AB for load pattern I:

$$FEM_{AB} = \frac{2.12 \times 25^2}{12} = 110.4 \text{ kip-ft}$$

1.6. Beam analysis using moment distribution method

Repeat the previous steps to all frame members to obtain the parameters necessary for the analysis. Moment distribution for the five loading conditions is shown in Table 1. Counter-clockwise rotational moments acting on member ends are taken as positive. Positive span moments are determined from the following equation:

$$M_{u(\text{midspan})} = M_o - \frac{(M_{uL} + M_{uR})}{2}$$

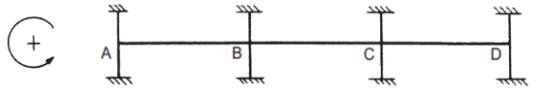
Where M_o is the moment at the midspan for a simple beam, M_{uL} and M_{uR} are the negative moment at the span left and right end, respectively.

When the end moments are not equal, the maximum moment in the span does not occur at the midspan, but its value is close to that midspan for this example.

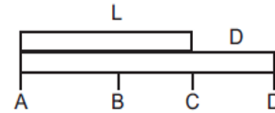
Positive moment in span A-B for load pattern I:

$$M_u^+ = \frac{2.12 \times 25^2}{8} - \frac{(99.7 + 109.4)}{2} = 61.1 \text{ ft-kip}$$

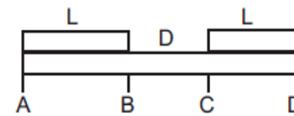
Table 1 – Moment Distribution [†]						
Joint	A	B		C		D
Member	AB	BA	BC	CB	CD	DC
DF	0.130	0.107	0.179	0.174	0.130	0.158
COF	0.500	0.500	0.500	0.500	0.500	0.500



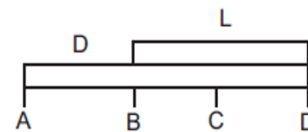
Load Pattern I (S2*)						
FEM	110.4	-110.4	39.8	-39.8	46.7	-46.7
Dist	-14.4	7.6	12.6	-1.2	-0.9	7.4
CO	3.8	-7.2	-0.6	6.3	3.7	-0.5
Dist	-0.5	0.8	1.4	-1.7	-1.3	0.1
CO	0.4	-0.2	-0.9	0.7	0.0	-0.7
Dist	-0.1	0.1	0.2	-0.1	-0.1	0.1
CO	0.1	0.0	-0.1	0.1	0.1	-0.1
Dist	0.0	0.0	0.0	0.0	0.0	0.0
M_u^-	99.7	-109.4	52.4	-35.7	48.1	-40.3
M_u^+	61.1		15.5		25.8	



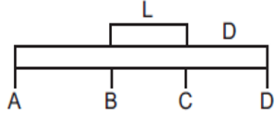
Load Pattern II (Odd*)						
FEM	110.4	-110.4	26.3	-26.3	70.7	-70.7
Dist	-14.4	9.0	15.0	-7.7	-5.8	11.2
CO	4.5	-7.2	-3.9	7.5	5.6	-2.9
Dist	-0.6	1.2	2.0	-2.3	-1.7	0.5
CO	0.6	-0.3	-1.1	1.0	0.2	-0.9
Dist	-0.1	0.2	0.3	-0.2	-0.2	0.1
CO	0.1	0.0	-0.1	0.1	0.1	-0.1
Dist	0.0	0.0	0.0	0.0	0.0	0.0
M_u^-	100.5	-107.6	38.4	-27.8	68.9	-62.7
M_u^+	61.6		6.2		40.2	



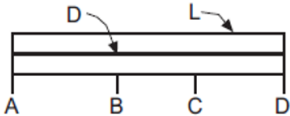
Load Pattern III (S3*)						
FEM	72.9	-72.9	39.8	-39.8	70.7	-70.7
Dist	-9.5	3.6	5.9	-5.4	-4.0	11.2
CO	1.8	-4.8	-2.7	3.0	5.6	-2.0
Dist	-0.2	0.8	1.3	-1.5	-1.1	0.3
CO	0.4	-0.1	-0.7	0.7	0.2	-0.6
Dist	-0.1	0.1	0.2	-0.1	-0.1	0.1
CO	0.0	0.0	-0.1	0.1	0.0	-0.1
Dist	0.0	0.0	0.0	0.0	0.0	0.0
M_u^-	65.3	-73.4	43.7	-43.1	71.2	-61.7
M_u^+	40.0		16.3		39.5	


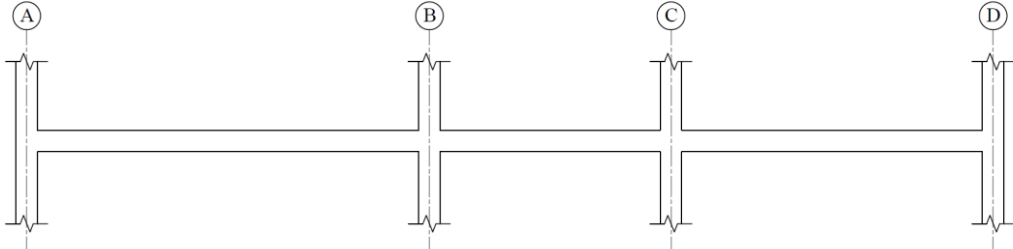


Load Pattern IV (Even*)						
FEM	72.9	-72.9	39.8	-39.8	46.7	-46.7
Dist	-9.5	3.6	5.9	-1.2	-0.9	7.4
CO	1.8	-4.8	-0.6	3.0	3.7	-0.5
Dist	-0.2	0.6	1.0	-1.2	-0.9	0.1
CO	0.3	-0.1	-0.6	0.5	0.0	-0.4
Dist	0.0	0.1	0.1	-0.1	-0.1	0.1
CO	0.0	0.0	0.0	0.1	0.0	0.0
Dist	0.0	0.0	0.0	0.0	0.0	0.0
M_u^-	65.2	-73.6	45.5	-38.7	48.6	-40.1
M_u^+	40.0		17.5		25.7	



Load Pattern V (All*)						
FEM	110.4	-110.4	39.8	-39.8	70.7	-70.7
Dist	-14.4	7.6	12.6	-5.4	-4.0	11.2
CO	3.8	-7.2	-2.7	6.3	5.6	-2.0
Dist	-0.5	1.1	1.8	-2.1	-1.6	0.3
CO	0.5	-0.2	-1.0	0.9	0.2	-0.8
Dist	-0.1	0.1	0.2	-0.2	-0.1	0.1
CO	0.1	0.0	-0.1	0.1	0.1	-0.1
Dist	0.0	0.0	0.0	0.0	0.0	0.0
M_u^-	99.8	-109.1	50.6	-40.1	70.7	-61.9
M_u^+	61.1		14.3		39.7	



Envelope of Maximum Moments						
						
Max M_u^- Column Center Line	100.5		-109.4	52.4	-43.1	71.2
Max M_u^- Column Face	83.5		-91.9	41.6	-33.0	57.2
Max M_u^+ Midspan		61.6		17.6		40.2

‡ Moments units are kip-ft
* Live load pattern designation in [spBeam](#)

2. Moment Redistribution

Now that the structural analysis is completed for all applicable live load patterns, and the enveloped moments are determined we can evaluate the impact of moment redistribution.

Moment redistribution is dependent on adequate ductility in plastic hinge regions. Plastic hinge regions develop at sections of maximum positive or negative moment and cause a shift in the elastic moment diagram. The usual result is a reduction in the values of maximum negative moments in the support regions and an increase in the values of positive moments between supports from those computed by elastic analysis. However, because negative moments are determined for one loading arrangement and positive moments for another, economies in reinforcement can sometimes be realized (depending on the load pattern) by reducing maximum elastic positive moments and increasing negative moments, thus narrowing the envelope of maximum negative and positive moments at any section in the span. The plastic hinges permit the utilization of the full capacity of more cross sections of a flexural member at ultimate loads. ACI 318-14 (R6.6.5)

The ACI code allows the reduction of factored moments calculated by elastic theory at sections of maximum negative or maximum positive moment in any span of continuous flexural members for any assumed loading arrangement by a percentage equal to $1000 \epsilon_t$ up to a maximum of 20 percent. ACI 318-14 (6.6.5.3)

Redistribution of moments shall be made only when ϵ_t is equal to or greater than 0.0075 at the section at which moment is reduced. ACI 318-14 (6.6.5.1)

Static equilibrium shall be maintained after redistribution of moments for each loading arrangement. The reduced moment shall be used for calculating redistributed moments at all other sections within the spans. ACI 318-14 (6.6.5.4)

2.1. Reduction percentage calculations

Using $d = 14.0$ in. and cover = 1.5 in.

Calculate the coefficient of resistance using the following equation:

$$\frac{R_n}{f_c'} = \frac{M_u}{\phi \times f_c' \times b \times d^2} \quad \text{PCA Notes on ACI 318-11 (8.4 Eq. 2)}$$

Calculate the net tensile strain (ϵ_t) using the following equation:

$$\epsilon_t = 0.003 \left(\frac{\beta_1}{1 - \sqrt{1 - \frac{40}{17} \times \frac{R_n}{f_c'}}} - 1 \right) \quad \text{PCA Notes on ACI 318-11 (8.4 Eq. 8)}$$

For M_u use envelope value at support face. Based ϵ_t calculate the adjustment. Iterate until the adjusted moments converge (start repeating) as follows: (see the following table)

For negative moment at support D:

First Iteration

$$(M_u)_1 = 49.3 \text{ kip-ft}$$

$$\left(\frac{R_n}{f_c'}\right)_1 = \frac{49.3 \times 12}{0.9 \times 4 \times 12 \times 14^2} = 0.0699$$

$$(\varepsilon_t)_1 = 0.003 \left(\frac{0.85}{1 - \sqrt{1 - \frac{40}{17} \times 0.0699}} - 1 \right) = 0.0267$$

$$\text{Adjustment}_1 = 1000 \times \varepsilon_t = 1000 \times 0.0267 = 26.7 > 20 \rightarrow \text{Adjustment}_1 = 20\%$$

Second Iteration

$$(M_u)_2 = 49.3 - 49.3 \times 0.2 = 39.4 \text{ kip-ft}$$

$$\left(\frac{R_n}{f_c'}\right)_2 = \frac{39.4 \times 12}{0.9 \times 4 \times 12 \times 14^2} = 0.0559$$

$$(\varepsilon_t)_2 = 0.003 \left(\frac{0.85}{1 - \sqrt{1 - \frac{40}{17} \times 0.0559}} - 1 \right) = 0.0345$$

$$\text{Adjustment}_2 = 1000 \times \varepsilon_t = 1000 \times 0.0345 = 34.5 > 20 \rightarrow \text{Adjustment}_2 = 20\%$$

Since $\text{Adjustment}_1 = \text{Adjustment}_2 \rightarrow$ End of Iterations

		Support					
		A	B		C		D
		Right	Left	Right	Left	Right	Left
Iteration 1	M_u , ft-kip	83.5	91.9	41.6	33	57.2	49.3
	R_n/f_c'	0.118	0.13	0.059	0.047	0.081	0.07
	ϵ_t , in./in.	0.014	0.012	0.033	0.042	0.022	0.027
	Adjustment, %	13.9	12.2	20	20	20	20
Iteration 2	M_u , ft-kip	71.9	80.7	33.3	26.4	45.8	39.4
	R_n/f_c'	0.102	0.114	0.047	0.037	0.065	0.056
	ϵ_t , in./in.	0.017	0.015	0.042	0.054	0.029	0.035
	Adjustment, %	16.9	14.6	20	20	20	20
Iteration 3	M_u , ft-kip	69.4	78.5				
	R_n/f_c'	0.098	0.111				
	ϵ_t , in./in.	0.018	0.015				
	Adjustment, %	17.7	15.1				
Iteration 4	M_u , ft-kip	68.8	78				
	R_n/f_c'	0.098	0.111				
	ϵ_t , in./in.	0.018	0.015				
	Adjustment, %	17.9	15.2				
Iteration 5	M_u , ft-kip	68.6	77.9				
	R_n/f_c'	0.097	0.11				
	ϵ_t , in./in.	0.018	0.015				
	Adjustment, %	17.9	15.3				
Iteration 6	M_u , ft-kip		77.9				
	R_n/f_c'		0.11				
	ϵ_t , in./in.		0.015				
	Adjustment, %		15.3				
Final Allowable Adjustment, %		17.9	15.3	20	20	20	20

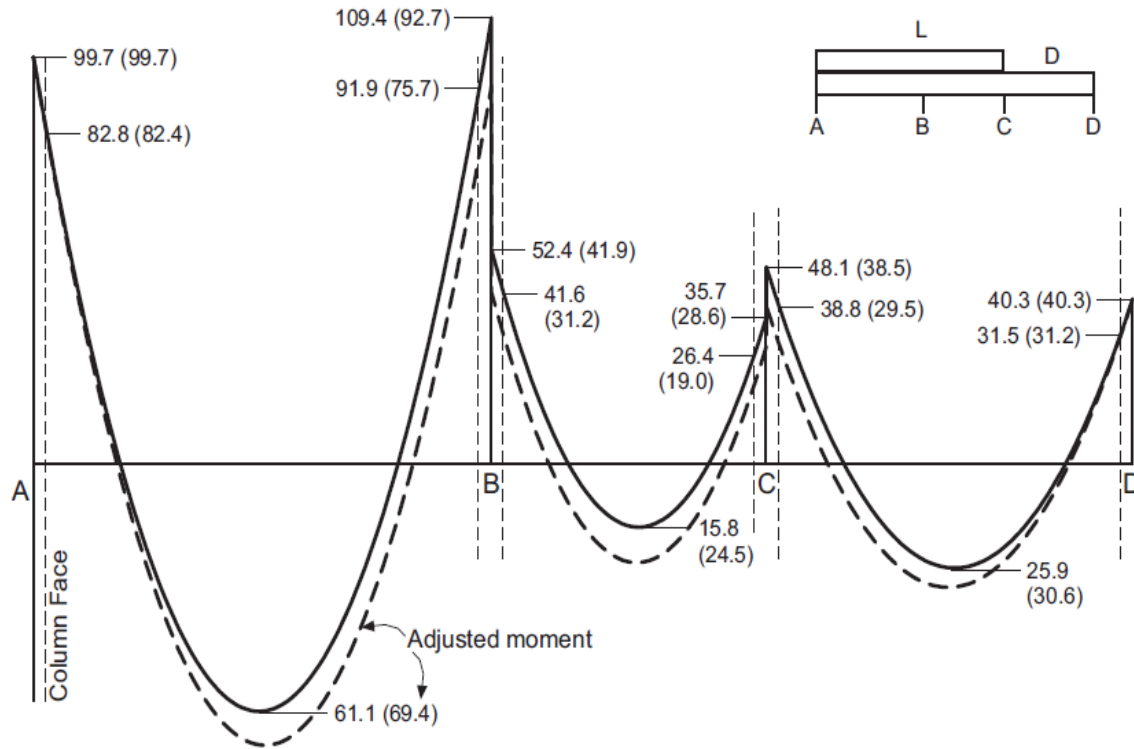
2.2. Adjustment of moments (redistribution)

Now the engineer can make decisions to reduce any negative moments (or positive) based on project parameters including:

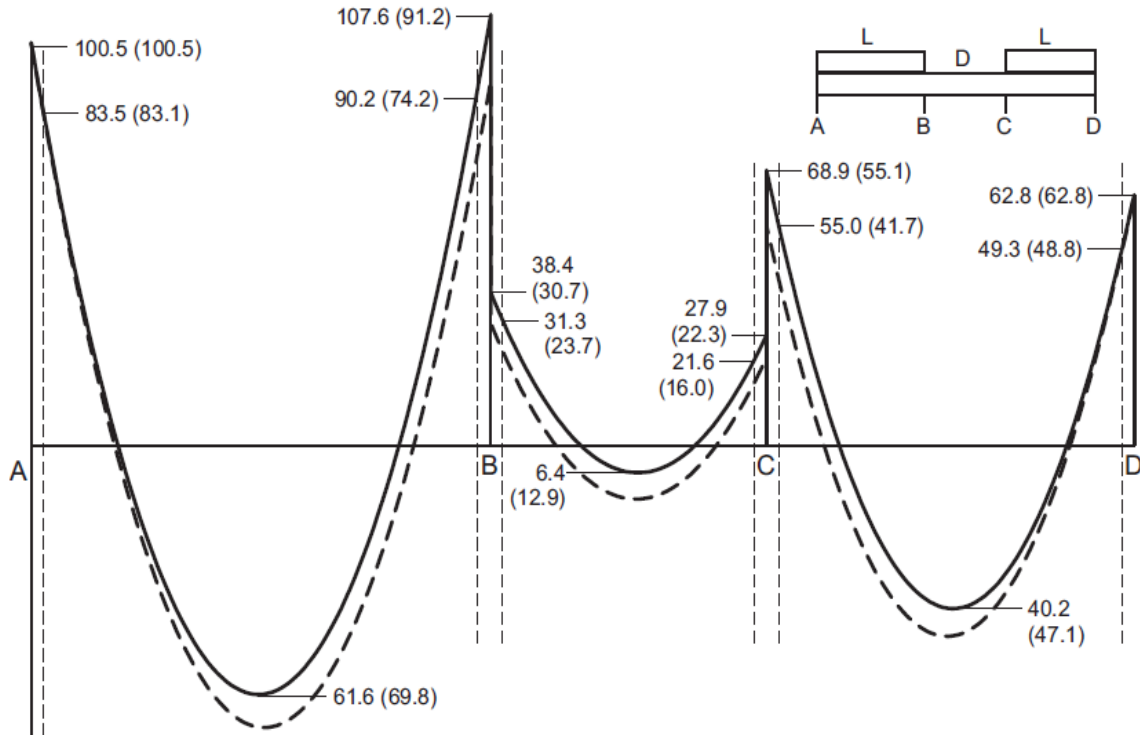
- Steel detailing and placement considerations.
- New design or investigation of existing beams
- Optimize the provided reinforcement for more economical design
- Optimize the provided reinforcement for improved uniformity

It was decided to reduce the negative moments on both sides of supports B and C and accept the increase in the corresponding positive moments, and not to adjust the negative moments at the exterior supports A and D.

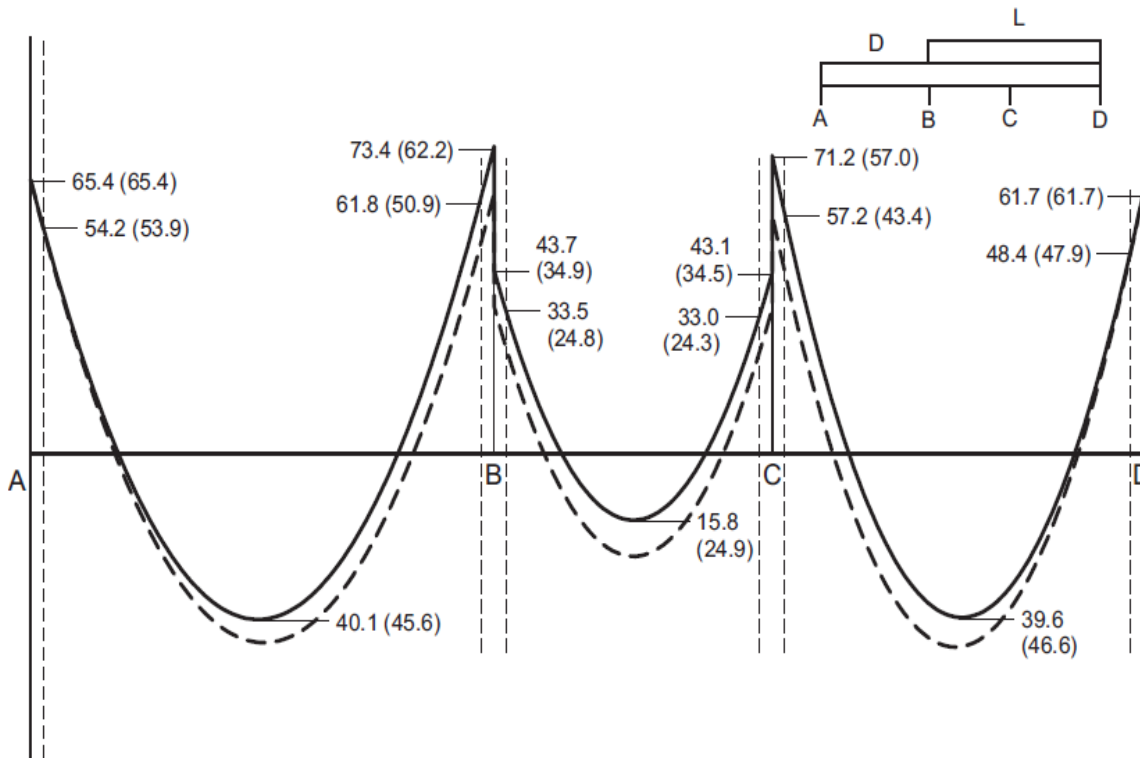
The following figures show the unadjusted and adjusted moment values at the columns centerlines, columns faces, and at the midspan for each load pattern and for the maximum values at each critical location (maximum moment envelopes).



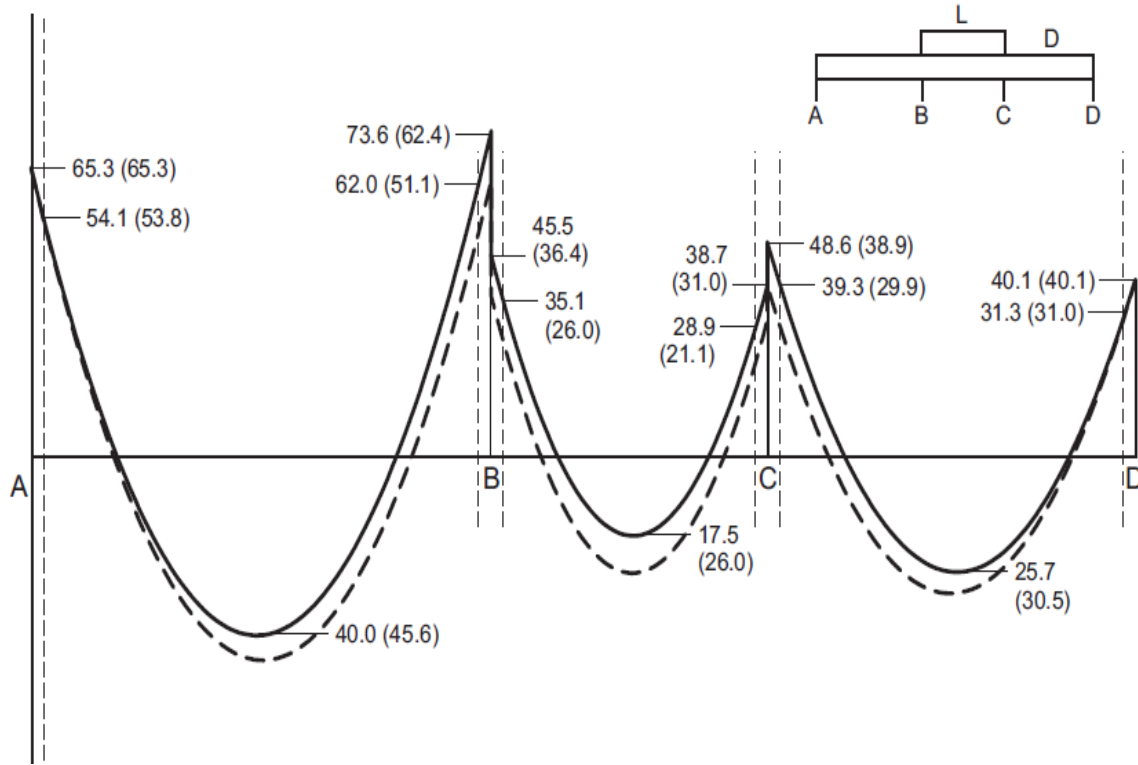
(a) Load Pattern I (moments in kip-ft)



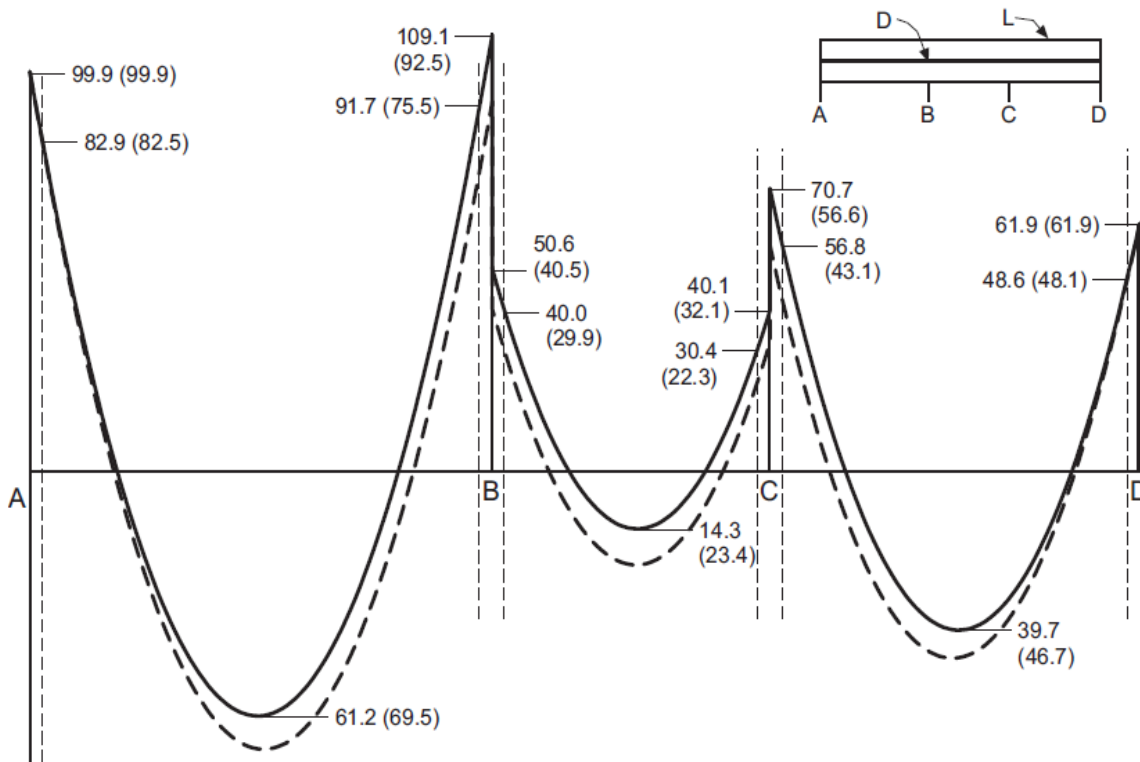
(b) Load Pattern II (moments in kip-ft)



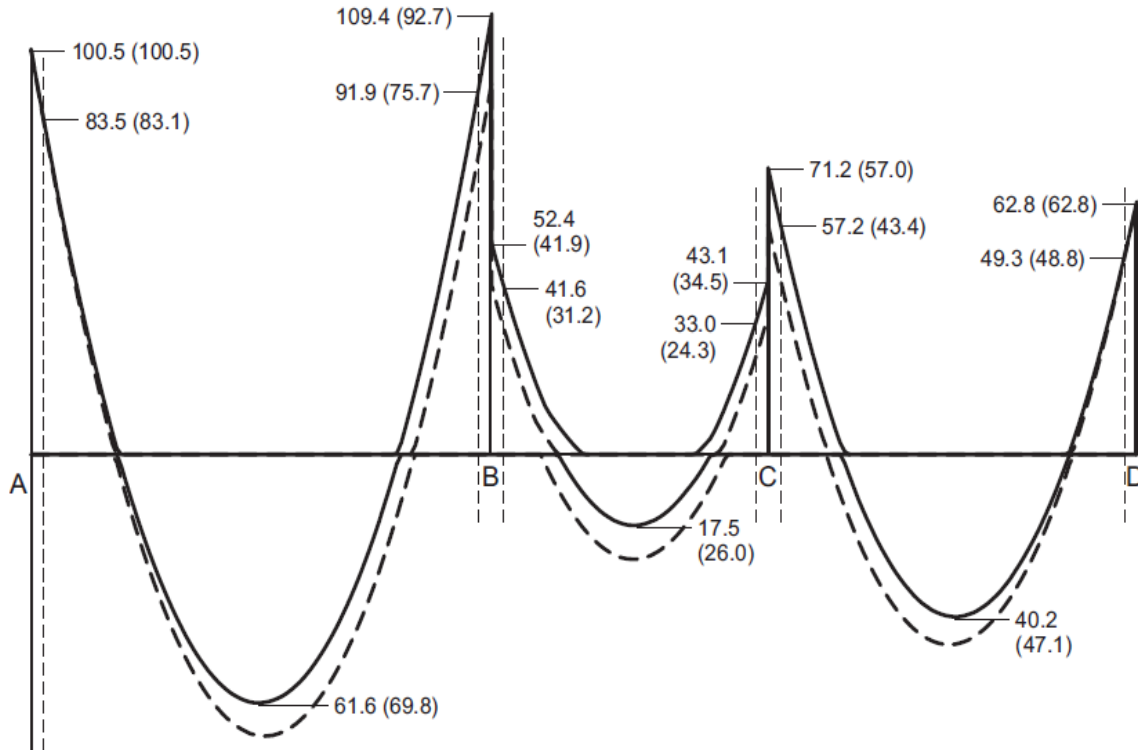
(c) Load Pattern III (moments in kip-ft)



(d) Load Pattern IV (moments in kip-ft)



(e) Load Pattern V (moments in kip-ft)



(f) Maximum Moment Envelopes for Pattern Loading (moments in ft-kips)

Figure 2 – Redistribution of Moments (All Load Patterns) (PCA Notes – Example 8-2)

For load pattern I

$$M_{B, \text{left}} = 109.4 \text{ kip-ft (adjustment} = 15.3\%)$$

$$\text{Adjusted } M_{B, \text{left}} = 109.4 - 109.4 \times 0.153 = 92.7 \text{ kip-ft}$$

Increase in positive moment in span A-B

$$M_A = 99.7 \text{ kip-ft}$$

$$\text{Adjusted } M_{B, \text{left}} = 92.7 \text{ kip-ft}$$

$$\text{Moment due to uniform load} = \frac{w_u \times l^2}{8} = \frac{2.12 \times 25^2}{8} = 165.6 \text{ kip-ft}$$

$$\text{Adjusted positive moment at mid-span} = 165.6 - \frac{99.7 + 92.7}{2} = 69.4 \text{ kip-ft}$$

Decrease in negative moment at the left face of support B

$$\text{Ordinate on line } M_A \text{ to } M_{B, \text{left}} = 99.7 + \frac{92.7 - 99.7}{25} \times 24.33 = 92.9 \text{ kip-ft}$$

$$\text{Moment due to uniform load} = \frac{1}{2} \times w_u \times x \times (l - x) = \frac{1}{2} \times 2.12 \times 24.33 \times (25 - 24.33) = 17.2 \text{ kip-ft}$$

$$\text{Adjusted negative moment at the left face of support B} = 92.9 - 17.2 = 75.7 \text{ kip-ft}$$

Similar calculations are made to determine the adjusted moment at other locations and for other load patterns. Results of the additional calculations are shown in the following table.

Location	Load Pattern I S2		Load Pattern II Odd		Load Pattern III S3		Load Pattern IV Even		Load Pattern V All	
	M _u	M _{adj}	M _u	M _{adj}	M _u	M _{adj}	M _u	M _{adj}	M _u	M _{adj}
A Center	-99.7	-99.7	-100.5	-100.5	-65.4	-65.4	-65.3	-65.3	-99.9	-99.9
A Right Face	-82.8	-82.4	-83.5	-83.1	-54.2	-53.9	-54.1	-53.8	-82.9	-82.5
Midspan A-B	61.1	69.4	61.6	69.8	40.1	45.6	40	45.6	61.2	69.5
B Left Face	-91.9	-75.7	-90.2	-74.2	-61.8	-50.9	-62	-51.1	-91.7	-75.5
B Left Center	-109.4	-92.7	-107.6	-91.2	-73.4	-62.2	-73.6	-62.4	-109.1	-92.5
B Right Center	-52.4	-41.9	-38.4	-30.7	-43.7	-34.9	-45.5	-36.4	-50.6	-40.5
B Right Face	-41.6	-31.2	-31.3	-23.7	-33.5	-24.8	-35.1	-26	-40	-29.9
Midspan B-C	15.8	24.5	6.4	12.9	15.8	24.9	17.5	26	14.3	23.4
C Left Face	-26.4	-19	-21.6	-16	-33	-24.3	-28.9	-21.1	-30.4	-22.3
C Left Center	-35.7	-28.6	-27.9	-22.3	-43.1	-34.5	-38.7	-31	-40.1	-32.1
C Right Center	-48.1	-38.5	-68.9	-55.1	-71.2	-57	-48.6	-38.9	-70.7	-56.6
C Right Face	-38.8	-29.5	-55	-41.7	-57.2	-43.4	-39.3	-29.9	-56.8	-43.1
Midspan C-D	25.9	30.6	40.2	47.1	39.6	46.6	25.7	30.5	39.7	46.7
D Left Face	-31.5	-31.2	-49.3	-48.8	-48.4	-47.9	-31.3	-31	-48.6	-48.1
D Center	-40.3	-40.3	-62.8	-62.8	-61.7	-61.7	-40.1	-40.1	-61.9	-61.9

Final design moments after redistribution for critical sections (left and right support face & midspan)

After the adjusted bending moments have been determined analytically, the adjusted bending moment diagrams for each load pattern can be determined. The adjusted moment curves were determined graphically and are indicated by the dashed lines in Figures 2 (a) through (e).

An Adjusted maximum moment envelope can now be obtained from the adjusted moment curves as shown in Figure 2 (f) by dashed lines.

From the redistribution moment envelopes of Figure 2 (f), the design factored moments and the required reinforcement area are obtained as shown in following table. Check example “[One-Way Wide Module \(Skip\) Joist Concrete Floor System Design](#)” for detailed calculations for flexural and shear design of continuous beams.

Location		Moment at column face, kip-ft		Load Case	A _s , in. ²		
		Undistributed	Redistributed		Undistributed	Redistributed	%
Support A	Right	-83.5	-83.1	II	1.43	1.43	100.0
Midspan A-B		61.6	69.8	II	1.04	1.18	113.5
Support B	Left	-91.9	-75.7	I	1.59	1.29	81.1
	Right	-41.6	-31.2	I	0.68	<i>0.51</i>	75.0
Midspan B-C		17.6	26	IV	<i>0.28</i>	<i>0.42</i>	150.0
Support C	Left	-33	-24.4	III	<i>0.54</i>	<i>0.39</i>	72.2
	Right	-57.2	-43.5	III	0.96	0.72	75.0
Midspan C-D		40.2	47.1	II	0.66	0.78	118.2
Support D	Left	-49.3	-48.8	II	0.81	0.81	100.0

Italic underlined values indicate A_{s,min} governs

$$\text{Where } A_{s,\min} = \max \left\{ \begin{array}{l} \frac{3 \times \sqrt{f'_c}}{f_y} \\ \frac{200}{f_y} \end{array} \right\} b_w \times d = \max \left\{ \begin{array}{l} 0.0032 \\ 0.0033 \end{array} \right\} \times 12 \times 14 = 0.56 \text{ in.}^2 \quad \underline{\underline{ACI 318-14 (9.6.1.2)}}$$

3. Continuous Beam Analysis and Design Using Moment Redistribution – spBeam Software

[spBeam](#) is widely used for analysis, design and investigation of beams, and one-way slab systems (including standard and wide module joist systems) per latest American (ACI 318-14) and Canadian (CSA A23.3-14) codes. [spBeam](#) can be used for new designs or investigation of existing structural members subjected to flexure, shear, and torsion loads. With capacity to integrate up to 20 spans and two cantilevers of wide variety of floor system types, [spBeam](#) is equipped to provide cost-effective, accurate, and fast solutions to engineering challenges.

[spBeam](#) provides top and bottom bar details including development lengths and material quantities, as well as live load patterning and immediate and long-term deflection results. Using the moment redistribution feature engineers can deliver safe designs with savings in materials and labor. Engaging this feature allows up to 20% reduction of negative moments over supports reducing reinforcement congestions in these areas.

Redistribution of negative moments applies to one-way and beam systems only. It can be engaged using the “*Input Redistribution*” option on the “*Solve Options*” tab in the “*General Information*” dialog box (see the following figure). The program allows for redistribution of negative moments at supports. Only reduction in negative moments is considered. Increase of negative moments at the support is not taken into account even though it is allowed by the code. Static equilibrium is maintained meaning that bending moments and shear forces along the span are adjusted in accordance with the reduction of moments applied at the supports.

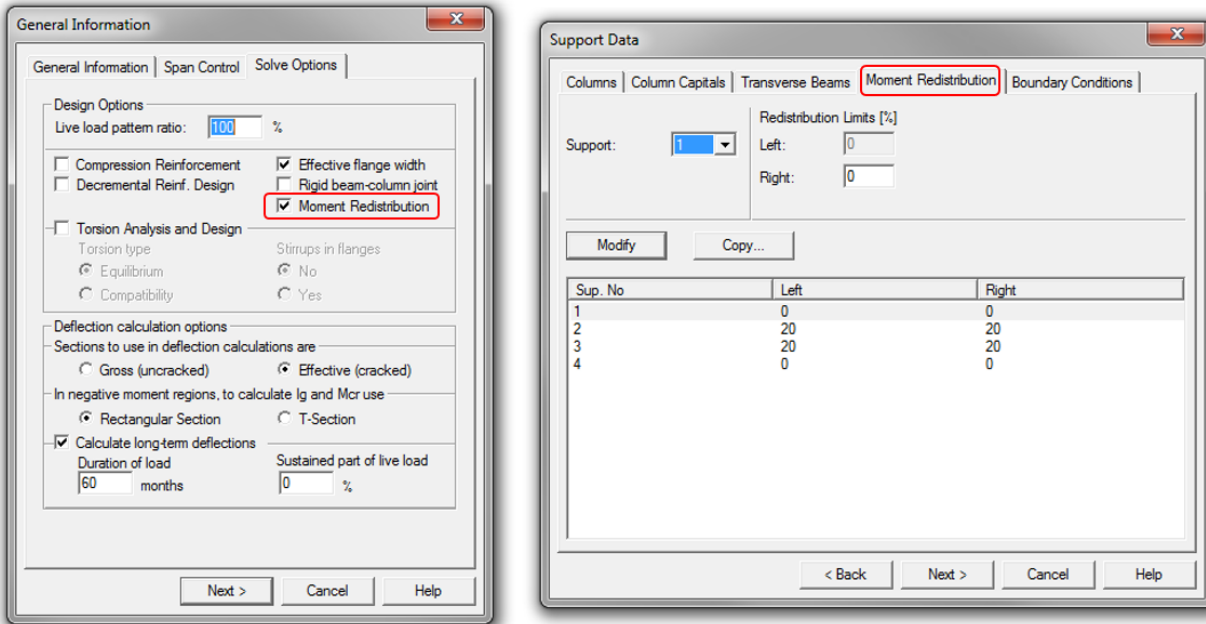


Figure 3 –Activating Moment Redistribution (spBeam)

From elastic static analysis, the largest moments from all load combinations and load patterns are determined at support faces on both ends of each span except cantilevers. These moments are used to calculate the maximum code allowable adjustment percentage of calculated moment.

In the investigation mode, program uses the area of provided reinforcement to obtain redistribution factors. In the design mode the required reinforcement area is used. The reduction percentage is limited to 20% and not to exceed the maximum values specified by the user. Negative moments at span ends are reduced by the amount of redistribution factors and new moment values are iteratively used to obtain new redistribution factors. This iterative procedure is repeated until the change in distribution factor is negligible (does not exceed 0.01%), but no more than 10 times.

For illustration and comparison purposes, the following figures provide a sample of the results obtained from an [spBeam](#) model created for the continuous beam in this example. Special emphasis can be given to Figure 7 that illustrated the maximum and adjusted moments for span 2.

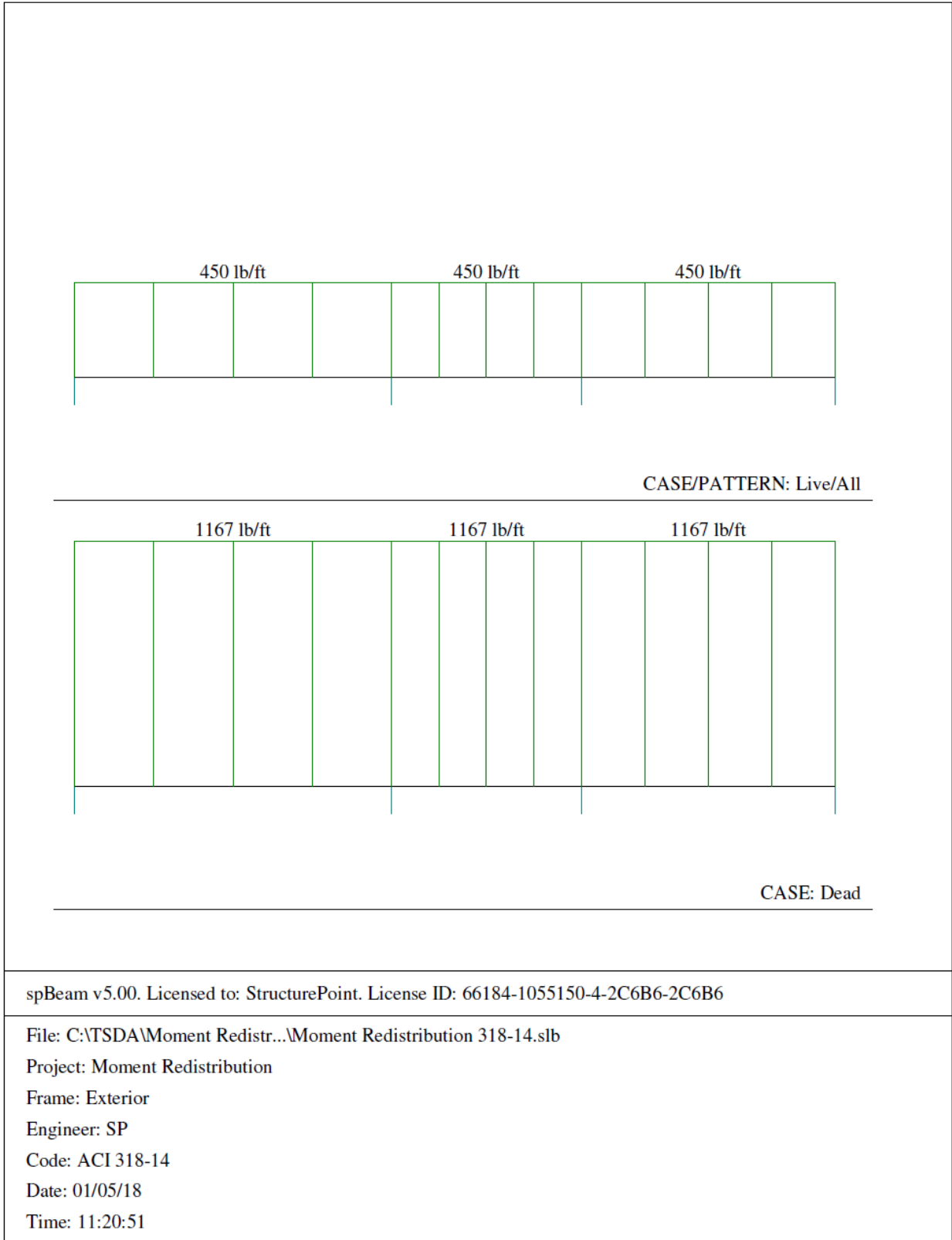
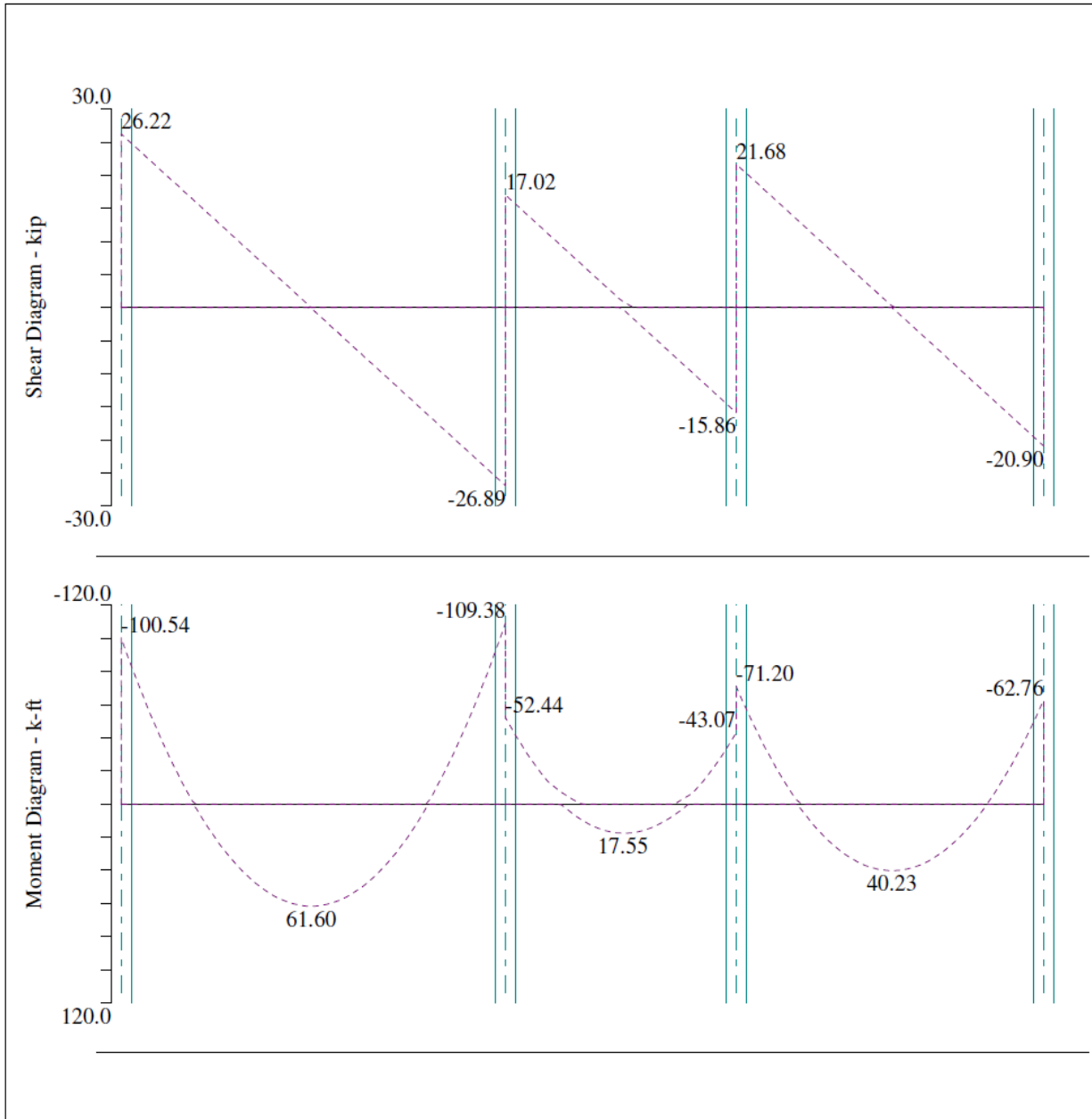


Figure 4 – Loading (spBeam)



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File: C:\TSDA\Moment Redistr...\Moment Redistribution 318-14.slb

Project: Moment Redistribution

Frame: Exterior

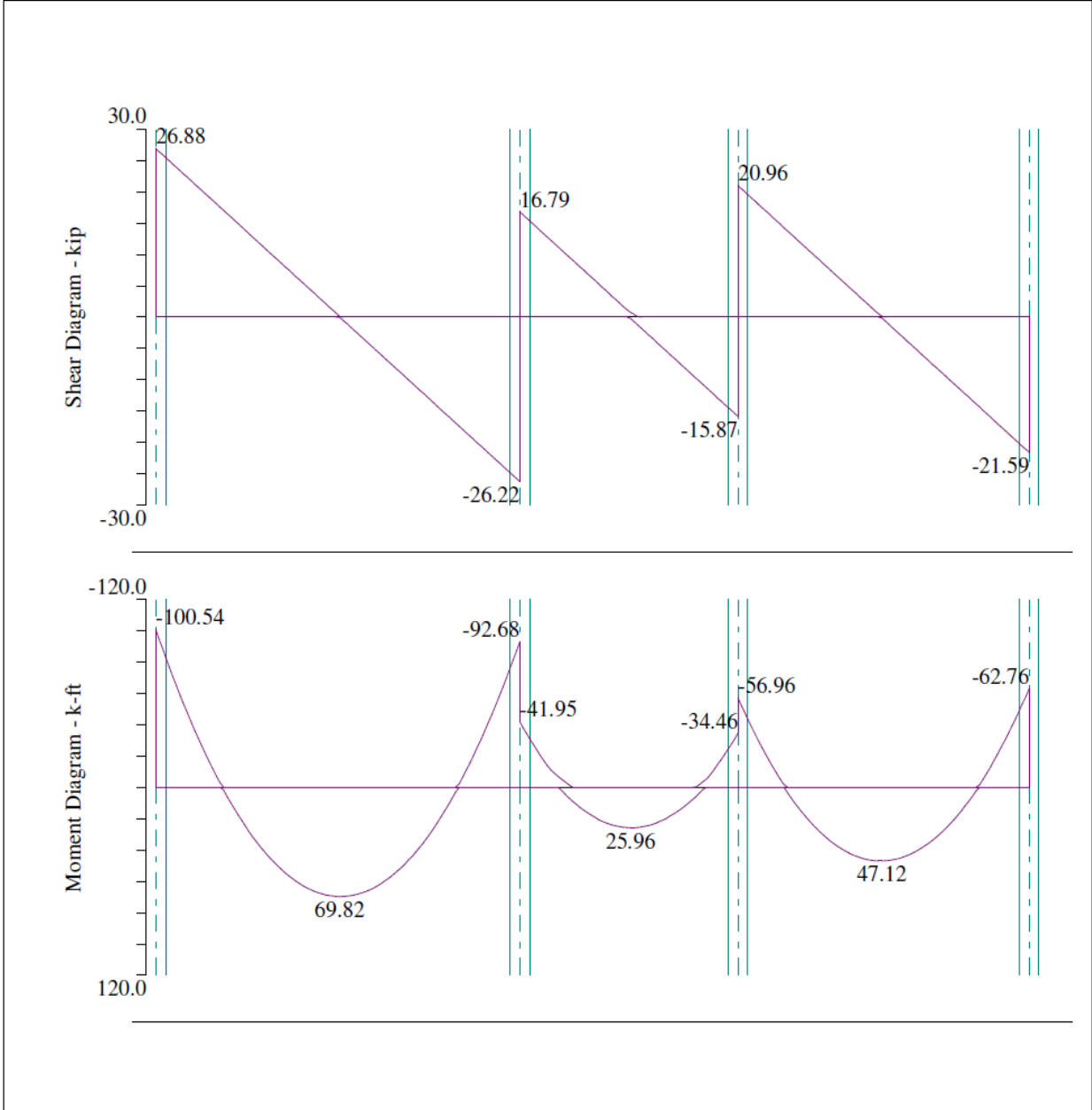
Engineer: SP

Code: ACI 318-14

Date: 01/05/18

Time: 11:29:44

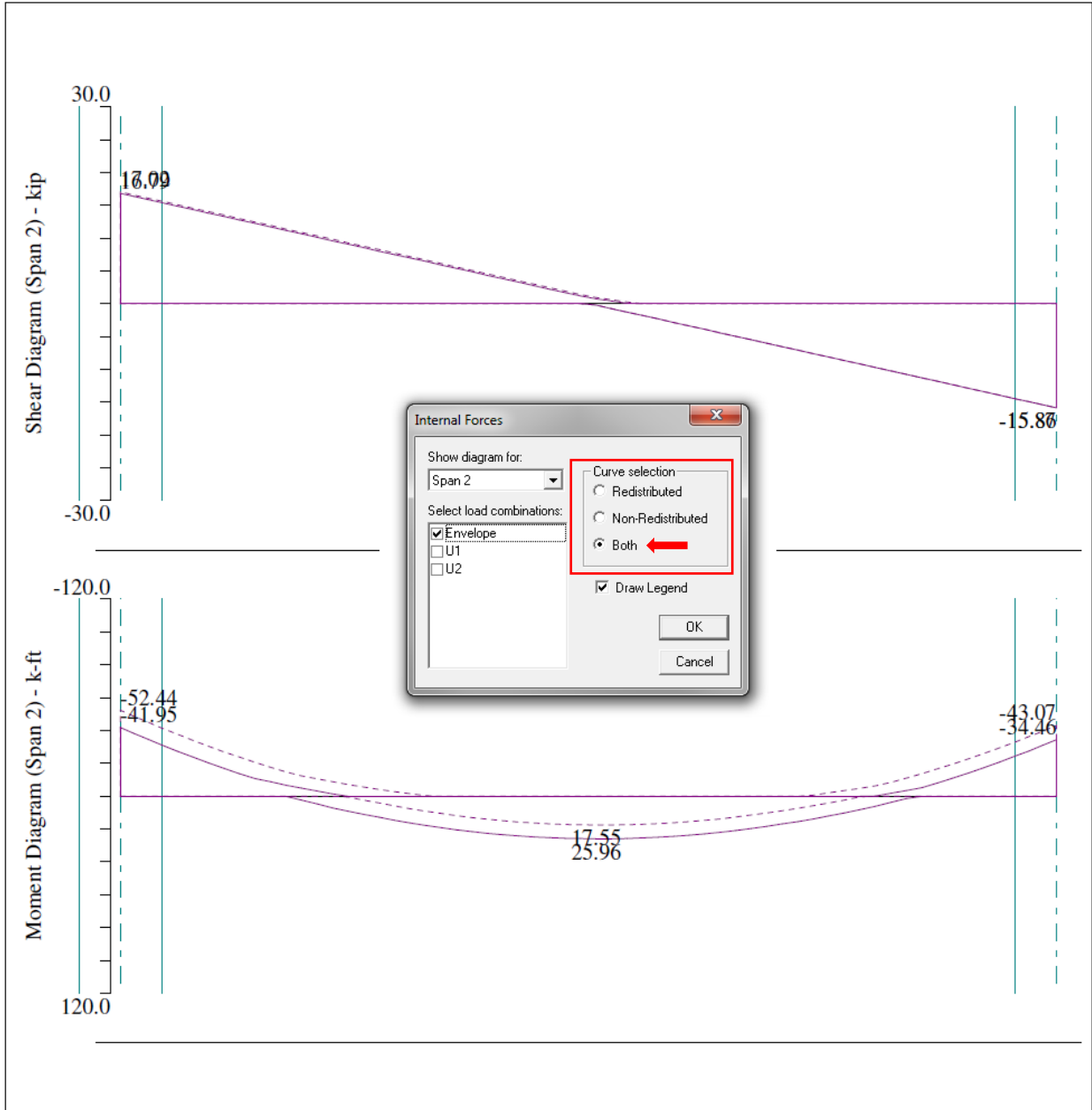
Figure 5 – Internal Forces before Moment Redistribution (spBeam)



spBeam v5.00. Licensed to: StructurePoint. License ID: 66184-1055150-4-2C6B6-2C6B6

File: C:\TSDA\Moment Redistr...\Moment Redistribution 318-14.slb
 Project: Moment Redistribution
 Frame: Exterior
 Engineer: SP
 Code: ACI 318-14
 Date: 01/05/18
 Time: 11:19:50

Figure 6 – Internal Forces after Moment Redistribution (spBeam)



spBeam v5.00. Licensed to: StructurePoint. License ID: 66184-1055150-4-2C6B6-2C6B6

File: C:\TSDA\Moment Redistr...\Moment Redistribution 318-14.slb

Project: Moment Redistribution

Frame: Exterior

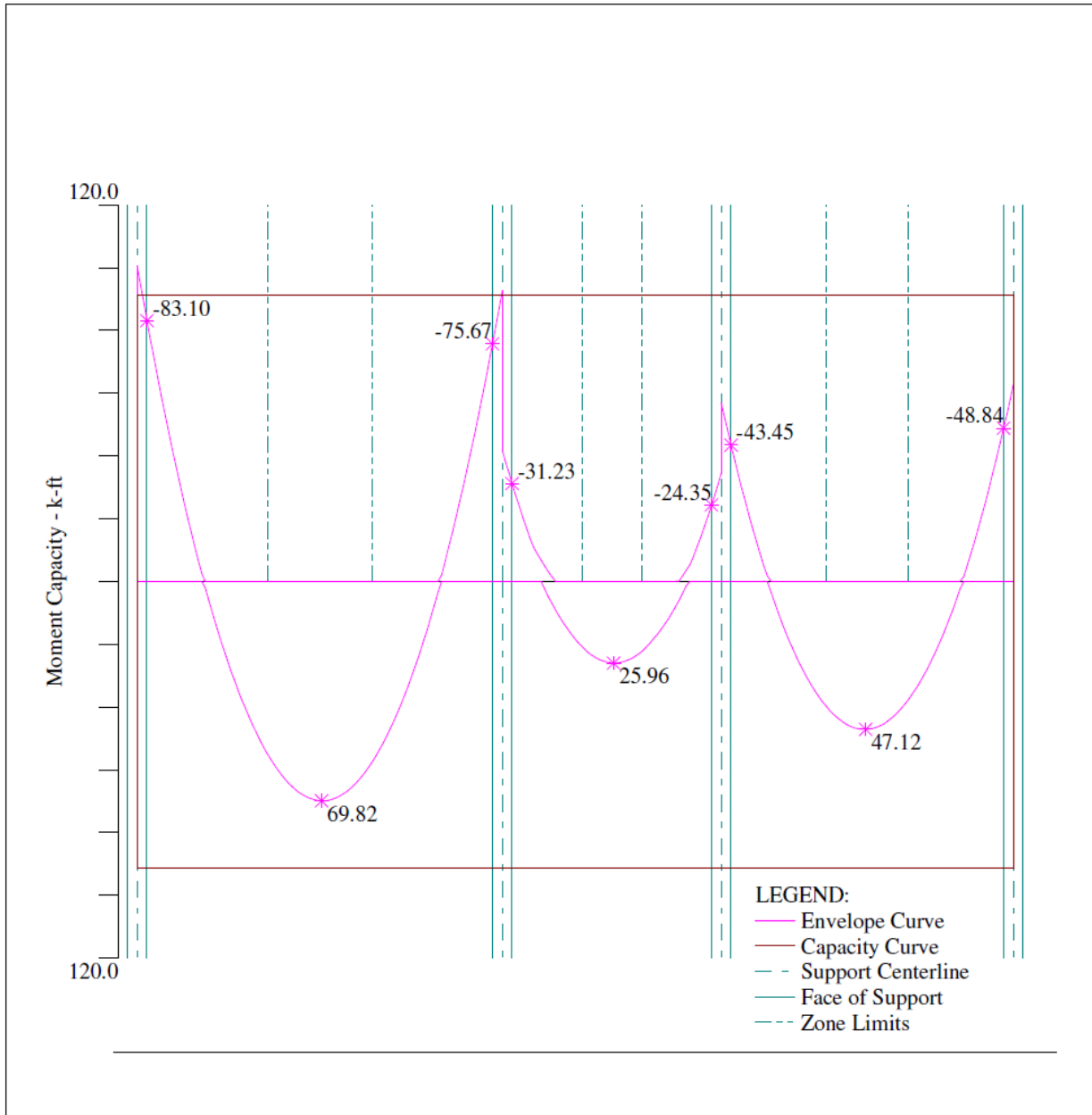
Engineer: SP

Code: ACI 318-14

Date: 01/05/18

Time: 11:33:37

Figure 7 – Internal Forces before and after Moment Redistribution for Span 2 (spBeam)



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Project: Moment Redistribution

Frame: Exterior

Engineer: SP

Code: ACI 318-14

Date: 01/05/18

Time: 11:21:46

Figure 8 – Moment Capacity Diagram after Moment Redistribution (spBeam)

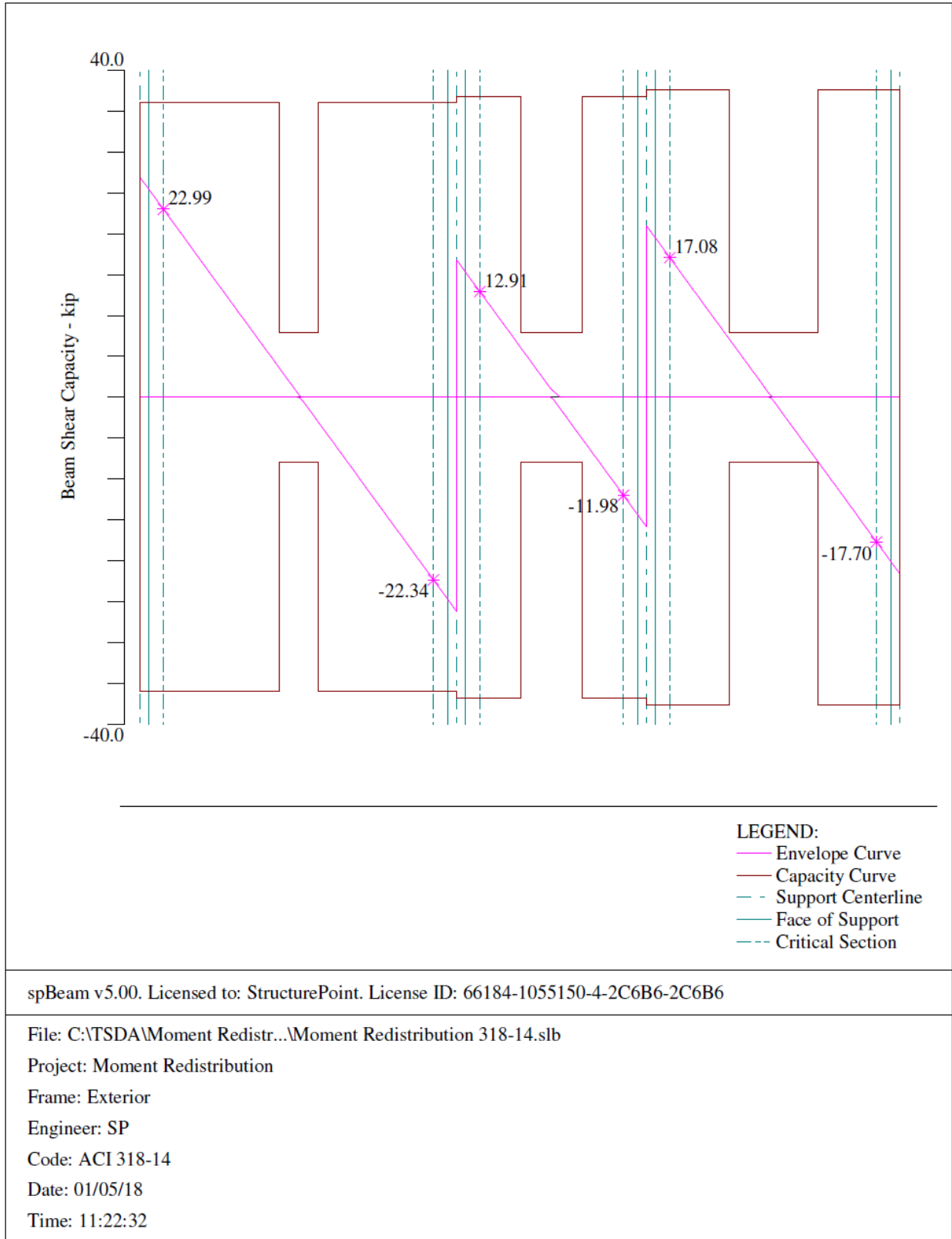


Figure 9 – Shear Capacity Diagram after Moment Redistribution ([spBeam](#))

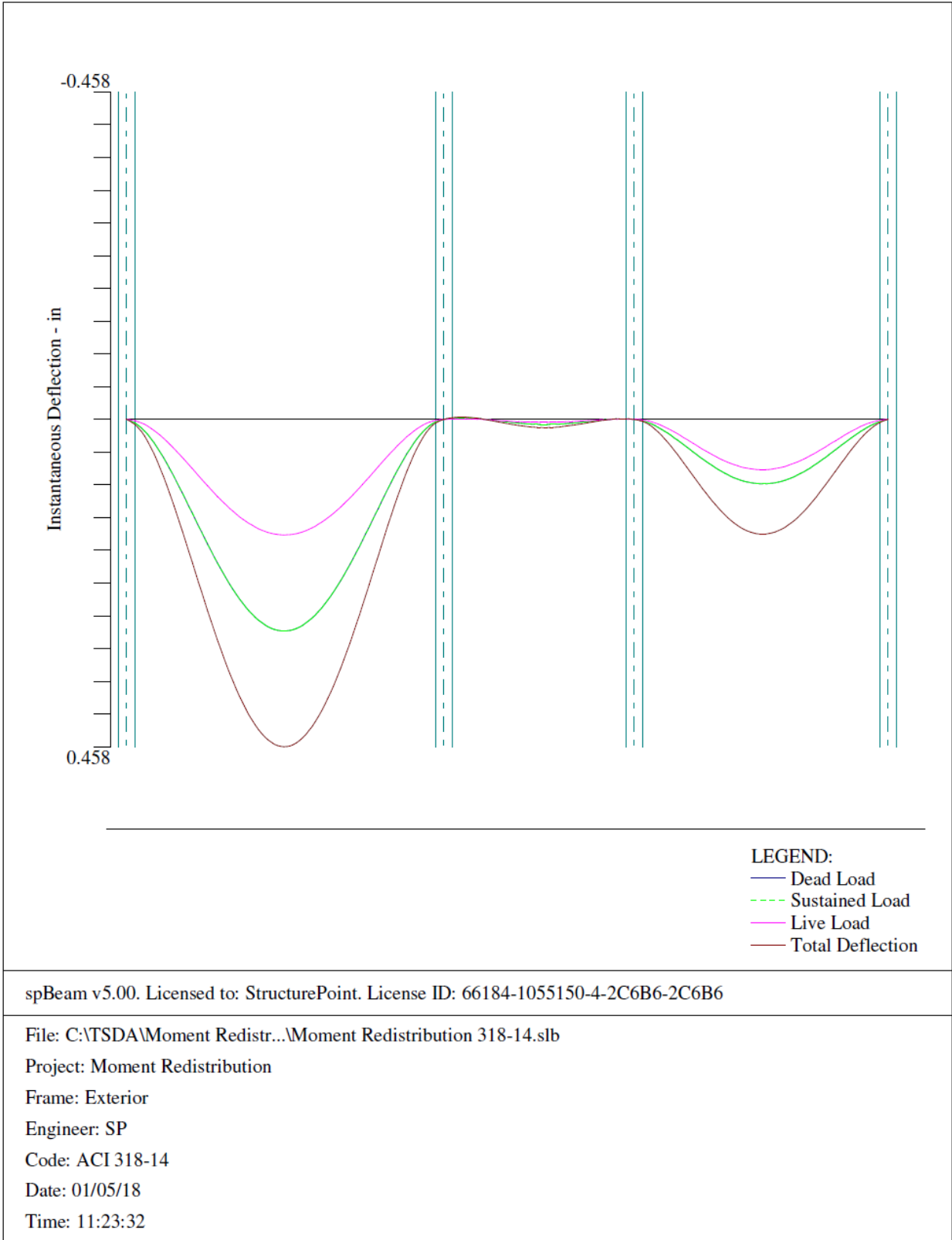


Figure 10 – Immediate Deflection Diagram (spBeam)

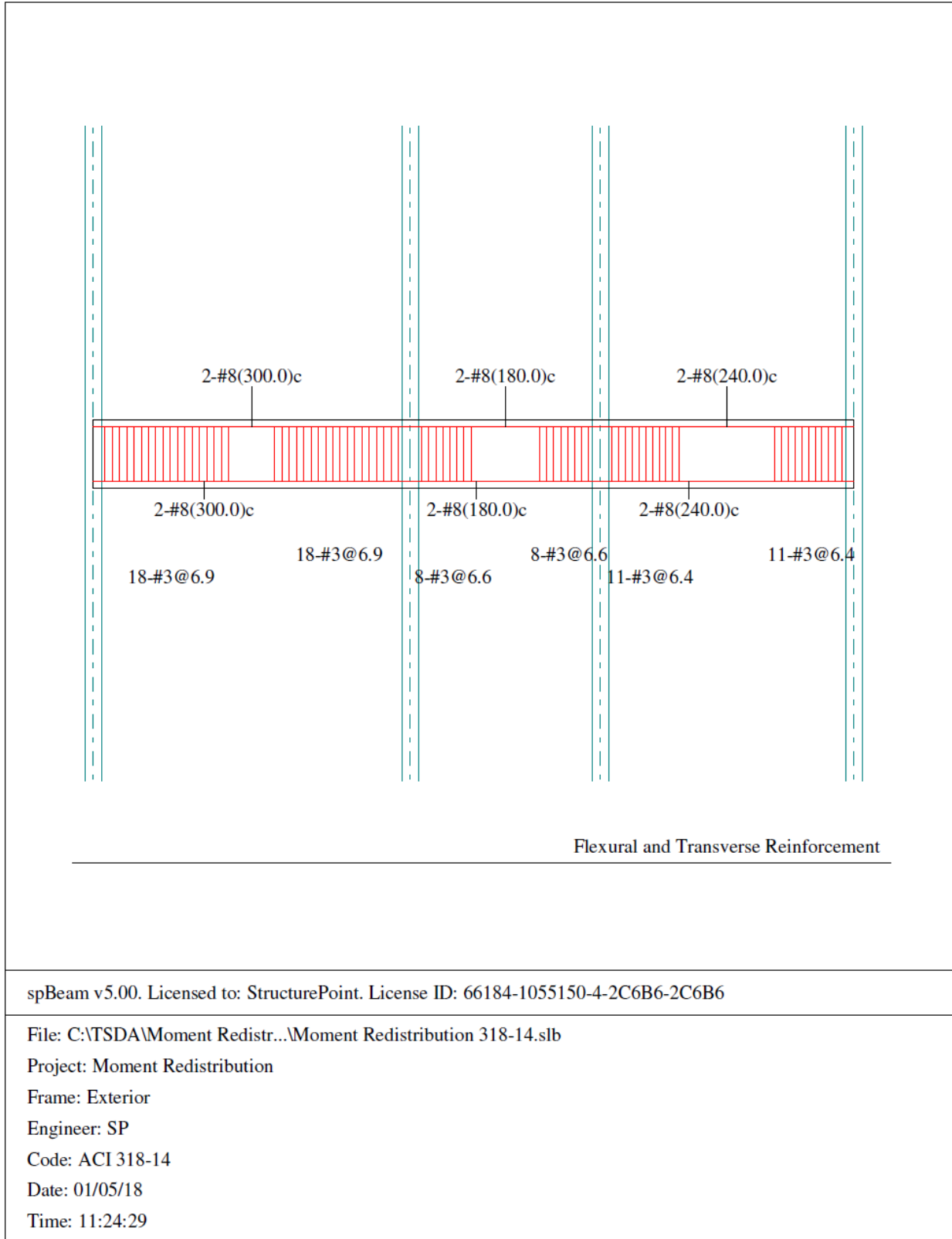


Figure 11 – Reinforcement after Moment Redistribution ([spBeam](#))

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                        spBeam v5.00 (TM)
A Computer Program for Analysis, Design, and Investigation of
Reinforced Concrete Beams and One-way Slab Systems
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```

=====
[1] INPUT ECHO
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General Information

```

=====
File name: C:\TSDA\Moment Redistribution\Moment Redistribution 318-14.slb
Project: Moment Redistribution
Frame: Exterior
Engineer: SP
Code: ACI 318-14
Reinforcement Database: ASTM A615
Mode: Design
Number of supports = 4
Floor System: One-Way/Beam

Live load pattern ratio = 100%
Deflections are based on cracked section properties.
In negative moment regions, Ig and Mcr DO NOT include flange/slab contribution (if available)
Long-term deflections are calculated for load duration of 60 months.
0% of live load is sustained.
Compression reinforcement calculations NOT selected.
Default incremental rebar design selected.
Moment redistribution selected.
Effective flange width calculations selected.
Rigid beam-column joint NOT selected.
Torsion analysis and design NOT selected.
    
```

Material Properties

```

=====
          Slabs|Beams          Columns
          -----          -----
wc =          150          150 lb/ft3
f'c =           4           4 ksi
Ec =        3834.3        3834.3 ksi
fr =         0.47434         0.47434 ksi

fy =           60 ksi, Bars are not epoxy-coated
fyt =          60 ksi
Es =        29000 ksi
    
```

Reinforcement Database

```

=====
Units: Db (in), Ab (in^2), Wb (lb/ft)
Size  Db    Ab    Wb  Size  Db    Ab    Wb
-----
#3    0.38  0.11  0.38  #4    0.50  0.20  0.67
#5    0.63  0.31  1.04  #6    0.75  0.44  1.50
#7    0.88  0.60  2.04  #8    1.00  0.79  2.67
#9    1.13  1.00  3.40  #10   1.27  1.27  4.30
#11   1.41  1.56  5.31  #14   1.69  2.25  7.65
#18   2.26  4.00  13.60
    
```

Span Data

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Slabs

Units: L1, wL, wR (ft); t, bEff, Hmin (in)

Span	Loc	L1	t	wL	wR	bEff	Hmin
1	ExtL	25.000	0.00	0.500	0.500	12.00	0.00
2	ExtL	15.000	0.00	0.500	0.500	12.00	0.00
3	ExtL	20.000	0.00	0.500	0.500	12.00	0.00

Ribs and Longitudinal Beams

Units: b, h, Sp (in)

Span	Ribs			Beams		Span Hmin
	b	h	Sp	b	h	
1	0.00	0.00	0.00	12.00	16.00	16.22 *b
2	0.00	0.00	0.00	12.00	16.00	8.57
3	0.00	0.00	0.00	12.00	16.00	12.97

NOTES:
*b - Span depth is less than minimum. Deflection check required.

Support Data

Columns

Units: c1a, c2a, clb, c2b (in); Ha, Hb (ft)

Supp	c1a	c2a	Ha	clb	c2b	Hb	Red%
1	16.00	16.00	10.000	16.00	16.00	10.000	100
2	16.00	16.00	10.000	16.00	16.00	10.000	100
3	16.00	16.00	10.000	16.00	16.00	10.000	100
4	16.00	16.00	10.000	16.00	16.00	10.000	100

Moment Redistribution Limits

Supp	Left[%]	Right[%]
1	0	0
2	20	20
3	20	20
4	0	0

Boundary Conditions

Units: Kz (kip/in); Kry (kip-in/rad)

Supp	Spring Kz	Spring Kry	Far End A	Far End B
1	0	0	Fixed	Fixed
2	0	0	Fixed	Fixed
3	0	0	Fixed	Fixed
4	0	0	Fixed	Fixed

Load Data

Load Cases and Combinations

Case Type	Dead DEAD	Live LIVE
U1	1.400	0.000
U2	1.200	1.600

Line Loads

Units: Wa, Wb (lb/ft), La, Lb (ft)

Case/Patt	Span	Wa	La	Wb	Lb
Dead	1	1167.00	0.000	1167.00	25.000
	2	1167.00	0.000	1167.00	15.000
	3	1167.00	0.000	1167.00	20.000
Live	3	450.00	0.000	450.00	20.000
	2	450.00	0.000	450.00	15.000
	1	450.00	0.000	450.00	25.000
Live/Odd	3	450.00	0.000	450.00	20.000
	1	450.00	0.000	450.00	25.000
Live/Even	2	450.00	0.000	450.00	15.000
Live/S1	1	450.00	0.000	450.00	25.000
Live/S2	2	450.00	0.000	450.00	15.000
Live/S3	1	450.00	0.000	450.00	25.000
	3	450.00	0.000	450.00	20.000
Live/S4	2	450.00	0.000	450.00	15.000
	3	450.00	0.000	450.00	20.000

Reinforcement Criteria

Slabs and Ribs

_____Top bars_____Bottom bars_____

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	Min	Max	Min	Max
Bar Size	#8	#8	#8	#8
Bar spacing	1.00	18.00	1.00	18.00 in
Reinf ratio	0.14	5.00	0.14	5.00 %
Cover	1.50		1.50	in

There is NOT more than 12 in of concrete below top bars.

Beams

	Top bars		Bottom bars		Stirrups	
	Min	Max	Min	Max	Min	Max
Bar Size	#8	#8	#8	#8	#3	#3
Bar spacing	1.00	18.00	1.00	18.00	6.00	18.00 in
Reinf ratio	0.14	5.00	0.14	5.00 %		
Cover	1.50		1.50			in
Layer dist.	1.00		1.00			in
No. of legs					2	6
Side cover					1.50	in
1st StIRRUP					3.00	in

There is NOT more than 12 in of concrete below top bars.

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Reinforced Concrete Beams and One-way Slab Systems
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[2] DESIGN RESULTS

Moment Redistribution Factors

Units: Org.Mu (k-ft)							
Supp	Side	Org.Mu	Calculated			User Limit[%]	Applied Factor[%]
			Iter.#	EpsilonT	Factor[%]		
1	Right	83.53	7	0.01796	17.96	0.00	0.00
2	Left	91.92	6	0.01526	15.26	20.00	15.26
2	Right	41.57	2	0.04168	20.00	20.00	20.00
3	Left	32.97	2	0.05368	20.00	20.00	20.00
3	Right	57.21	2	0.02909	20.00	20.00	20.00
4	Left	49.30	2	0.03446	20.00	0.00	0.00



Top Reinforcement

Units: Width (ft), Mmax (k-ft), Xmax (ft), As (in^2), Sp (in)									
Span	Zone	Width	Mmax	Xmax	AsMin	AsMax	AsReq	SpProv	Bars
1	Left	1.00	83.10	0.667	0.560	3.035	1.426	7.104	2-#8
	Midspan	1.00	0.00	12.500	0.000	3.035	0.238	7.104	2-#8 *8
	Right	1.00	75.67	24.333	0.560	3.035	1.288	7.104	2-#8
2	Left	1.00	31.23	0.667	0.560	3.035	0.509	7.104	2-#8 *3
	Midspan	1.00	0.00	7.500	0.000	3.035	0.085	7.104	2-#8 *8
	Right	1.00	24.35	14.333	0.525	3.035	0.395	7.104	2-#8 *3
3	Left	1.00	43.45	0.667	0.560	3.035	0.717	7.104	2-#8
	Midspan	1.00	0.00	10.000	0.000	3.035	0.135	7.104	2-#8 *8
	Right	1.00	48.84	19.333	0.560	3.035	0.810	7.104	2-#8

NOTES:
*3 - Design governed by minimum reinforcement.
*8 - Reinforcement required for structural integrity.

Top Bar Details

Units: Length (ft)										
Span	Left				Continuous		Right			
	Bars	Length	Bars	Length	Bars	Length	Bars	Length	Bars	Length
1	---		---		2-#8	25.00	---		---	
2	---		---		2-#8	15.00	---		---	
3	---		---		2-#8	20.00	---		---	

Top Bar Development Lengths

Units: Length (in)											
Span	Left				Continuous		Right				
	Bars	Length	Bars	DevLen	Bars	DevLen	Bars	DevLen	Bars	DevLen	
1	---		---		---		---		---		
2	---		---		---		---		---		
3	---		---		---		---		---		

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1	---	---	2-#8	12.00	---	---
2	---	---	2-#8	12.00	---	---
3	---	---	2-#8	12.00	---	---

Bottom Reinforcement

Units:	Width (ft),	Mmax (k-ft),	Xmax (ft),	As (in ²),	Sp (in)		
Span	Width	Mmax	Xmax	AsMin	AsMax	AsReq	SpProv
1	1.00	69.82	12.625	0.560	3.035	1.182	7.104
2	1.00	25.96	7.624	0.560	3.035	0.421	7.104
3	1.00	47.12	9.876	0.560	3.035	0.780	7.104

NOTES:
*3 - Design governed by minimum reinforcement.

Bottom Bar Details

Units:	Start (ft),	Length (ft)			
Span	Long Bars		Short Bars		
	Bars	Start	Length	Bars	Start
1	2-#8	0.00	25.00	---	---
2	2-#8	0.00	15.00	---	---
3	2-#8	0.00	20.00	---	---

Bottom Bar Development Lengths

Units:	DevLen (in)		
Span	Long Bars		Short Bars
	Bars	DevLen	DevLen
1	2-#8	26.61	---
2	2-#8	12.00	---
3	2-#8	17.56	---

Flexural Capacity

Units:	x (ft),	As (in ²),	PhiMn,	Mu (k-ft)										
Span	Top				Bottom									
	x	AsTop	PhiMn-	Mu-	Comb	Pat	Status	AsBot	PhiMn+	Mu+	Comb	Pat	Status	
1	0.000	1.58	-91.28	-100.54	U2	Odd	---	1.58	91.28	0.00	U1	All	---	
	0.222	1.58	-91.28	-94.62	U2	Odd	---	1.58	91.28	0.00	U1	All	---	
	0.667	1.58	-91.28	-83.10	U2	Odd	OK	1.58	91.28	0.00	U1	All	OK	
	8.950	1.58	-91.28	0.00	U1	All	OK	1.58	91.28	55.09	U2	Odd	OK	
	12.500	1.58	-91.28	0.00	U1	All	OK	1.58	91.28	69.78	U2	Odd	OK	
	12.625	1.58	-91.28	0.00	U1	All	OK	1.58	91.28	69.82	U2	Odd	OK	
	16.050	1.58	-91.28	0.00	U1	All	OK	1.58	91.28	57.75	U2	Odd	OK	
	24.333	1.58	-91.28	-75.67	U2	S2	OK	1.58	91.28	0.00	U1	All	OK	
	25.000	1.58	-91.28	-92.68	U2	S2	---	1.58	91.28	0.00	U1	All	---	
	2	0.000	1.58	-91.28	-41.95	U2	S2	---	1.58	91.28	0.00	U1	All	---
0.667		1.58	-91.28	-31.23	U2	S2	OK	1.58	91.28	0.00	U1	All	OK	
5.450		1.58	-91.28	0.00	U1	All	OK	1.58	91.28	20.72	U2	Even	OK	
7.500		1.58	-91.28	0.00	U1	All	OK	1.58	91.28	25.92	U2	Even	OK	
7.624		1.58	-91.28	0.00	U1	All	OK	1.58	91.28	25.96	U2	Even	OK	
9.550		1.58	-91.28	0.00	U1	All	OK	1.58	91.28	22.21	U2	Even	OK	
14.333		1.58	-91.28	-24.35	U2	S3	OK	1.58	91.28	0.00	U1	All	OK	
15.000		1.58	-91.28	-34.46	U2	S3	---	1.58	91.28	0.00	U1	All	---	
3		0.000	1.58	-91.28	-56.96	U2	S3	---	1.58	91.28	0.00	U1	All	---
		0.667	1.58	-91.28	-43.45	U2	S3	OK	1.58	91.28	0.00	U1	All	OK
	7.200	1.58	-91.28	0.00	U1	All	OK	1.58	91.28	39.84	U2	Odd	OK	
	9.876	1.58	-91.28	0.00	U1	All	OK	1.58	91.28	47.12	U2	Odd	OK	
	10.000	1.58	-91.28	0.00	U1	All	OK	1.58	91.28	47.08	U2	Odd	OK	
	12.800	1.58	-91.28	0.00	U1	All	OK	1.58	91.28	37.70	U2	Odd	OK	
	19.333	1.58	-91.28	-48.84	U2	Odd	OK	1.58	91.28	0.00	U1	All	OK	
	20.000	1.58	-91.28	-62.76	U2	Odd	---	1.58	91.28	0.00	U1	All	---	

Longitudinal Beam Transverse Reinforcement Demand and Capacity

Section Properties

Units:	d (in),	Av/s (in ² /in),	PhiVc (kip)
Span	d	(Av/s)min	PhiVc
1	14.00	0.0100	15.94
2	14.00	0.0100	15.94
3	14.00	0.0100	15.94

Beam Transverse Reinforcement Demand

Units: Start, End, Xu (in), Vu (ft), Av/s (kip/in^2)

Span	Start	End	Required			Demand	
			Xu	Vu Comb/Patt	Av/s	Av/s	
1	0.917	4.881	1.833	22.99	U2/Odd	0.0112	0.0112
	4.881	7.929	4.881	16.53	U2/Odd	0.0009	0.0100 *8
	7.929	10.976	7.929	10.07	U2/Odd	0.0000	0.0100 *8
	10.976	14.024	10.976	3.61	U2/Odd	0.0000	0.0000
	14.024	17.071	17.071	9.41	U2/S2	0.0000	0.0100 *8
	17.071	20.119	20.119	15.87	U2/S2	0.0000	0.0100 *8
2	0.917	3.452	1.833	12.91	U2/S2	0.0000	0.0100 *8
	3.452	5.071	3.452	9.47	U2/S2	0.0000	0.0100 *8
	5.071	6.690	5.071	6.04	U2/S2	0.0000	0.0000
	6.690	8.310	6.690	2.61	U2/S2	0.0000	0.0000
	8.310	9.929	9.929	5.12	U2/S3	0.0000	0.0000
	9.929	11.548	11.548	8.55	U2/S3	0.0000	0.0100 *8
3	0.917	4.167	1.833	17.08	U2/S3	0.0018	0.0100 *8
	4.167	6.500	4.167	12.13	U2/S3	0.0000	0.0100 *8
	6.500	8.833	6.500	7.18	U2/S3	0.0000	0.0000
	8.833	11.167	11.167	2.86	U2/Odd	0.0000	0.0000
	11.167	13.500	13.500	7.80	U2/Odd	0.0000	0.0000
	13.500	15.833	15.833	12.75	U2/Odd	0.0000	0.0100 *8
15.833	19.083	18.167	17.70	U2/Odd	0.0028	0.0100 *8	

NOTES:
*8 - Minimum transverse (stirrup) reinforcement governs.

Beam Transverse Reinforcement Details

Units: spacing & distance (in).
Span Size Stirrups (2 legs each unless otherwise noted)

- 1 #3 18 @ 6.9 + <-- 36.6 --> + 18 @ 6.9
- 2 #3 8 @ 6.6 + <-- 58.3 --> + 8 @ 6.6
- 3 #3 11 @ 6.4 + <-- 84.0 --> + 11 @ 6.4

Beam Transverse Reinforcement Capacity

Units: Start, End, Xu (ft), Vu, PhiVn (kip), Av/s (in^2/in), Av (in^2), Sp (in)

Span	Start	End	Xu	Required			Provided			
				Vu	Comb/Patt	Av/s	Av	Sp	Av/s	PhiVn
1	0.000	0.917	1.833	22.99	U2/Odd	-----	-----	-----	-----	-----
	0.917	10.976	1.833	22.99	U2/Odd	0.0112	0.22	6.9	0.0319	36.03
	10.976	14.024	10.976	3.61	U2/Odd	0.0000	-----	-----	-----	7.97
	14.024	24.083	23.167	22.34	U2/S2	0.0102	0.22	6.9	0.0319	36.03
	24.083	25.000	23.167	22.34	U2/S2	-----	-----	-----	-----	-----
2	0.000	0.917	1.833	12.91	U2/S2	-----	-----	-----	-----	-----
	0.917	5.071	1.833	12.91	U2/S2	0.0000	0.22	6.6	0.0331	36.79 *8
	5.071	9.929	5.071	6.04	U2/S2	0.0000	-----	-----	-----	7.97
	9.929	14.083	13.167	11.98	U2/S3	0.0000	0.22	6.6	0.0331	36.79 *8
	14.083	15.000	13.167	11.98	U2/S3	-----	-----	-----	-----	-----
3	0.000	0.917	1.833	17.08	U2/S3	-----	-----	-----	-----	-----
	0.917	6.500	1.833	17.08	U2/S3	0.0018	0.22	6.4	0.0345	37.66 *8
	6.500	13.500	13.500	7.80	U2/Odd	0.0000	-----	-----	-----	7.97
	13.500	19.083	18.167	17.70	U2/Odd	0.0028	0.22	6.4	0.0345	37.66 *8
	19.083	20.000	18.167	17.70	U2/Odd	-----	-----	-----	-----	-----

NOTES:
*8 - Minimum transverse (stirrup) reinforcement governs.

Slab Shear Capacity

Units: b, d (in), Xu (ft), PhiVc, Vu(kip)

Span	b	d	Vratio	PhiVc	Vu	Xu
1	---	---	---	---	---	---
2	---	---	---	---	---	---
3	---	---	---	---	---	---

Material Takeoff

Reinforcement in the Direction of Analysis

Top Bars:	320.4 lb	<=>	5.34 lb/ft	<=>	5.340 lb/ft^2
Bottom Bars:	320.4 lb	<=>	5.34 lb/ft	<=>	5.340 lb/ft^2
Stirrups:	102.0 lb	<=>	1.70 lb/ft	<=>	1.700 lb/ft^2
Total Steel:	742.8 lb	<=>	12.38 lb/ft	<=>	12.380 lb/ft^2

4. Design Results Comparison and Conclusions

The following table shows the comparison between hand results and [spBeam](#) model results.

Table 5 – Comparison of the Continuous Beam Analysis and Design Results							
Location		M _u , kip-ft Before Redistribution		M _u , kip-ft After Redistribution		A _{s,req} , in. ²	
		Hand	spBeam	Hand	spBeam	Hand	spBeam
Support A	Right Face	83.5	83.5	83.1	83.1	1.43	1.43
Midspan A-B		61.6	61.6	69.8	69.8	1.18	1.18
Support B	Left Face	91.9	91.9	75.7	75.7	1.29	1.29
	Right Face	41.6	41.6	31.2	31.2	0.51*	0.51*
Midspan B-C		17.5	17.6	26	26	0.42*	0.42*
Support C	Left Face	33	33	24.3	24.4	0.39*	0.40*
	Right Face	57.2	57.2	43.4	43.5	0.72	0.72
Midspan C-D		40.2	40.2	47.1	47.1	0.78	0.78
Support D	Left Face	49.3	49.3	48.8	48.8	0.81	0.81
* A _{s,min} governs							

The results of all the hand calculations used illustrated above are in precise agreement with the automated exact results obtained from the [spBeam](#) program.

The moment redistribution is often utilized for the investigation of existing structures for conditions such as change of use, additional loading, or verifying adequacy for the latest design code. In these conditions, any reserve capacity from existing reinforcement layout at mid-span (or support) of a span may be utilized to compensate for the inadequacy of the support (or mid-span) of the same span.

The moment redistribution can also be utilized in the design of a new structure. One such example of its application may help reduce the negative moment at an interior support and corresponding top reinforcement while increasing the positive moment at mid-span. The advantage of this may be the alleviation of the congestion of rebar at support top regions.

The calculation of moment redistribution is a tedious process especially while considering live load patterning as presented in this example. The procedure gets far more complicated if point loads or partial line loads are present. The [spBeam](#) software program performs the moment redistribution calculations with speed and accuracy.