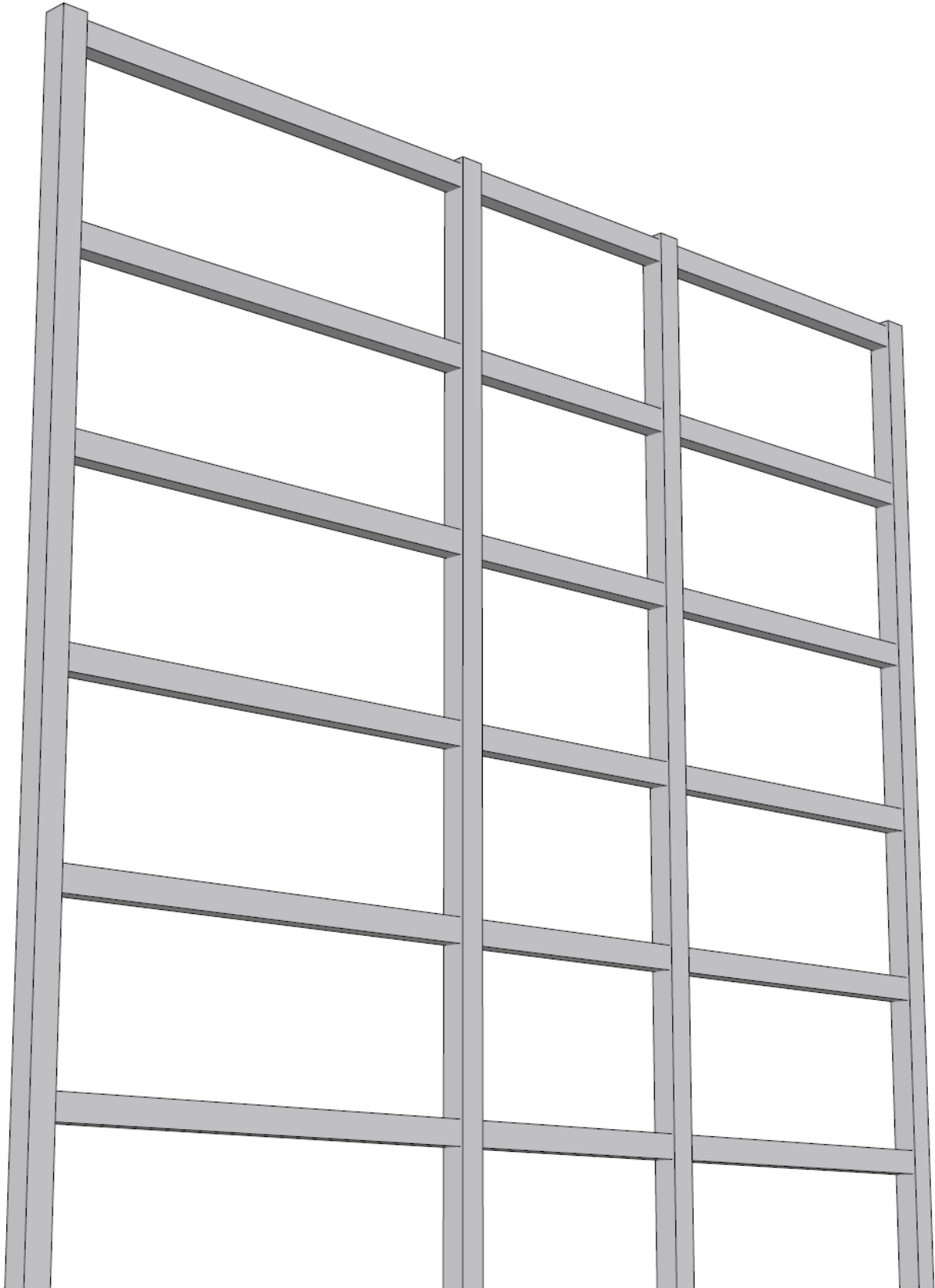


Continuous Beam Design with Moment Redistribution (CSA A23.3-14)



Continuous Beam Design with Moment Redistribution (CSA A23.3-14)

A structural reinforced concrete continuous beam at an intermediate floor level in an exterior frame (spandrel Beam) provides gravity load resistance for the applied dead and live loads.

The required reinforcement areas are determined for this continuous beam after analysis are adjusted and optimized using moment redistribution provisions from CSA A23.3 standard. The results of hand calculations are then compared with numerical analysis results obtained from the [spBeam](#) engineering software program by [StructurePoint](#).

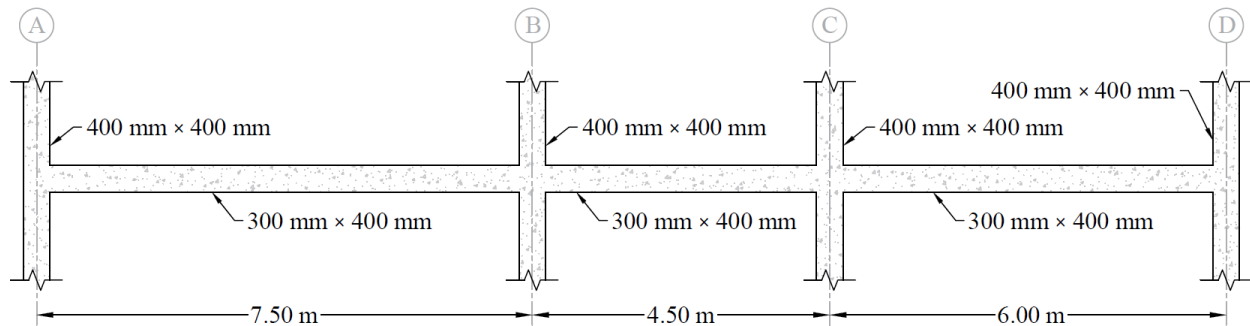


Figure 1 – Reinforced Concrete Continuous Beam at Intermediate Floor Level

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Code

Design of Concrete Structures (CSA A23.3-14) and Explanatory Notes on CSA Group standard A23.3-14 “Design of Concrete Structures”

References

- PCA Notes on ACI 318-11 Building Code Requirements for Structural Concrete, Twelfth Edition, 2013 Portland Cement Association, Example 8.2
- [spBeam Engineering Software Program Manual v10.00](#), [STRUCTUREPOINT](#), 2024
- “[One-Way Wide Module \(Skip\) Joist Concrete Floor System Design \(ACI 318-14\)](#)” Design Example, [STRUCTUREPOINT](#), 2025
- Contact Support@StructurePoint.org to obtain supplementary materials ([spBeam](#) model: DE-Moment-Redistribution-CSA-14.slbx)

Design Data

$f_c' = 25$ MPa normal weight concrete ($\gamma_c = 24.00$ kN/m³)

$f_y = 400$ MPa

Story height = 3.00 m

Columns = 400.00 mm × 400.00 mm

Spandrel beam = 300.00 mm × 400.00 mm

Dead Loads, $DL = 17.00$ kN/m

Live Loads, $LL = 7.00$ kN/m

Solution

Continuous beams are frequently analyzed and designed using simplified methods such as the approximate frame analysis coefficients provided in CSA A23.3 to approximate the bending moments and shear forces. There are many important limitations to allow the use of coefficients. The factored moment and shear can be determined using the simplified method if the requirements are satisfied: **CSA A23.3-14 (9.3.1)**

- ✓ There are at least two spans.
- ✓ Loads are uniformly distributed.
- ✓ Members are prismatic.
- ✓ Factored live load \leq Twice the factored dead load
- X The longer of two adjacent spans does not exceed the shorter by more than 20 percent.

In this example the ratio of the two adjacent spans lengths exceeds 1.2 and coefficients can't be used. Therefore, the analysis of the continuous beam framing into columns must use traditional analysis methods and will be performed using the following steps:

1. Determine the factored loads.
2. Perform the structural analysis using the moment distribution method.
3. Repeat the analysis for each live load pattern to arrive at the enveloped maximum design moments.
4. Apply moment redistribution provisions to get adjusted (reduced) design moments.
5. Determine the required area of steel optimized to the adjusted design moments.

It is important in this example to distinguish between the two terms: **moment distribution** and **moment redistribution**. **Moment distribution** is a structural analysis method for statically indeterminate beams and frames, while **moment redistribution** refers to the behavior of statically indeterminate structures that are not completely elastic, but have some reserve plastic capacity. When one location first yields, further application of load to the structure causes the bending moment to redistribute differently from what a purely elastic analysis would suggest.

Moment redistribution is not commonly used primarily due to the extensive additional and tedious calculations required involving many live load patterns and the iterative nature of the procedure that lends itself to automation as is provided by [spBeam](#) engineering software program from [StructurePoint](#).

When permitted, **moment redistribution** is used to reduce total reinforcement required and this example will illustrate the extent of redistribution of bending moments and the corresponding reduction of steel area achievable. Typically, negative moments over supports governs the design of reinforcement and any reduction in the required area of steel at the supports is favorable due to savings in materials, labor, and construction time and effort.

1. Continuous Beam Analysis – Moment Distribution Method

Determine moment distribution factors and fixed-end moments for the frame members. The moment distribution procedure will be used to analyze the frame. Stiffness factors, carry over factors, and fixed-end moment factors for the beams and columns are determined as follows:

Determine the elastic bending moment diagrams for each of the load patterns per CSA and the maximum moment envelope values for all patterns as shown in [Table 1](#). **CSA A23.3-14 (9.2.3)**

1.1. Load Combination

$$U = 1.25 \times D + 1.50 \times L \quad \text{CSA A23.3-14 (Annex C, Table C.1a)}$$

$$w_d = 1.25 \times 17.00 = 21.25 \text{ kN/m}$$

$$w_l = 1.50 \times 7.00 = 10.50 \text{ kN/m}$$

$$w_f = 21.25 + 10.75 = 31.75 \text{ kN/m}$$

1.2. Flexural Stiffness of Beams and Columns Ends, K

$$K = \frac{4 \times E_c \times I}{l}$$

Where K is referred to as stiffness factor at beam or column end and can be defined as the amount of moment required to rotate the end of the beam or column 1 rad.

$$I = \frac{b \times h^3}{12}$$

$$E_c = (3,300 \times \sqrt{f'_c} + 6,900) \times \left(\frac{\gamma_c}{2,300} \right)^{1.5} = (3,300 \times \sqrt{25} + 6,900) \times \left(\frac{2,447.30}{2,300} \right)^{1.5} \quad \text{CSA A23.3-14 (8.6.2.2)}$$

$$E_c = 25,683.54 \text{ MPa}$$

For Member AB:

$$l = 7.50 \text{ m}$$

$$I = \frac{300.00 \times 400.00^3}{12} = 1.60 \times 10^9 \text{ mm}^2$$

$$E_c = (3,300 \times \sqrt{25} + 6,900) \times \left(\frac{2,447.30}{2,300} \right)^{1.5} = 25,683.54 \text{ MPa}$$

$$K_{AB} = \frac{4 \times 25,683.54 \times 1.60 \times 10^9}{7,500.00} = 2.19 \times 10^{10} \text{ N-mm}$$

For Column Ends:

$$h = 3.00 \text{ m}$$

$$I = \frac{400.00 \times 400.00^3}{12} = 2.13 \times 10^9 \text{ mm}^4$$

$$K_{Col} = \frac{4 \times 25,683.54 \times 2.13 \times 10^9}{7,500.00} = 7.31 \times 10^{10} \text{ N-mm}$$

1.3. Distribution Factor, *DF*

$$DF = \frac{K}{\sum K}$$

The distribution factor for a member that is connected to a fixed joint is defined as the fraction of the total resisting moment supplied by this member.

For Member AB:

$$DF_{AB} = \frac{2.19 \times 10^{10}}{7.31 \times 10^{10} + 2.19 \times 10^{10} + 7.31 \times 10^{10}} = 0.130$$

1.4. Carry Over Factor, *COF*

$$COF = 0.5$$

Where *COF* is the Carry-Over Factor that represents the fraction of the moment that is “carried over” from the joint to the beam end when the beam far end is fixed.

1.5. Fixed-End Moments, *FEMs*

For a beam with uniformly distributed load and fixed ends, *FEM* can be found using the following equation:

$$FEM = \frac{w \times l^2}{12}$$

For Member AB for Load Pattern I:

$$FEM_{AB} = \frac{31.75 \times 7.50^2}{12} = 148.83 \text{ kN-m}$$

1.6. Beam Analysis Using Moment Distribution Method

Repeat the previous steps to all frame members to obtain the parameters necessary for the analysis. Moment distribution for the five loading conditions is shown in [Table 1](#). Counter-clockwise rotational moments acting on member ends are taken as positive. Maximum positive span moments are determined from the following equation:

$$M_{max}^+ = \frac{w_u \times l_1^2}{8} - \frac{M_L^- + M_R^-}{2} + \frac{(M_L^- - M_R^-)^2}{2 \times w_u \times l_1^2} \text{ at distance } x_{max} = \frac{l_1}{2} + \frac{M_L^- - M_R^-}{w_u \times l_1}$$

Where:

- M_{max}^+ = Maximum positive moment in the span
- M_L^- = Negative moment in the left support
- M_R^- = Negative moment in the right support
- l_1 = The span length

For Load Pattern I:

Maximum positive moment in spans A-B:

$$M_{max}^+ = \frac{(31.75) \times 7.50^2}{8} - \frac{134.42 + 147.39}{2} + \frac{(134.42 - 147.39)^2}{2 \times (31.75) \times 7.50^2} = 82.38 \text{ kN-m}$$

$$x_{max} = \frac{7.50}{2} + \frac{(134.42 - 147.39)}{(31.75) \times 7.50} = 3.70 \text{ m}$$

Where:

$$M_L^- = 134.42 \text{ kN-m}$$

$$M_R^- = 147.39 \text{ kN-m}$$

Maximum positive moment in span B-C:

$$M_{max}^+ = \frac{(31.75) \times 4.50^2}{8} - \frac{70.61 + 48.32}{2} + \frac{(70.61 - 48.32)^2}{2 \times (31.75) \times 4.50^2} = 21.29 \text{ kN-m}$$

$$x_{max} = \frac{4.50}{2} + \frac{(70.61 - 48.32)}{(31.75) \times 4.50} = 2.41 \text{ m}$$

Where:

$$M_L^- = 70.61 \text{ kN-m}$$

$$M_R^- = 48.32 \text{ kN-m}$$

Maximum positive moment in span C-D:

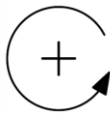
$$M_{max}^+ = \frac{(21.25) \times 6.00^2}{8} - \frac{65.66 + 55.05}{2} + \frac{(65.66 - 55.05)^2}{2 \times (21.25) \times 6.00^2} = 35.34 \text{ kN-m}$$

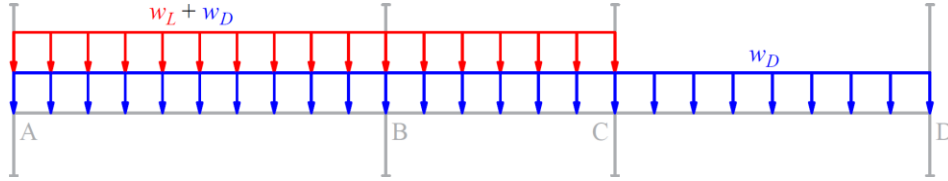
$$x_{max} = \frac{6.00}{2} + \frac{(65.66 - 55.05)}{(21.25) \times 6.00} = 3.08 \text{ m}$$

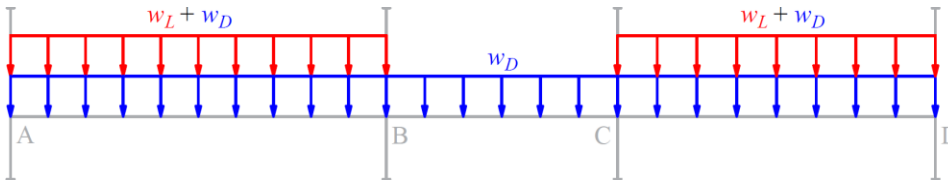
Where:

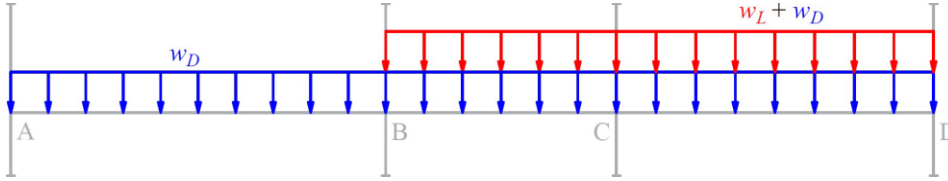
$$M_L^- = 65.66 \text{ kN-m}$$

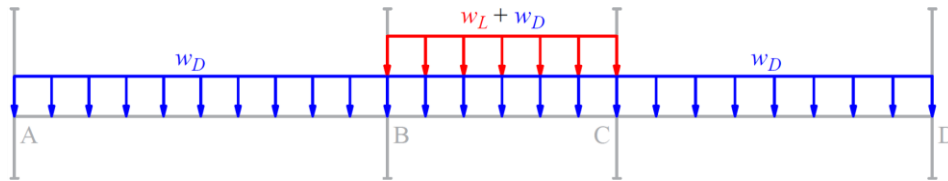
$$M_R^- = 55.05 \text{ kN-m}$$

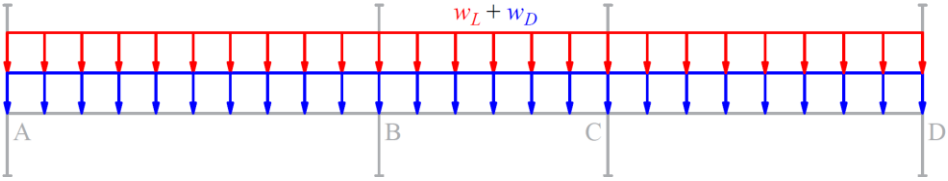
| Table 1 – Moment Distribution [‡] | | | | | | |
|---|-------|-------|-------|-------|-------|-------|
|  | | | | | | |
| Joint | A | B | | C | | D |
| Member | AB | BA | BC | CB | CD | DC |
| DF | 0.130 | 0.107 | 0.179 | 0.174 | 0.130 | 0.158 |
| COF | 0.500 | 0.500 | 0.500 | 0.500 | 0.500 | 0.500 |

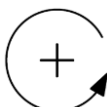
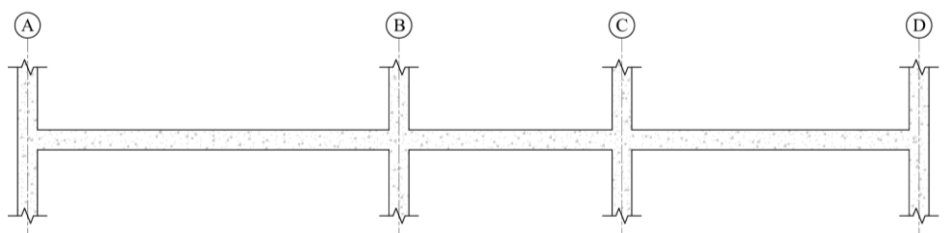
| Load Pattern I (S2*) | | | | | | |
|-----------------------|--|---------|-------|--------|-------|--------|
| LP I |  | | | | | |
| Joint | A | B | | C | | D |
| Member | AB | BA | BC | CB | CD | DC |
| FEM | 148.83 | -148.83 | 53.58 | -53.58 | 63.75 | -63.75 |
| Dist. | -19.41 | 10.21 | 17.01 | -1.77 | -1.33 | 10.07 |
| CO | 5.10 | -9.71 | -0.88 | 8.50 | 5.03 | -0.66 |
| Dist. | -0.67 | 1.13 | 1.89 | -2.35 | -1.77 | 0.10 |
| CO | 0.57 | -0.33 | -1.18 | 0.95 | 0.05 | -0.88 |
| Dist. | -0.07 | 0.16 | 0.27 | -0.17 | -0.13 | 0.14 |
| CO | 0.08 | -0.04 | -0.09 | 0.13 | 0.07 | -0.07 |
| Dist. | -0.01 | 0.01 | 0.02 | -0.04 | -0.03 | 0.01 |
| CO | 0.01 | -0.01 | -0.02 | 0.01 | 0.01 | -0.01 |
| Dist. | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| M ⁻ (kN-m) | 134.42 | -147.39 | 70.61 | -48.32 | 65.66 | -55.05 |
| M ⁺ (kN-m) | 82.38 | | 21.29 | | 35.34 | |

| Load Pattern II (Odd*) | | | | | | |
|------------------------|--|---------|-------|--------|-------|--------|
| LP II |  | | | | | |
| Joint | A | B | | C | | D |
| Member | AB | BA | BC | CB | CD | DC |
| FEM | 148.83 | -148.83 | 35.86 | -35.86 | 95.25 | -95.25 |
| Dist. | -19.41 | 12.10 | 20.17 | -10.33 | -7.75 | 15.04 |
| CO | 6.05 | -9.71 | -5.16 | 10.09 | 7.52 | -3.87 |
| Dist. | -0.79 | 1.59 | 2.66 | -3.06 | -2.30 | 0.61 |
| CO | 0.80 | -0.39 | -1.53 | 1.33 | 0.31 | -1.15 |
| Dist. | -0.10 | 0.21 | 0.34 | -0.28 | -0.21 | 0.18 |
| CO | 0.10 | -0.05 | -0.14 | 0.17 | 0.09 | -0.11 |
| Dist. | -0.01 | 0.02 | 0.03 | -0.05 | -0.03 | 0.02 |
| CO | 0.01 | -0.01 | -0.02 | 0.02 | 0.01 | -0.02 |
| Dist. | 0.00 | 0.00 | 0.01 | 0.00 | 0.00 | 0.00 |
| M ⁻ (kN-m) | 135.47 | -145.06 | 52.21 | -37.98 | 92.88 | -84.54 |
| M ⁺ (kN-m) | 83.00 | | 8.93 | | 54.19 | |

| Load Pattern III (S3*) | | | | | | |
|------------------------|--|---------|-------|--------|-------|--------|
| LP III |  | | | | | |
| Joint | A | B | | C | | D |
| Member | AB | BA | BC | CB | CD | DC |
| FEM | 99.61 | -99.61 | 53.58 | -53.58 | 95.25 | -95.25 |
| Dist. | -12.99 | 4.93 | 8.22 | -7.25 | -5.44 | 15.04 |
| CO | 2.47 | -6.50 | -3.62 | 4.11 | 7.52 | -2.72 |
| Dist. | -0.32 | 1.08 | 1.81 | -2.02 | -1.52 | 0.43 |
| CO | 0.54 | -0.16 | -1.01 | 0.90 | 0.21 | -0.76 |
| Dist. | -0.07 | 0.13 | 0.21 | -0.19 | -0.15 | 0.12 |
| CO | 0.06 | -0.04 | -0.10 | 0.10 | 0.06 | -0.07 |
| Dist. | -0.01 | 0.01 | 0.02 | -0.03 | -0.02 | 0.01 |
| CO | 0.01 | 0.00 | -0.01 | 0.01 | 0.01 | -0.01 |
| Dist. | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| M ⁻ (kN-m) | 89.29 | -100.15 | 59.09 | -57.94 | 95.93 | -83.21 |
| M ⁺ (kN-m) | 54.74 | | 21.85 | | 53.38 | |

| Load Pattern IV (Even*) | | | | | | |
|-------------------------|--|---------|-------|--------|-------|--------|
| LP IV |  | | | | | |
| Joint | A | B | | C | | D |
| Member | AB | BA | BC | CB | CD | DC |
| FEM | 99.61 | -99.61 | 53.58 | -53.58 | 63.75 | -63.75 |
| Dist. | -12.99 | 4.93 | 8.22 | -1.77 | -1.33 | 10.07 |
| CO | 2.47 | -6.50 | -0.88 | 4.11 | 5.03 | -0.66 |
| Dist. | -0.32 | 0.79 | 1.32 | -1.59 | -1.19 | 0.10 |
| CO | 0.40 | -0.16 | -0.80 | 0.66 | 0.05 | -0.60 |
| Dist. | -0.05 | 0.10 | 0.17 | -0.12 | -0.09 | 0.09 |
| CO | 0.05 | -0.03 | -0.06 | 0.09 | 0.05 | -0.05 |
| Dist. | -0.01 | 0.01 | 0.02 | -0.02 | -0.02 | 0.01 |
| CO | 0.00 | 0.00 | -0.01 | 0.01 | 0.00 | -0.01 |
| Dist. | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| M ⁻ (kN-m) | 89.15 | -100.46 | 61.55 | -52.22 | 66.26 | -54.79 |
| M ⁺ (kN-m) | 54.66 | | 23.55 | | 35.19 | |

| Load Pattern V (All*) | | | | | | |
|-----------------------|--|---------|-------|--------|-------|--------|
| LP V |  | | | | | |
| Joint | A | B | | C | | D |
| Member | AB | BA | BC | CB | CD | DC |
| FEM | 148.83 | -148.83 | 53.58 | -53.58 | 95.25 | -95.25 |
| Dist. | -19.41 | 10.21 | 17.01 | -7.25 | -5.44 | 15.04 |
| CO | 5.10 | -9.71 | -3.62 | 8.50 | 7.52 | -2.72 |
| Dist. | -0.67 | 1.43 | 2.38 | -2.79 | -2.09 | 0.43 |
| CO | 0.71 | -0.33 | -1.39 | 1.19 | 0.21 | -1.05 |
| Dist. | -0.09 | 0.18 | 0.31 | -0.24 | -0.18 | 0.17 |
| CO | 0.09 | -0.05 | -0.12 | 0.15 | 0.08 | -0.09 |
| Dist. | -0.01 | 0.02 | 0.03 | -0.04 | -0.03 | 0.01 |
| CO | 0.01 | -0.01 | -0.02 | 0.02 | 0.01 | -0.02 |
| Dist. | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| M ⁻ (kN-m) | 134.56 | -147.08 | 68.15 | -54.04 | 95.33 | -83.47 |
| M ⁺ (kN-m) | 82.46 | | 19.43 | | 53.54 | |

| Envelop of Maximum Moments | | | | | | |
|---|--|---------|-------|--------|-------|--------|
|  |  | | | | | |
| Span | AB | | BC | | CD | |
| | M_L | M_R | M_L | M_R | M_L | M_R |
| Max M_f^- (Column Center Line) | 135.47 | -147.39 | 70.61 | -57.94 | 95.93 | -84.54 |
| Max M_f^- (Column Face) | 112.55 | -123.87 | 55.96 | -44.34 | 77.09 | -66.41 |
| Max M_f^+ | 83.00 | | 23.55 | | 54.19 | |

‡ Moments units are kN-m

* Live load pattern designation in [spBeam](#)

2. Moment Redistribution

Now that the structural analysis is completed for all applicable live load patterns, and the enveloped moments are determined we can evaluate the impact of moment redistribution.

Redistribution of elastic bending moments can occur prior to failure due to inelastic rotations in regions with high moments. Beam sections having low percentages of tension reinforcement or containing compression reinforcement have low c/d values and so can tolerate larger redistributions. Due to redistribution, the computed bending moments at a support may be reduced provided that the bending moments in each adjacent span are increased to satisfy equilibrium for the loading case under consideration. Since the loading that causes maximum moments in the adjacent spans, accounting for moment redistribution can result in a reduction of the required flexural reinforcement at both the support and span regions. CSA A23.3-14 (N9.2.4)

Except when approximate values for bending moments are used, the negative moments at the supports of continuous flexural members calculated by elastic analysis for any assumed loading arrangement may each be increased or decreased by not more than $(30 - 50c/d)\%$, but not more than 20%, and the modified negative moments shall be used for calculating the moments at sections within the spans. CSA A23.3-14 (9.2.4)

Note that static equilibrium shall be maintained after redistribution of moments for each loading arrangement. The reduced moment shall be used for calculating redistributed moments at all other sections within the spans.

2.1. Reduction Percentage Calculations

Using $d = 355.00$ mm and cover = 30.00 mm

For negative moment at support D:

First Iteration

Calculate the required reinforcement to resist the negative moment at support D:

$$(M_f)_1 = 66.41 \text{ kN-m}$$

In this example, jd is assumed equal to $0.928 \times d$. The assumption will be verified once the area of steel is finalized.

$$jd = 0.928 \times d = 0.928 \times 355.00 = 329.56 \text{ mm}$$

$$b = 300.00 \text{ mm}$$

The required reinforcement at initial trial is calculated as follows:

$$A_s = \frac{(M_f)_1}{\phi_s \times f_y \times jd} = \frac{66.41 \times 10^6}{0.85 \times 400 \times 329.56} = 592.64 \text{ mm}^2$$

$$\alpha_1 = 0.85 - 0.0015 \times f'_c = 0.85 - 0.0015 \times 25 = 0.813 > 0.67 \quad \text{CSA A23.3-14 (10.1.7)}$$

$$\beta_1 = 0.97 - 0.0025 \times f'_c = 0.97 - 0.0025 \times 25 = 0.908 > 0.67 \quad \text{CSA A23.3-14 (10.1.7)}$$

Recalculate 'a' for the actual $A_s = 592.64 \text{ mm}^2$: $a = \frac{\phi_s \times A_s \times f_y}{\phi_c \times \alpha_1 \times f'_c \times b} = \frac{0.85 \times 592.64 \times 400}{0.65 \times 0.813 \times 25 \times 300.00} = 50.87 \text{ mm}$

$$c = \frac{a}{\beta_1} = \frac{50.87}{0.908} = 56.06 \text{ mm}$$

The tension reinforcement in flexural members shall not be assumed to reach yield unless:

$$\frac{c}{d} \leq \frac{700}{700 + f_y} \quad \text{CSA A23.3-14 (10.5.2)}$$

$$\frac{56.06}{355.00} = 0.158 \leq 0.636$$

$$jd = \frac{d - \frac{a}{2}}{d} = 0.928d$$

Therefore, the assumption that tension reinforcements will yield and jd equals to $0.928 \times d$ is valid.

$$Adjustment_1 = \left(30 - 50 \times \frac{c}{d} \right) = \left(30 - 50 \times \frac{56.06}{355} \right) = 22.10 > 20.00 \rightarrow Adjustment_1 = 20.00\%$$

Second Iteration

$$(M_f)_2 = 66.41 - 66.41 \times 0.20 = 53.12 \text{ kN-m}$$

jd is assumed equal to $0.944 \times d$.

$$jd = 0.944 \times d = 0.944 \times 355.00 = 334.98 \text{ mm}$$

The required reinforcement at initial trial is calculated as follows:

$$A_s = \frac{(M_f)_2}{\phi_s \times f_y \times jd} = \frac{53.12 \times 10^6}{0.85 \times 400 \times 334.98} = 466.44 \text{ mm}^2$$

Recalculate 'a' for the actual $A_s = 466.44 \text{ mm}^2$: $a = \frac{\phi_s \times A_s \times f_y}{\phi_c \times \alpha_1 \times f'_c \times b} = \frac{0.85 \times 466.44 \times 400}{0.65 \times 0.813 \times 25 \times 300.00} = 40.04 \text{ mm}$

$$c = \frac{a}{\beta_1} = \frac{40.04}{0.908} = 44.12 \text{ mm}$$

The tension reinforcement in flexural members shall not be assumed to reach yield unless:

$$\frac{c}{d} \leq \frac{700}{700 + f_y} \quad \text{CSA A23.3-14 (10.5.2)}$$

$$\frac{44.12}{355.00} = 0.124 \leq 0.636$$

$$jd = \frac{d - \frac{a}{2}}{d} = 0.944d$$

Therefore, the assumption that tension reinforcements will yield and jd equals to $0.944 \times d$ is valid.

$$Adjustment_2 = \left(30 - 50 \times \frac{c}{d} \right) = \left(30 - 50 \times \frac{44.12}{355} \right) = 23.79 > 20.00 \rightarrow Adjustment_2 = 20.00\%$$

Since $Adjustment_1 = Adjustment_2 \rightarrow$ End of Iterations

Table 2 – Moment Adjustments at Supports

| | | Support | | | | | |
|--------------------------------|--------------------|---------|--------|-------|-------|-------|-------|
| | | A | B | | C | | D |
| | | Right | Left | Right | Left | Right | Left |
| Iteration 1 | $M_f(\text{kN-m})$ | 112.55 | 123.87 | 55.96 | 44.34 | 77.09 | 66.41 |
| | c/d | 0.285 | 0.320 | 0.131 | 0.103 | 0.186 | 0.158 |
| | Adjustment (%) | 15.73 | 14.01 | 20.00 | 20.00 | 20.00 | 20.00 |
| Iteration 2 | $M_f(\text{kN-m})$ | 94.84 | 106.52 | 44.77 | 35.47 | 61.67 | 53.12 |
| | c/d | 0.234 | 0.268 | 0.104 | 0.081 | 0.146 | 0.124 |
| | Adjustment (%) | 18.29 | 16.62 | 20.00 | 20.00 | 20.00 | 20.00 |
| Iteration 3 | $M_f(\text{kN-m})$ | 91.97 | 103.28 | | | | |
| | c/d | 0.226 | 0.258 | | | | |
| | Adjustment (%) | 18.69 | 17.09 | | | | |
| Iteration 4 | $M_f(\text{kN-m})$ | 91.52 | 102.70 | | | | |
| | c/d | 0.225 | 0.257 | | | | |
| | Adjustment (%) | 18.75 | 17.17 | | | | |
| Iteration 5 | $M_f(\text{kN-m})$ | 91.44 | 102.60 | | | | |
| | c/d | 0.225 | 0.256 | | | | |
| | Adjustment (%) | 18.76 | 17.19 | | | | |
| Iteration 6 | $M_f(\text{kN-m})$ | | 102.58 | | | | |
| | c/d | | 0.256 | | | | |
| | Adjustment (%) | | 17.19 | | | | |
| Final Allowable Adjustment (%) | | 18.76 | 17.19 | 20.00 | 20.00 | 20.00 | 20.00 |

2.2. Adjustment of Moments (Redistribution)

Now the engineer can make decisions to reduce any negative moments (or positive) based on project parameters including:

- Steel detailing and placement considerations.
- New design or investigation of existing beams
- Optimize the provided reinforcement for more economical design
- Optimize the provided reinforcement for improved uniformity

It was decided to reduce the negative moments on both sides of supports B and C and accept the increase in the corresponding positive moments, and not to adjust the negative moments at the exterior supports A and D.

The following figures show the unadjusted and adjusted moment values at the columns centerlines, column faces, and at the midspan for each load pattern and for the maximum values at each critical location (maximum moment envelopes).

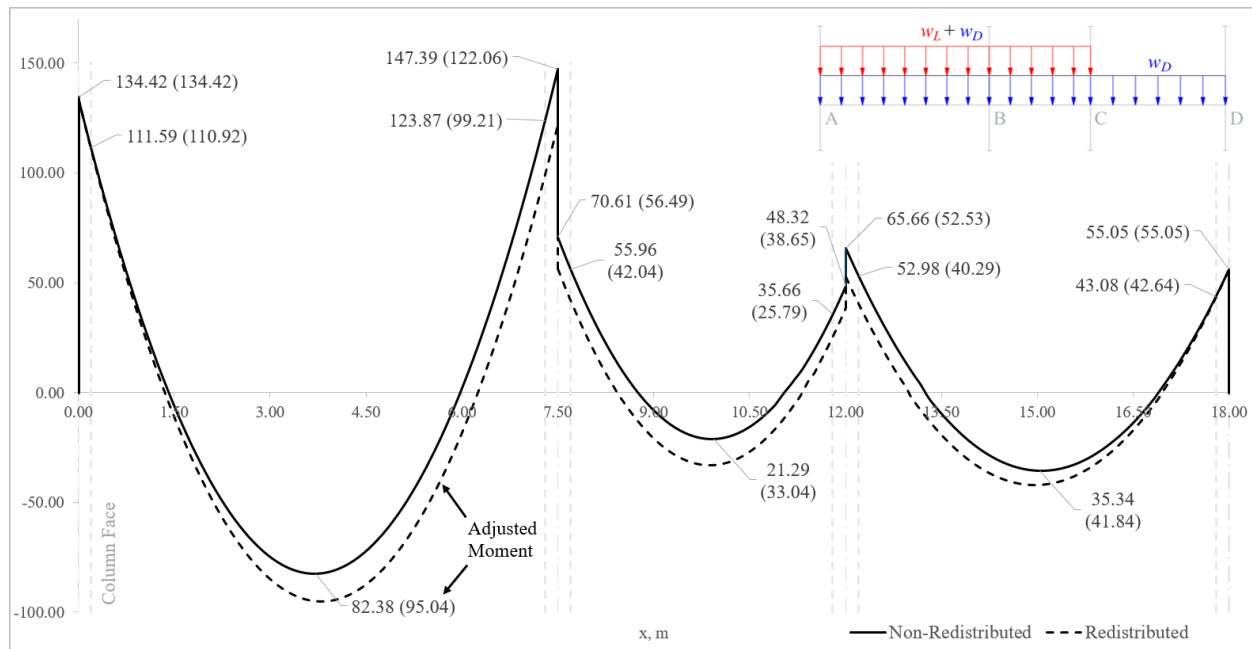


Figure 2 – Load Pattern I (moments in kN-m)

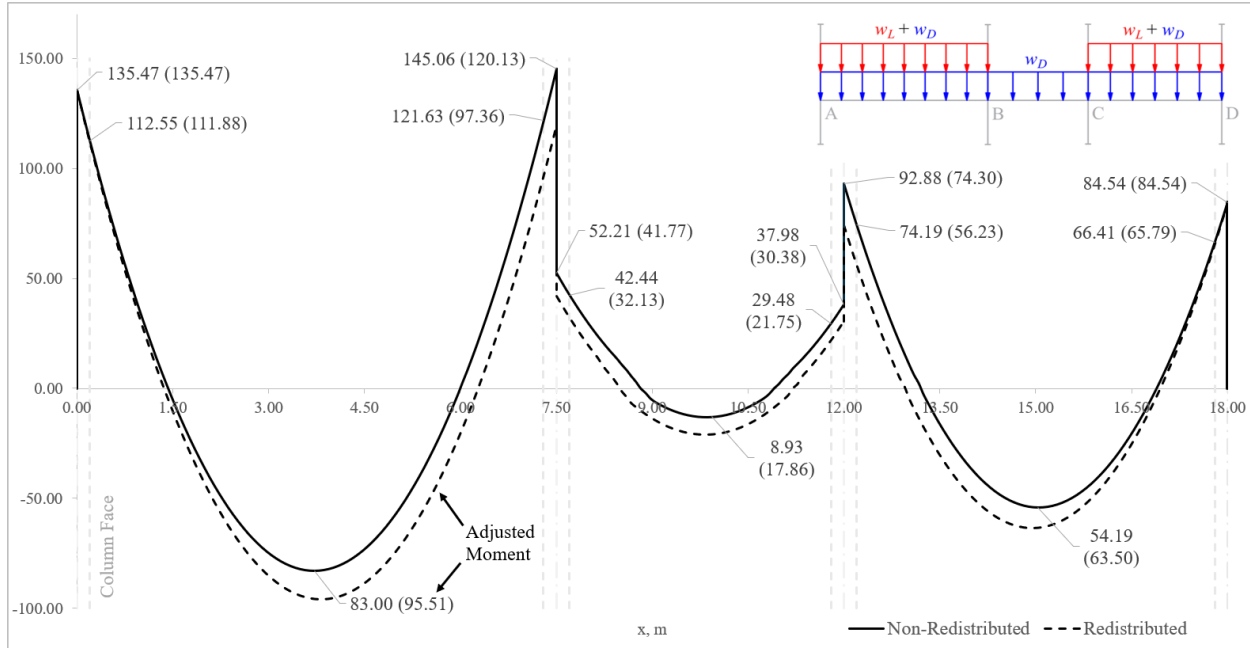


Figure 3 – Load Pattern II (moments in kN-m)

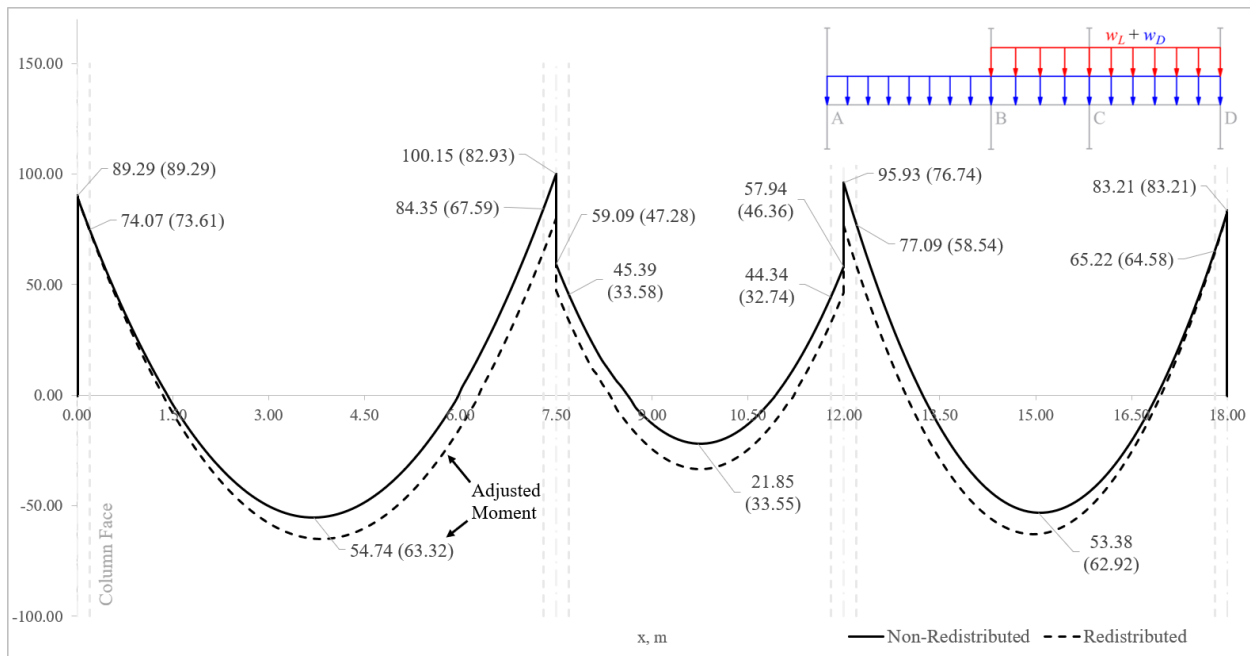


Figure 4 – Load Pattern III (moments in kN-m)

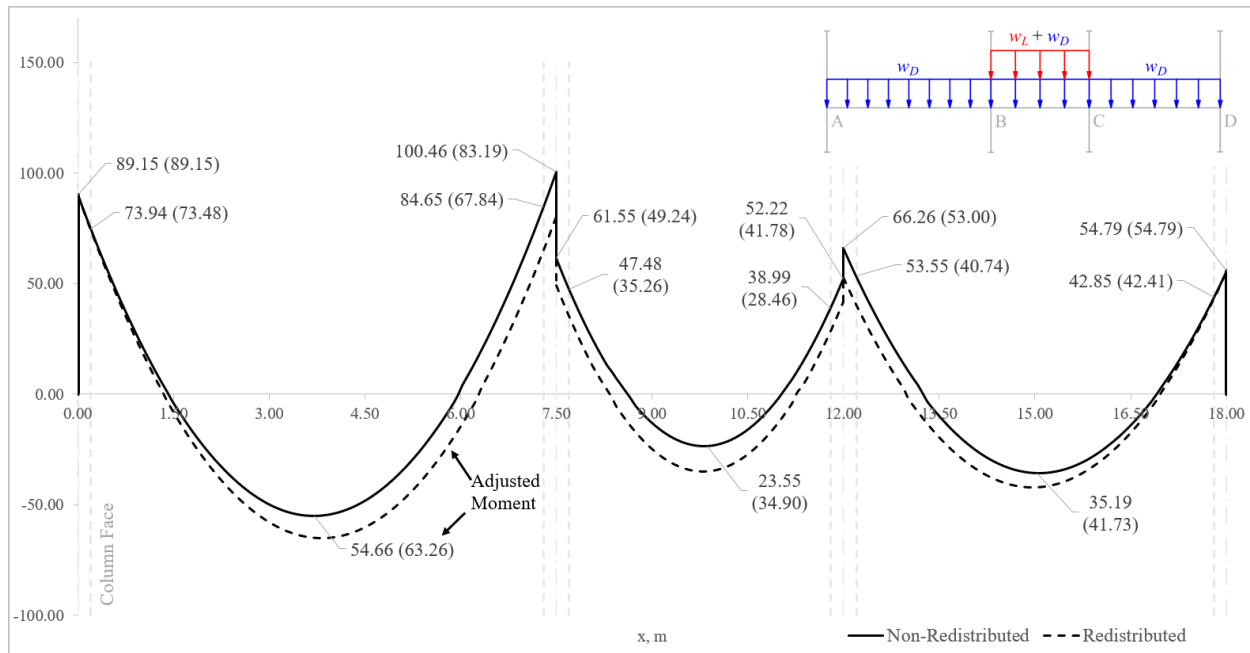


Figure 5 – Load Pattern IV (moments in kN-m)

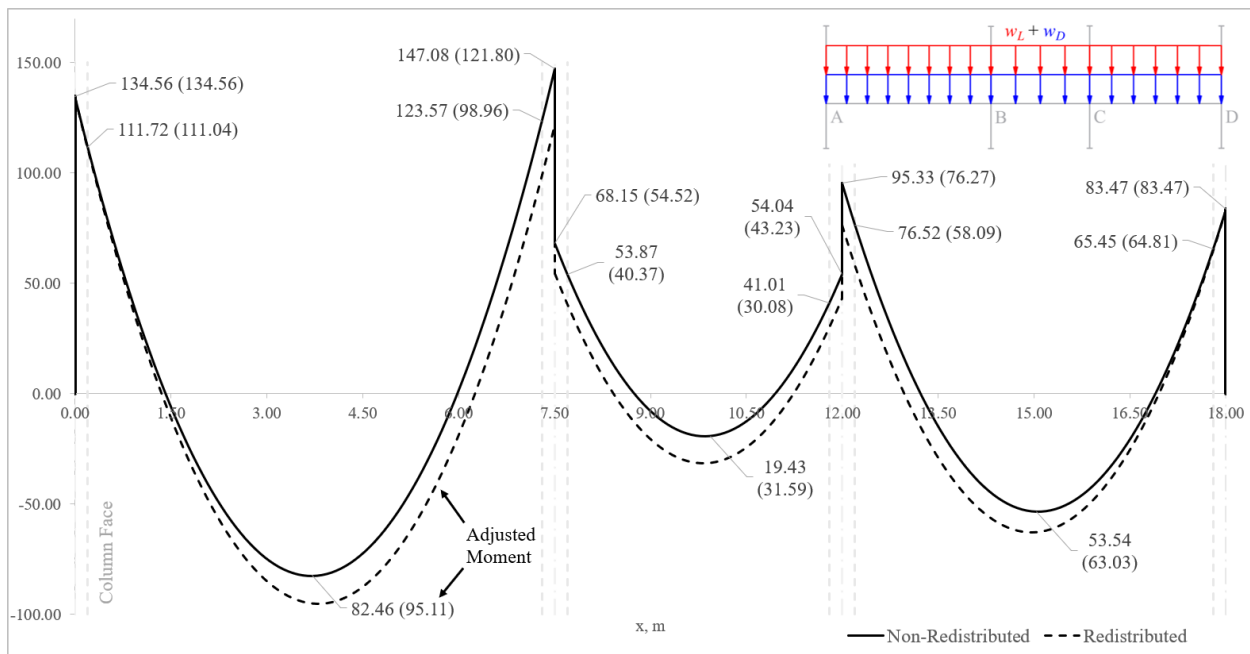


Figure 6 – Load Pattern V (moments in kN-m)

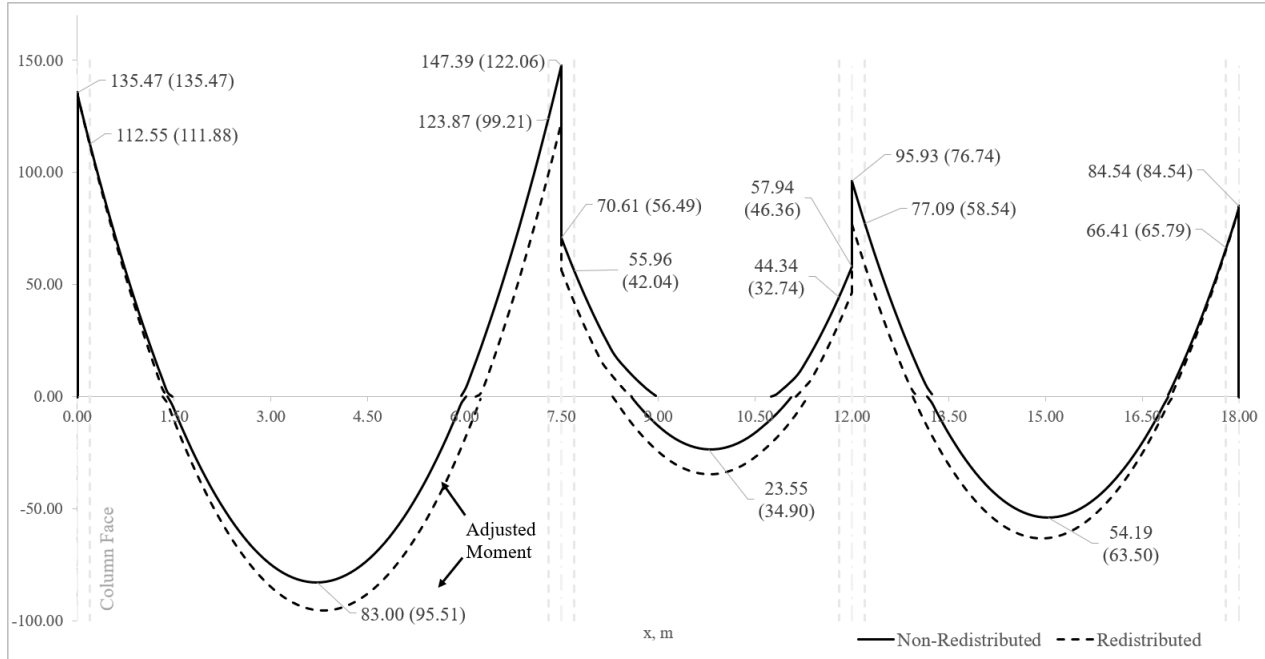


Figure 7 – Maximum Moment Envelopes for Pattern Loading (moments in kN-m)

For load pattern I

$$M_{B, \text{left}} = 147.39 \text{ kN-m (adjustment} = 17.19\%)$$

$$\text{Adjusted } M_{B, \text{left}} = 147.39 - 147.39 \times 0.172 = 122.06 \text{ kN-m}$$

Increase in positive moment in span A-B

$$M_L^- = M_A = 134.42 \text{ kN-m}$$

$$\text{Adjusted } M_R^- = M_{B, \text{left}} = 122.06 \text{ kN-m}$$

Repeat the same procedure as [Section 1.6](#) to calculate the maximum positive moment.

$$M_{\text{max}}^+ = \frac{w_u \times l_1^2}{8} - \frac{M_L^- + M_R^-}{2} + \frac{(M_L^- - M_R^-)^2}{2 \times w_u \times l_1^2} \text{ at distance } x_{\text{max}} = \frac{l_1}{2} + \frac{M_L^- - M_R^-}{w_u \times l_1}$$

$$M_{\text{max}}^+ = \frac{(31.75) \times 7.50^2}{8} - \frac{134.42 + 122.06}{2} + \frac{(134.42 - 122.06)^2}{2 \times (31.75) \times 7.50^2} = 95.04 \text{ kN-m}$$

$$x_{\text{max}} = \frac{7.50}{2} + \frac{(134.42 - 122.06)}{(31.75) \times 7.50} = 3.80 \text{ m}$$

Decrease in negative moment at the left face of support B

$$\text{Ordinate on line } M_A \text{ to } M_{B,\text{left}} = 134.42 + \frac{122.06 - 134.42}{7.50} \times 7.30 = 122.39 \text{ kN-m}$$

$$\text{Moment due to uniform load} = \frac{1}{2} \times w_f \times x \times (l - x) = \frac{1}{2} \times 31.75 \times 7.30 \times (7.50 - 7.30) = 23.18 \text{ kN-m}$$

$$\text{Adjusted negative moment at the left face of support B} = 122.39 - 23.18 = 99.21 \text{ kN-m}$$

Similar calculations are made to determine the adjusted moment at other locations and for other load patterns.

Results of the additional calculations are shown in the [following table](#).

| Table 3 – Moments Before and After Redistribution (Moments in kN-m) | | | | | | | | | | |
|---|----------------------|-----------|------------------------|-----------|------------------------|-----------|-------------------------|-----------|-----------------------|-----------|
| Location | Load Pattern I S2 | | Load Pattern II Odd | | Load Pattern III S3 | | Load Pattern IV Even | | Load Pattern V All | |
| | M_f | M_{adj} | M_f | M_{adj} | M_f | M_{adj} | M_f | M_{adj} | M_f | M_{adj} |
| A Center | -134.42 | -134.42 | -135.47 | -135.47 | -89.29 | -89.29 | -89.15 | -89.15 | -134.56 | -134.56 |
| A Right Face | -111.59 | -110.92 | -112.55 | -111.88 | -74.07 | -73.61 | -73.94 | -73.48 | -111.72 | -111.04 |
| Midspan A-B | 82.38 | 95.04 | 83.00 | 95.51 | 54.74 | 63.32 | 54.66 | 63.26 | 82.46 | 95.11 |
| B Left Face | -123.87 | -99.21 | -121.63 | -97.36 | -84.35 | -67.59 | -84.65 | -67.84 | -123.57 | -98.96 |
| B Left Center | -147.39 | -122.06 | -145.06 | -120.13 | -100.15 | -82.93 | -100.46 | -83.19 | -147.08 | -121.80 |
| B Right Center | -70.61 | -56.49 | -52.21 | -41.77 | -59.09 | -47.28 | -61.55 | -49.24 | -68.15 | -54.52 |
| B Right Face | -55.96 | -42.04 | -42.44 | -32.13 | -45.39 | -33.58 | -47.48 | -35.26 | -53.87 | -40.37 |
| Midspan B-C | 21.29 | 33.04 | 8.93 | 17.86 | 21.85 | 33.55 | 23.55 | 34.90 | 19.43 | 31.59 |
| C Left Face | -35.66 | -25.79 | -29.48 | -21.75 | -44.34 | -32.74 | -38.99 | -28.46 | -41.01 | -30.08 |
| C Left Center | -48.32 | -38.65 | -37.98 | -30.38 | -57.94 | -46.36 | -52.22 | -41.78 | -54.04 | -43.23 |
| C Right Center | -65.66 | -52.53 | -92.88 | -74.30 | -95.93 | -76.74 | -66.26 | -53.00 | -95.33 | -76.27 |
| C Right Face | -52.98 | -40.29 | -74.19 | -56.23 | -77.09 | -58.54 | -53.55 | -40.74 | -76.52 | -58.09 |
| Midspan C-D | 35.34 | 41.84 | 54.19 | 63.50 | 53.38 | 62.92 | 35.19 | 41.73 | 53.54 | 63.03 |
| D Left Face | -43.08 | -42.64 | -66.41 | -65.79 | -65.22 | -64.58 | -42.85 | -42.41 | -65.45 | -64.81 |
| D Center | -55.05 | -55.05 | -84.54 | -84.54 | -83.21 | -83.21 | -54.79 | -54.79 | -83.47 | -83.47 |

Final design moments after redistribution for critical sections (left and right support face & midspan)

After the adjusted bending moments have been determined analytically, the adjusted bending moment diagrams for each load pattern can be determined. The adjusted moment curves were determined graphically and are indicated by the dashed lines in [Figure 2](#) through [Figure 6](#).

An Adjusted maximum moment envelope can now be obtained from the adjusted moment curves as shown in [Figure 7](#) by dashed lines.

From the redistribution moment envelopes of [Figure 7](#), the design factored moments and the required reinforcement area are obtained as shown in [following table](#). Check example “[One-Way Wide Module \(Skip\) Joist Concrete Floor System Design \(ACI 318-14\)](#)” for detailed calculations for flexural and shear design of continuous beams.

| Table 4 – Summary of Final Design (comparison of % reduction and required Reinforcement) | | | | | | | |
|--|-------|------------------------------|---------------|-----------|--------------------------|---------------|--------|
| Location | | Moment at column face (kN-m) | | Load Case | A_s (mm ²) | | |
| | | Undistributed | Redistributed | | Undistributed | Redistributed | % |
| Support A | Right | -112.55 | -111.88 | II | 1,071 | 1,064 | 99.31 |
| Midspan A-B | | 83.00 | 95.51 | II | 757 | 886 | 117.08 |
| Support B | Left | -123.87 | -99.21 | I | 1,200 | 926 | 77.10 |
| | Right | -55.96 | -42.04 | I | 493 | 364 | 73.90 |
| Midspan B-C | | 23.55 | 34.90 | IV | <u>300</u> | <u>300</u> | 100.00 |
| Support C | Left | -44.34 | -32.74 | III | 385 | <u>300</u> | 77.86 |
| | Right | -77.09 | -58.54 | III | 698 | 517 | 74.18 |
| Midspan C-D | | 54.19 | 63.50 | II | 476 | 565 | 118.51 |
| Support D | Left | -66.41 | -65.79 | II | 593 | 587 | 98.99 |
| Italic underlined values indicate $A_{s,min} = 300.00 \text{ mm}^2$ governs | | | | | | | |

$$\text{Where } A_{s,min} = \left(\frac{0.2 \times \sqrt{f'_c}}{f_y} \times b_t \times h \right) = \left(\frac{0.2 \times \sqrt{25}}{400} \times 300.00 \times 400.00 \right) = 300.00 \text{ mm}^2 \quad \text{CSA A23.3-14 (10.5.1.2)}$$

3. Continuous Beam Analysis and Design Using Moment Redistribution – spBeam Software

[spBeam](#) is widely used for analysis, design and investigation of beams, and one-way slab systems (including standard and wide module joist systems) per latest Canadian (CSA A23.3-14) and American (ACI 318-14) codes. [spBeam](#) can be used for new designs or investigation of existing structural members subjected to flexure, shear, and torsion loads. With capacity to integrate up to 20 spans and two cantilevers of wide variety of floor system types, [spBeam](#) is equipped to provide cost-effective, accurate, and fast solutions to engineering challenges.

[spBeam](#) provides top and bottom bar details including development lengths and material quantities, as well as live load patterning and immediate and long-term deflection results. Using the moment redistribution feature engineers can deliver safe designs with savings in materials and labor. Engaging this feature allows up to 20% reduction of negative moments over supports reducing reinforcement congestions in these areas.

Redistribution of negative moments applies to one-way and beam systems only. It can be engaged using the **Design & Modeling Options** from the DEFINITIONS dialog box ([see the following figure](#)). The program allows for redistribution of negative moments at supports. Only reduction in negative moments is considered. Increase of negative moments at the support is not taken into account even though it is allowed by the code. Static equilibrium is maintained meaning that bending moments and shear forces along the span are adjusted in accordance with the reduction of moments applied at the supports.

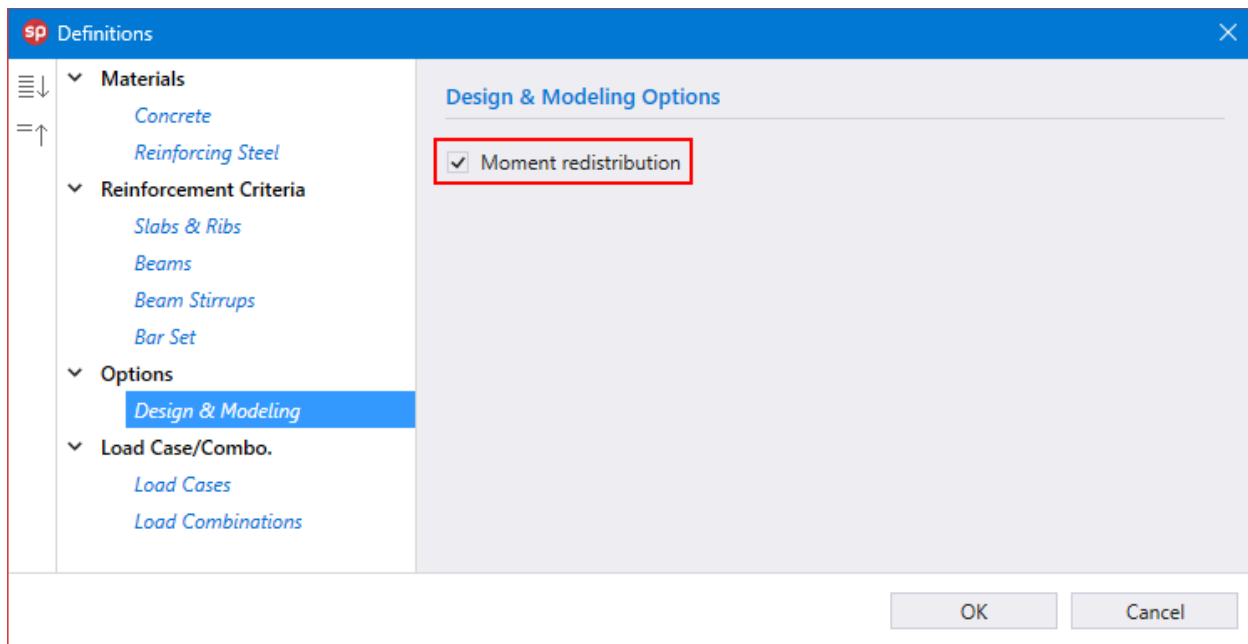


Figure 8 – Activating Moment Redistribution ([spBeam](#))

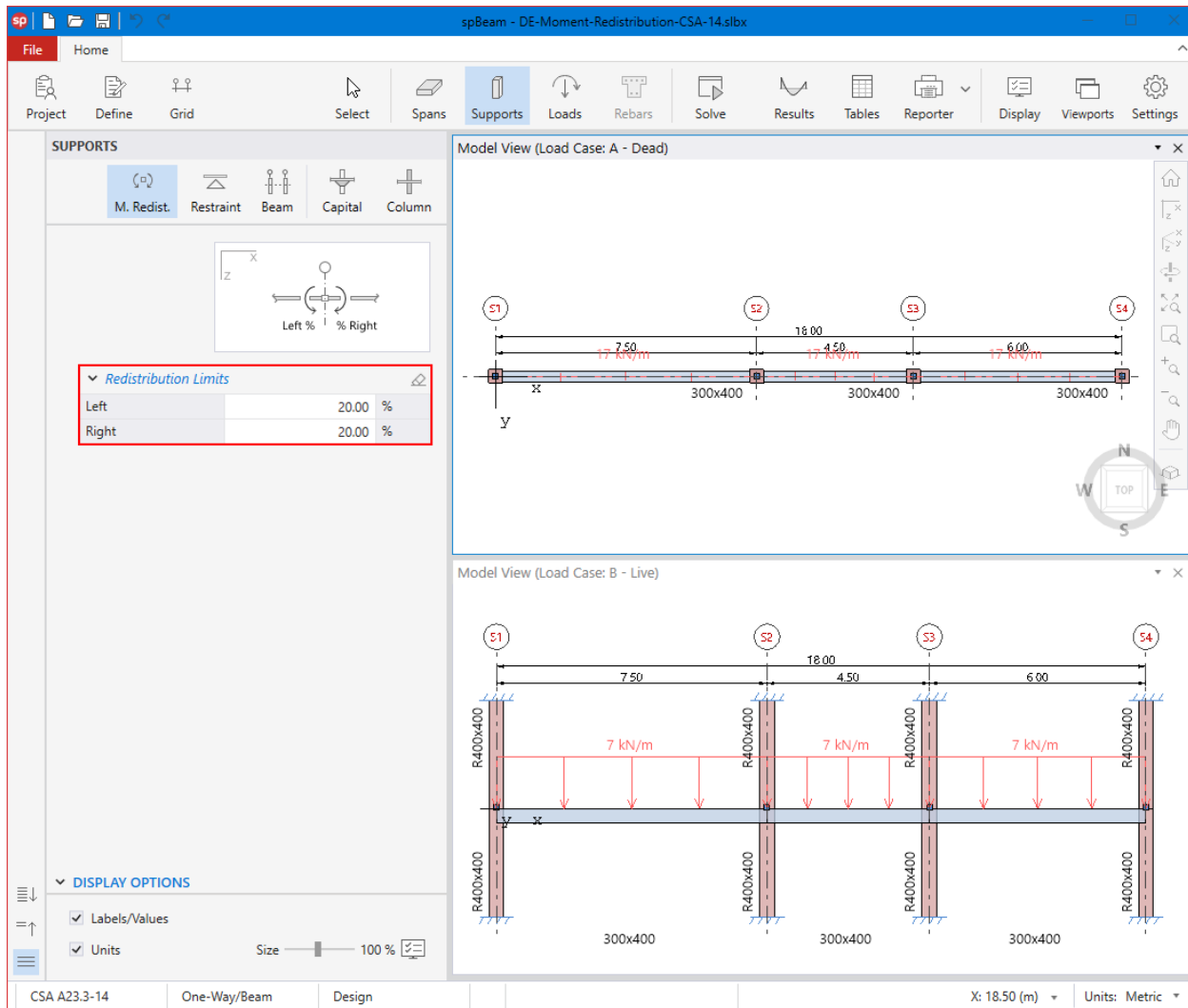


Figure 9 – Assigning Moment Redistribution Limits (spBeam)

From elastic static analysis, the largest moments from all load combinations and load patterns are determined at support faces on both ends of each span except cantilevers. These moments are used to calculate the maximum code allowable adjustment percentage of calculated moment.

In the investigation mode, program uses the area of provided reinforcement to obtain redistribution factors. In the design mode the required reinforcement area is used. The reduction percentage is limited to 20% and not to exceed the maximum values specified by the user. Negative moments at span ends are reduced by the amount of redistribution factors and new moment values are iteratively used to obtain new redistribution factors. This iterative procedure is repeated until the change in distribution factor is negligible (does not exceed 0.01%), but no more than 10 times.

For illustration and comparison purposes, the following figures provide a sample of the results obtained from an [spBeam](#) model created for the continuous beam in this example. Special emphasis can be given to [Figure 12](#) that illustrated the maximum and adjusted moments for span 2.

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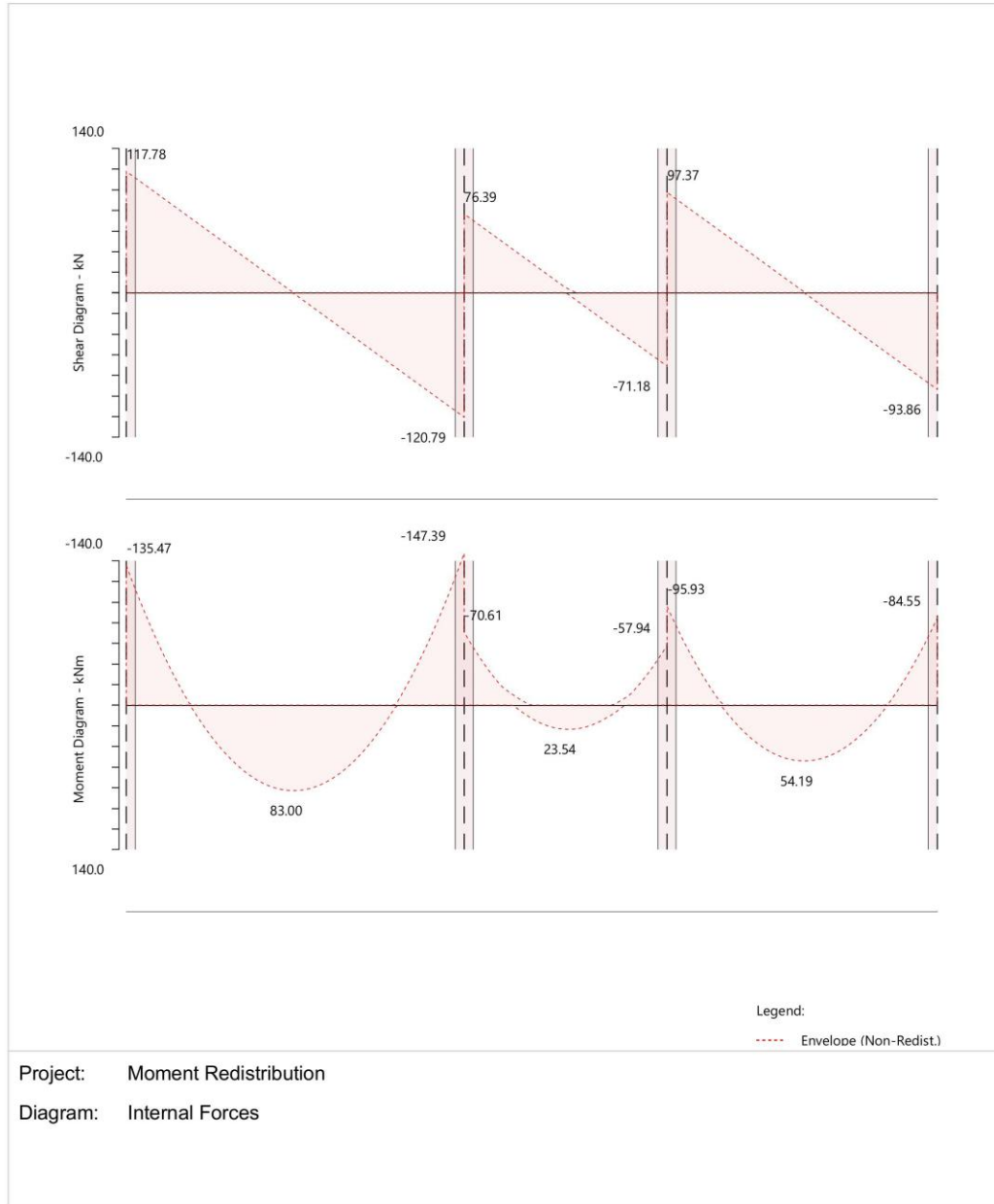


Figure 10 – Internal Forces before Moment Redistribution ([spBeam](#))

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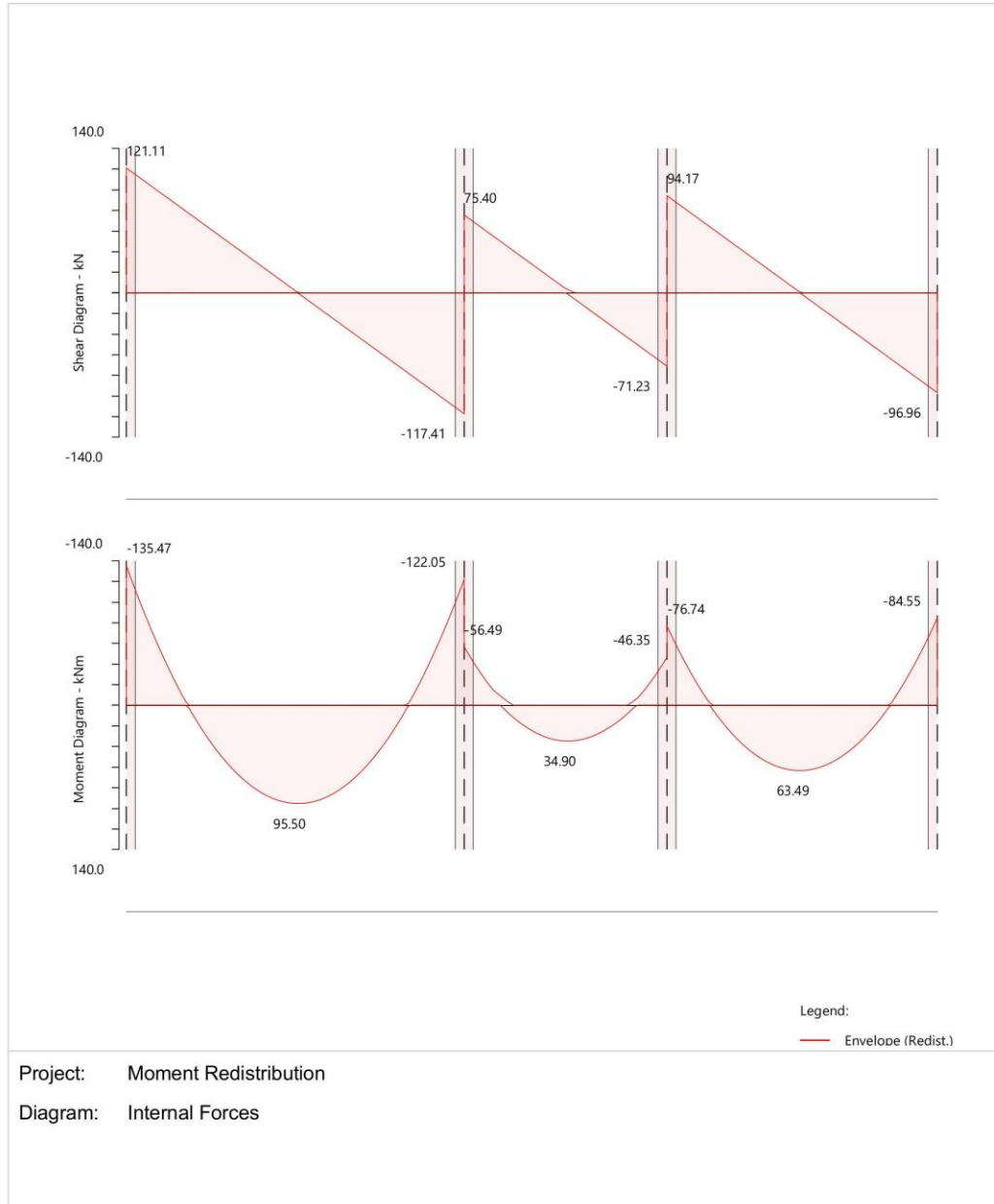


Figure 11 – Internal Forces after Moment Redistribution ([spBeam](#))

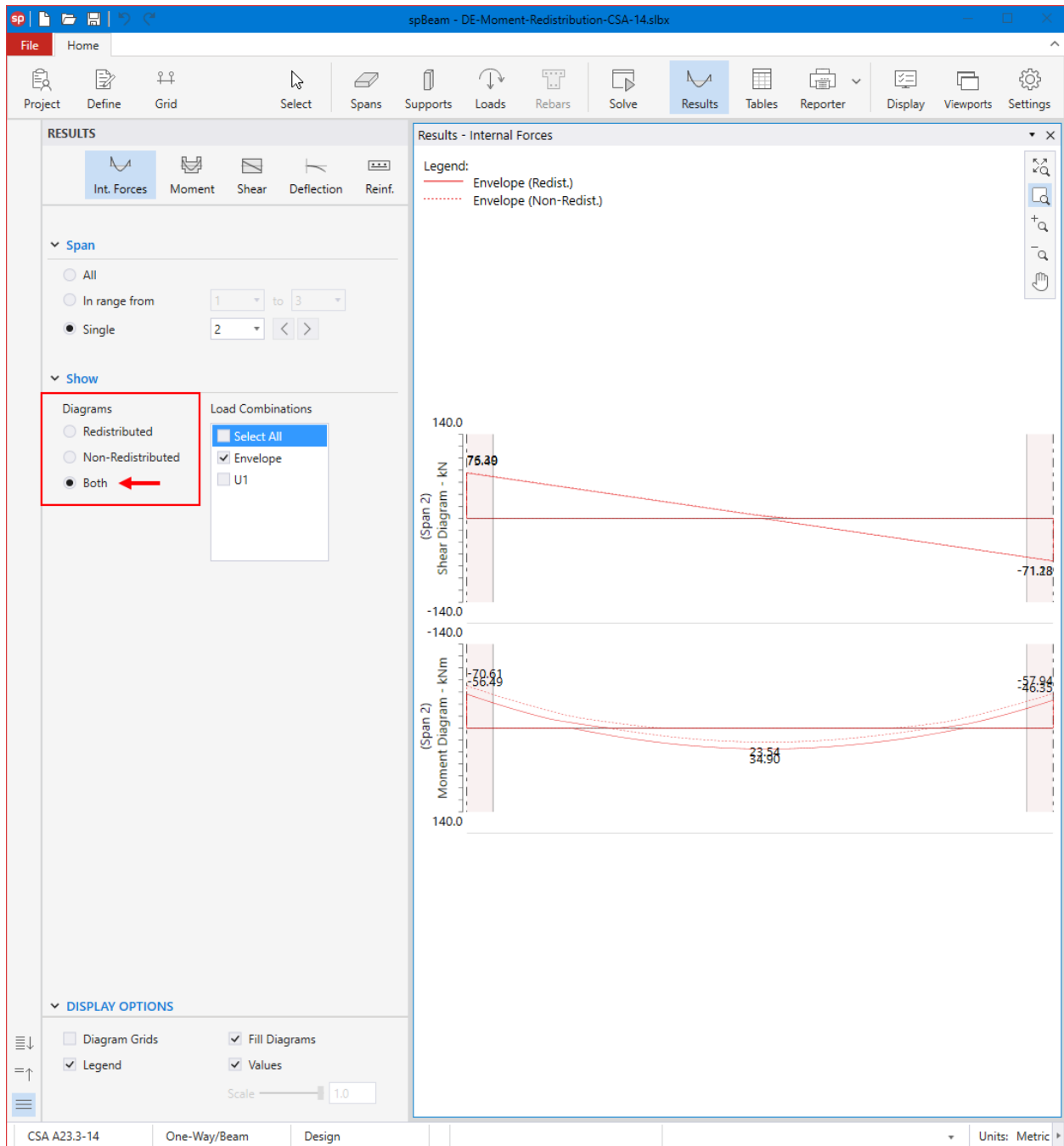
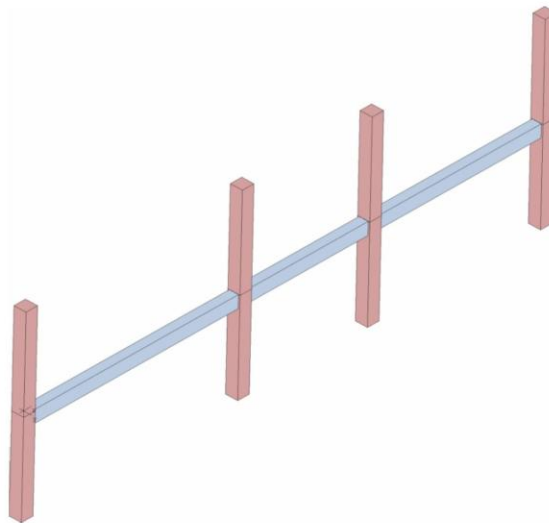


Figure 12 – Internal Forces before and after Moment Redistribution for Span 2 (spBeam)



spBeam v10.00 (TM)
A Computer Program for Analysis, Design, and Investigation of
Reinforced Concrete Beams and One-way Slab Systems
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1. Input Echo

1.1. General Information

| | |
|------------------------|---|
| File Name | C:\Struct...\DE-Moment-Redistribution-CSA-14.slbx |
| Project | Moment Redistribution |
| Frame | Exterior |
| Engineer | SP |
| Code | CSA A23.3-14 |
| Units | Metric |
| Reinforcement Database | CSA G30.18 |
| Mode | Design |
| Number of supports = | 4 |
| Floor System | One-Way/Beam |

1.2. Solve Options

| |
|---|
| Live load pattern ratio = 100% |
| Deflections are based on cracked section properties. |
| In negative moment regions, I_g and M_{cr} DO NOT include flange/slab contribution (if available) |
| Long-term deflections are calculated for load duration of 60 months. |
| 0% of live load is sustained. |
| Compression reinforcement calculations NOT selected. |
| Default incremental rebar design selected. |
| Combined M-V-T reinforcement design NOT selected. |
| Moment redistribution selected.  |
| Effective flange width calculations selected. |
| Rigid beam-column joint NOT selected. |
| Torsion analysis and design NOT selected. |

1.3. Material Properties

1.3.1. Concrete: Slabs / Beams

| | |
|------------------|--------------------------|
| w_c | 2447.3 kg/m ³ |
| f'_c | 25 MPa |
| E_c | 25683.5 MPa |
| f_r | 1.5 MPa |
| Precast concrete | No |

1.3.2. Concrete: Columns

| | |
|------------------|--------------------------|
| w_c | 2447.3 kg/m ³ |
| f'_c | 25 MPa |
| E_c | 25683.5 MPa |
| f_r | 3 MPa |
| Precast concrete | No |

1.3.3. Reinforcing Steel

| | |
|----------|------------|
| f_y | 400 MPa |
| f_{yt} | 400 MPa |
| E_s | 200000 MPa |

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Epoxy coated bars No

1.4. Reinforcement Database

| Size | Db mm | Ab mm ² | Wb kg/m | Size | Db mm | Ab mm ² | Wb kg/m |
|------|----------|-----------------------|------------|------|----------|-----------------------|------------|
| #10 | 11 | 100 | 1 | #15 | 16 | 200 | 2 |
| #20 | 20 | 300 | 2 | #25 | 25 | 500 | 4 |
| #30 | 30 | 700 | 5 | #35 | 36 | 1000 | 8 |
| #45 | 44 | 1500 | 12 | #55 | 56 | 2500 | 20 |

1.5. Span Data

1.5.1. Slabs

Notes:

| Span | Loc | L1 m | t mm | wL m | wR m | bE _{ff} mm | H _{min} mm |
|------|------|---------|---------|---------|---------|------------------------|------------------------|
| 1 | ExtL | 7.500 | 0 | 0.150 | 0.150 | 300 | 0 --- |
| 2 | ExtL | 4.500 | 0 | 0.150 | 0.150 | 300 | 0 --- |
| 3 | ExtL | 6.000 | 0 | 0.150 | 0.150 | 300 | 0 --- |

1.5.2. Ribs and Longitudinal Beams

Notes:

| Span | Ribs | | | Beams | | Span H _{min} mm |
|------|---------|---------|----------|---------|---------|--------------------------------|
| | b mm | h mm | Sp mm | b mm | h mm | |
| 1 | 0 | 0 | 0 | 300 | 400 | 394 |
| 2 | 0 | 0 | 0 | 300 | 400 | 195 |
| 3 | 0 | 0 | 0 | 300 | 400 | 311 |

1.6. Support Data

1.6.1. Columns

| Support | c1a mm | c2a mm | Ha m | c1b mm | c2b mm | Hb m | Red % |
|---------|-----------|-----------|---------|-----------|-----------|---------|-------|
| 1 | 400 | 400 | 3.000 | 400 | 400 | 3.000 | 100 |
| 2 | 400 | 400 | 3.000 | 400 | 400 | 3.000 | 100 |
| 3 | 400 | 400 | 3.000 | 400 | 400 | 3.000 | 100 |
| 4 | 400 | 400 | 3.000 | 400 | 400 | 3.000 | 100 |

1.6.2. Moment Redistribution Limits

| Support | Left % | Right % |
|---------|-----------|------------|
| 1 | 0 | 0 |
| 2 | 20 | 20 |
| 3 | 20 | 20 |
| 4 | 0 | 0 |

1.6.3. Boundary Conditions

| Support | Spring | | Far End | |
|---------|-------------------------|------------------------------|---------|-------|
| | K _x kN/mm | K _{ry} kN-mm/rad | Above | Below |
| 1 | 0.00 | 0.00 | Fixed | Fixed |
| 2 | 0.00 | 0.00 | Fixed | Fixed |

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| Support | Spring | | Far End | |
|---------|-------------------------|-----------------------------|---------|-------|
| | K _x kN/mm | K _y kN-mm/rad | Above | Below |
| 3 | 0.00 | 0.00 | Fixed | Fixed |
| 4 | 0.00 | 0.00 | Fixed | Fixed |

1.7. Load Data

1.7.1. Load Cases and Combinations

| Case Type | Dead DEAD | Live LIVE |
|-----------|-----------|-----------|
| U1 | 1.250 | 1.500 |

1.7.2. Line Loads

| Case/Patt | Span | W _a kN/m | L _a m | W _b kN/m | L _b m |
|-----------|------|------------------------|---------------------|------------------------|---------------------|
| Dead | 1 | 17.00 | 0.000 | 17.00 | 7.500 |
| | 2 | 17.00 | 0.000 | 17.00 | 4.500 |
| | 3 | 17.00 | 0.000 | 17.00 | 6.000 |
| Live | 1 | 7.00 | 0.000 | 7.00 | 7.500 |
| | 2 | 7.00 | 0.000 | 7.00 | 4.500 |
| | 3 | 7.00 | 0.000 | 7.00 | 6.000 |
| Live/Odd | 1 | 7.00 | 0.000 | 7.00 | 7.500 |
| | 3 | 7.00 | 0.000 | 7.00 | 6.000 |
| Live/Even | 2 | 7.00 | 0.000 | 7.00 | 4.500 |
| Live/S1 | 1 | 7.00 | 0.000 | 7.00 | 7.500 |
| Live/S2 | 1 | 7.00 | 0.000 | 7.00 | 7.500 |
| | 2 | 7.00 | 0.000 | 7.00 | 4.500 |
| Live/S3 | 2 | 7.00 | 0.000 | 7.00 | 4.500 |
| | 3 | 7.00 | 0.000 | 7.00 | 6.000 |
| Live/S4 | 3 | 7.00 | 0.000 | 7.00 | 6.000 |

1.8. Reinforcement Criteria

1.8.1. Slabs and Ribs

| | Units | Top Bars | | Bottom Bars | |
|-------------|-------|----------|------|-------------|------|
| | | Min. | Max. | Min. | Max. |
| Bar Size | | #35 | #35 | #35 | #35 |
| Bar spacing | mm | 25 | 457 | 25 | 457 |
| Reinf ratio | % | 0.14 | 5.00 | 0.14 | 5.00 |
| Clear Cover | mm | 38 | | 38 | |

There is NOT more than 300 mm of concrete below top bars.

1.8.2. Beams

| | Units | Top Bars | | Bottom Bars | | Stirrups | |
|-------------|-------|----------|------|-------------|------|----------|------|
| | | Min. | Max. | Min. | Max. | Min. | Max. |
| Bar Size | | #30 | #30 | #30 | #30 | #10 | #10 |
| Bar spacing | mm | 25 | 457 | 25 | 457 | 152 | 457 |
| Reinf ratio | % | 0.14 | 5.00 | 0.14 | 5.00 | | |
| Clear Cover | mm | 30 | | 30 | | | |
| Layer dist. | mm | 25 | | 25 | | | |
| No. of legs | | | | | | 2 | 6 |
| Side cover | mm | | | | | 30 | |
| 1st Stirrup | mm | | | | | 76 | |

There is NOT more than 300 mm of concrete below top bars.

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2. Design Results

2.1. Moment Redistribution Factors

| Support | Side | Org. M _u kNm | Calculated Iter.# | c/d | Factor % | User Limit % | Applied Factor % |
|---------|-------|----------------------------|----------------------|---------|-------------|--------------------|------------------------|
| 1 | Right | 112.55 | 5 | 0.22471 | 18.76 | 0.00 | 0.00 |
| 2 | Left | 123.87 | 6 | 0.25614 | 17.19 | 20.00 | 17.19 |
| 2 | Right | 55.96 | 2 | 0.10368 | 20.00 | 20.00 | 20.00 |
| 3 | Left | 44.34 | 2 | 0.08128 | 20.00 | 20.00 | 20.00 |
| 3 | Right | 77.09 | 2 | 0.14574 | 20.00 | 20.00 | 20.00 |
| 4 | Left | 66.41 | 2 | 0.12425 | 20.00 | 0.00 | 0.00 |

2.2. Top Reinforcement

Notes:

*3 - Design governed by minimum reinforcement.

| Span Zone | Width m | M _{max} kNm | X _{max} m | A _{s,min} mm ² | A _{s,max} mm ² | A _{s,req} mm ² | Sp _{Prov} mm | Bars |
|-----------|------------|-------------------------|-----------------------|---------------------------------------|---------------------------------------|---------------------------------------|--------------------------|----------|
| 1 Left | 0.30 | 111.88 | 0.200 | 300 | 2389 | 1064 | 183 | 2-#30 |
| Midspan | 0.30 | 0.00 | 3.750 | 0 | 2389 | 0 | 0 | --- |
| Right | 0.30 | 99.20 | 7.300 | 300 | 2389 | 925 | 183 | 2-#30 |
| 2 Left | 0.30 | 42.04 | 0.200 | 300 | 2389 | 364 | 183 | 2-#30 |
| Midspan | 0.30 | 0.00 | 2.250 | 0 | 2389 | 0 | 0 | --- |
| Right | 0.30 | 32.74 | 4.300 | 300 | 2389 | 281 | 183 | 2-#30 *3 |
| 3 Left | 0.30 | 58.54 | 0.200 | 300 | 2389 | 517 | 183 | 2-#30 |
| Midspan | 0.30 | 0.00 | 3.000 | 0 | 2389 | 0 | 0 | --- |
| Right | 0.30 | 65.79 | 5.800 | 300 | 2389 | 587 | 183 | 2-#30 |

2.3. Top Bar Details

NOTES:

* - Bar cut-off location shall be manually checked for compliance with CSA A23.3, 11.2.13.

| Span | Bars | Left | | Continuous | | Right | | | |
|------|-------|-------------|---------|-------------|------|-------------|------|-------------|------|
| | | Length m | Bars | Length m | Bars | Length m | Bars | Length m | Bars |
| 1 | 1-#30 | 1.84 | 1-#30 * | 1.29 | --- | 1-#30 | 1.76 | 1-#30 * | 1.15 |
| 2 | 1-#30 | 1.45 | 1-#30 * | 0.57 | --- | 1-#30 | 1.30 | 1-#30 * | 0.56 |
| 3 | 1-#30 | 1.38 | 1-#30 * | 0.73 | --- | 1-#30 | 1.45 | 1-#30 * | 0.80 |

2.4. Top Bar Development Lengths

| Span | Bars | Left | | Continuous | | Right | | | |
|------|-------|--------------|-------|--------------|------|--------------|--------|--------------|--------|
| | | DevLen mm | Bars | DevLen mm | Bars | DevLen mm | Bars | DevLen mm | Bars |
| 1 | 1-#30 | 1091.77 | 1-#30 | 1091.77 | --- | 1-#30 | 949.80 | 1-#30 | 949.80 |
| 2 | 1-#30 | 373.95 | 1-#30 | 373.95 | --- | 1-#30 | 300.00 | 1-#30 | 300.00 |
| 3 | 1-#30 | 531.03 | 1-#30 | 531.03 | --- | 1-#30 | 602.12 | 1-#30 | 602.12 |

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2.5. Bottom Reinforcement

Notes:

*3 - Design governed by minimum reinforcement.

| Span | Width m | M _{max} kNm | X _{max} m | A _{s,min} mm ² | A _{s,max} mm ² | A _{s,req} mm ² | Sp _{prov} mm | Bars |
|------|------------|-------------------------|-----------------------|---------------------------------------|---------------------------------------|---------------------------------------|--------------------------|----------|
| 1 | 0.30 | 95.50 | 3.787 | 300 | 2389 | 886 | 183 | 2-#30 |
| 2 | 0.30 | 34.90 | 2.287 | 300 | 2389 | 300 | 183 | 2-#30 *3 |
| 3 | 0.30 | 63.49 | 2.963 | 300 | 2389 | 564 | 183 | 2-#30 |

2.6. Bottom Bar Details

| Span | Long Bars | | | Short Bars | | |
|------|-----------|------------|-------------|------------|------------|-------------|
| | Bars | Start m | Length m | Bars | Start m | Length m |
| 1 | 2-#30 | 0.00 | 7.50 | --- | | |
| 2 | 2-#30 | 0.00 | 4.50 | --- | | |
| 3 | 2-#30 | 0.00 | 6.00 | --- | | |

2.7. Bottom Bar Development Lengths

| Span | Long Bars | | Short Bars | |
|------|-----------|--------------|------------|--------------|
| | Bars | DevLen mm | Bars | DevLen mm |
| 1 | 2-#30 | 909.49 | --- | |
| 2 | 2-#30 | 307.91 | --- | |
| 3 | 2-#30 | 579.43 | --- | |

2.8. Flexural Capacity

| Span | x m | A _{s,top} mm ² | Top | | Comb Pat | Status | Bottom | | | | |
|------|--------|---------------------------------------|--------------------------|-------------------------|----------|--------|---------------------------------------|--------------------------|-------------------------|----------|--------|
| | | | ΦM _n - kNm | M _u - kNm | | | A _{s,bot} mm ² | ΦM _n + kNm | M _u + kNm | Comb Pat | Status |
| 1 | 0.000 | 1400 | -140.40 | -135.47 | U1 Odd | --- | 1400 | 140.40 | 0.00 | U1 All | --- |
| | 0.200 | 1400 | -140.40 | -111.88 | U1 Odd | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 0.748 | 1049 | -110.56 | -53.81 | U1 Odd | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 1.292 | 351 | -40.60 | -5.54 | U1 Odd | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 1.840 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 33.91 | U1 S2 | OK |
| | 2.685 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 75.24 | U1 Odd | OK |
| | 3.750 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 95.42 | U1 Odd | OK |
| | 3.787 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 95.50 | U1 Odd | OK |
| | 4.815 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 79.60 | U1 Odd | OK |
| | 5.735 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 36.94 | U1 Odd | OK |
| | 6.350 | 453 | -51.72 | -8.06 | U1 S2 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 6.685 | 947 | -101.21 | -36.92 | U1 S2 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 7.300 | 1400 | -140.40 | -99.20 | U1 S2 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| 2 | 7.500 | 1400 | -140.40 | -122.05 | U1 S2 | --- | 1400 | 140.40 | 0.00 | U1 All | --- |
| | 0.000 | 1400 | -140.40 | -56.49 | U1 S2 | --- | 1400 | 140.40 | 0.00 | U1 All | --- |
| | 0.200 | 1400 | -140.40 | -42.04 | U1 S2 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 0.574 | 700 | -77.35 | -18.44 | U1 S2 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 1.079 | 700 | -77.35 | -0.03 | U1 S1 | OK | 1400 | 140.40 | 11.55 | U1 S3 | OK |

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| Span | x m | Top | | | | | Bottom | | | | |
|------|--------|---------------------------------------|--------------------------|-------------------------|----------|--------|---------------------------------------|--------------------------|-------------------------|----------|--------|
| | | A _{s,top} mm ² | ΦM _n - kNm | M _u - kNm | Comb Pat | Status | A _{s,bot} mm ² | ΦM _n + kNm | M _u + kNm | Comb Pat | Status |
| 3 | 1.453 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 23.45 | U1 Even | OK |
| | 1.635 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 27.82 | U1 Even | OK |
| | 2.250 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 34.84 | U1 Even | OK |
| | 2.287 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 34.90 | U1 Even | OK |
| | 2.865 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 29.86 | U1 Even | OK |
| | 3.196 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 22.33 | U1 S2 | OK |
| | 3.496 | 700 | -77.35 | 0.00 | U1 All | OK | 1400 | 140.40 | 13.08 | U1 S2 | OK |
| | 3.941 | 700 | -77.35 | -11.52 | U1 S3 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 4.241 | 1400 | -140.40 | -29.00 | U1 S3 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 4.300 | 1400 | -140.40 | -32.74 | U1 S3 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 4.500 | 1400 | -140.40 | -46.35 | U1 S3 | --- | 1400 | 140.40 | 0.00 | U1 All | --- |
| | 0.000 | 1400 | -140.40 | -76.74 | U1 S3 | --- | 1400 | 140.40 | 0.00 | U1 All | --- |
| | 0.200 | 1400 | -140.40 | -58.54 | U1 S3 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 0.731 | 700 | -77.35 | -16.39 | U1 S3 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 0.849 | 700 | -77.35 | -8.24 | U1 S3 | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 1.380 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 24.54 | U1 Odd | OK |
| | 2.160 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 53.67 | U1 Odd | OK |
| | 2.963 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 63.49 | U1 Odd | OK |
| | 3.000 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 63.43 | U1 Odd | OK |
| | 3.840 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 50.80 | U1 Odd | OK |
| | 4.545 | 0 | 0.00 | 0.00 | U1 All | OK | 1400 | 140.40 | 23.32 | U1 S3 | OK |
| | 5.147 | 700 | -77.35 | -13.43 | U1 Odd | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 5.198 | 700 | -77.35 | -16.99 | U1 Odd | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 5.800 | 1400 | -140.40 | -65.79 | U1 Odd | OK | 1400 | 140.40 | 0.00 | U1 All | OK |
| | 6.000 | 1400 | -140.40 | -84.55 | U1 Odd | --- | 1400 | 140.40 | 0.00 | U1 All | --- |

2.9. Longitudinal Beam Transverse Reinforcement Demand and Capacity

2.9.1. Section Properties

| Span | d _v mm | (A _v /s) _{min} mm ² /mm | ΦV _c kN | V _{r,max} kN |
|------|----------------------|---|-----------------------|--------------------------|
| 1 | 319.5 | 0.225 | 56.08 | 389.45 |
| 2 | 319.5 | 0.225 | 56.08 | 389.45 |
| 3 | 319.5 | 0.225 | 56.08 | 389.45 |

2.9.2. Beam Transverse Reinforcement Demand

Notes:

*8 - Minimum transverse (stirrup) reinforcement governs.

| Span | Start m | End m | Required | | | | Demand A _v /s mm ² /mm |
|------|------------|----------|---------------------|----------------------|-----------|--|--|
| | | | X _u m | V _u kN | Comb/Patt | A _v /s mm ² /mm | |
| 1 | 0.276 | 1.443 | 0.520 | 104.61 | U1/Odd | 0.313 | 0.313 |
| | 1.443 | 2.366 | 1.443 | 75.31 | U1/Odd | 0.124 | 0.225 *8 |
| | 2.366 | 3.289 | 2.366 | 46.00 | U1/Odd | 0.000 | 0.000 |
| | 3.289 | 4.211 | 3.289 | 16.70 | U1/Odd | 0.000 | 0.000 |
| | 4.211 | 5.134 | 5.134 | 42.31 | U1/S2 | 0.000 | 0.000 |
| | 5.134 | 6.057 | 6.057 | 71.61 | U1/S2 | 0.100 | 0.225 *8 |
| | 6.057 | 7.224 | 6.980 | 100.92 | U1/S2 | 0.289 | 0.289 |
| 2 | 0.276 | 1.014 | 0.520 | 58.90 | U1/S2 | 0.018 | 0.225 *8 |
| | 1.014 | 1.508 | 1.014 | 43.21 | U1/S2 | 0.000 | 0.000 |
| | 1.508 | 2.003 | 1.508 | 27.51 | U1/S2 | 0.000 | 0.000 |

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| Span | Start m | End m | Required | | | Demand | |
|------|------------|----------|------------|-------------|-----------|--------------------------------|--------------------------------|
| | | | X_u m | V_u kN | Comb/Patt | A_s/s mm ² /mm | A_s/s mm ² /mm |
| | 2.003 | 2.497 | 2.003 | 11.81 | U1/S2 | 0.000 | 0.000 |
| | 2.497 | 2.992 | 2.992 | 23.34 | U1/S3 | 0.000 | 0.000 |
| | 2.992 | 3.486 | 3.486 | 39.04 | U1/S3 | 0.000 | 0.000 |
| | 3.486 | 4.224 | 3.980 | 54.74 | U1/S3 | 0.000 | 0.225 *8 |
| 3 | 0.276 | 1.228 | 0.520 | 77.68 | U1/S3 | 0.139 | 0.225 *8 |
| | 1.228 | 1.937 | 1.228 | 55.18 | U1/S3 | 0.000 | 0.225 *8 |
| | 1.937 | 2.646 | 1.937 | 32.67 | U1/S3 | 0.000 | 0.000 |
| | 2.646 | 3.354 | 3.354 | 12.96 | U1/Odd | 0.000 | 0.000 |
| | 3.354 | 4.063 | 4.063 | 35.46 | U1/Odd | 0.000 | 0.000 |
| | 4.063 | 4.772 | 4.772 | 57.96 | U1/Odd | 0.012 | 0.225 *8 |
| | 4.772 | 5.724 | 5.480 | 80.46 | U1/Odd | 0.157 | 0.225 *8 |

2.9.3. Beam Transverse Reinforcement Details

| Span | Size | Stirrups (2 legs each unless otherwise noted) |
|------|------|---|
| 1 | #10 | 10 @ 220 + <-- 2769 --> + 10 @ 220 |
| 2 | #10 | 4 @ 211 + <-- 2472 --> + 4 @ 211 |
| 3 | #10 | 8 @ 221 + <-- 2126 --> + 8 @ 221 |

2.9.4. Beam Transverse Reinforcement Capacity

Notes:

*8 - Minimum transverse (stirrup) reinforcement governs.

| Span | Start m | End m | X_u m | V_u kN | Required Comb/Patt | A_s/s mm ² /mm | Reqd/Min | Provided | | | |
|------|------------|----------|------------|-------------|-----------------------|--------------------------------|----------|--------------------------|----------|--------------------------------|------------------|
| | | | | | | | | A_v mm ² | Sp mm | A_s/s mm ² /mm | ΦV_n kN |
| 1 | 0.000 | 0.276 | 0.520 | 104.61 | U1/Odd | ----- | ----- | ----- | ----- | ----- | ----- |
| | 0.276 | 2.366 | 0.520 | 104.61 | U1/Odd | 0.313 | 1.39 | 200.0 | 220 | 0.909 | 197.18 |
| | 2.366 | 5.134 | 2.366 | 46.00 | U1/Odd | 0.000 | 0.00 | ----- | ----- | ----- | 54.31 |
| | 5.134 | 7.224 | 6.980 | 100.92 | U1/S2 | 0.289 | 1.28 | 200.0 | 220 | 0.909 | 197.18 |
| | 7.224 | 7.500 | 6.980 | 100.92 | U1/S2 | ----- | ----- | ----- | ----- | ----- | ----- |
| 2 | 0.000 | 0.276 | 0.520 | 58.90 | U1/S2 | ----- | ----- | ----- | ----- | ----- | ----- |
| | 0.276 | 1.014 | 0.520 | 58.90 | U1/S2 | 0.018 | 0.08 | 200.0 | 211 | 0.949 | 203.30 *8 |
| | 1.014 | 3.486 | 1.014 | 43.21 | U1/S2 | 0.000 | 0.00 | ----- | ----- | ----- | 54.31 |
| | 3.486 | 4.224 | 3.980 | 54.74 | U1/S3 | 0.000 | 0.00 | 200.0 | 211 | 0.949 | 203.30 *8 |
| | 4.224 | 4.500 | 3.980 | 54.74 | U1/S3 | ----- | ----- | ----- | ----- | ----- | ----- |
| 3 | 0.000 | 0.276 | 0.520 | 77.68 | U1/S3 | ----- | ----- | ----- | ----- | ----- | ----- |
| | 0.276 | 1.937 | 0.520 | 77.68 | U1/S3 | 0.139 | 0.62 | 200.0 | 221 | 0.903 | 196.22 *8 |
| | 1.937 | 4.063 | 4.063 | 35.46 | U1/Odd | 0.000 | 0.00 | ----- | ----- | ----- | 54.31 |
| | 4.063 | 5.724 | 5.480 | 80.46 | U1/Odd | 0.157 | 0.70 | 200.0 | 221 | 0.903 | 196.22 *8 |
| | 5.724 | 6.000 | 5.480 | 80.46 | U1/Odd | ----- | ----- | ----- | ----- | ----- | ----- |

2.10. Slab Shear Capacity

| Span | b mm | d_v mm | β | V_{ratio} | ΦV_c kN | V_u kN | X_u m |
|------|---------|-------------|---------|-------------|------------------|-------------|------------|
| 1 | --- | Not checked | --- | | | | |
| 2 | --- | Not checked | --- | | | | |
| 3 | --- | Not checked | --- | | | | |

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2.11. Material TakeOff

2.11.1. Reinforcement in the Direction of Analysis

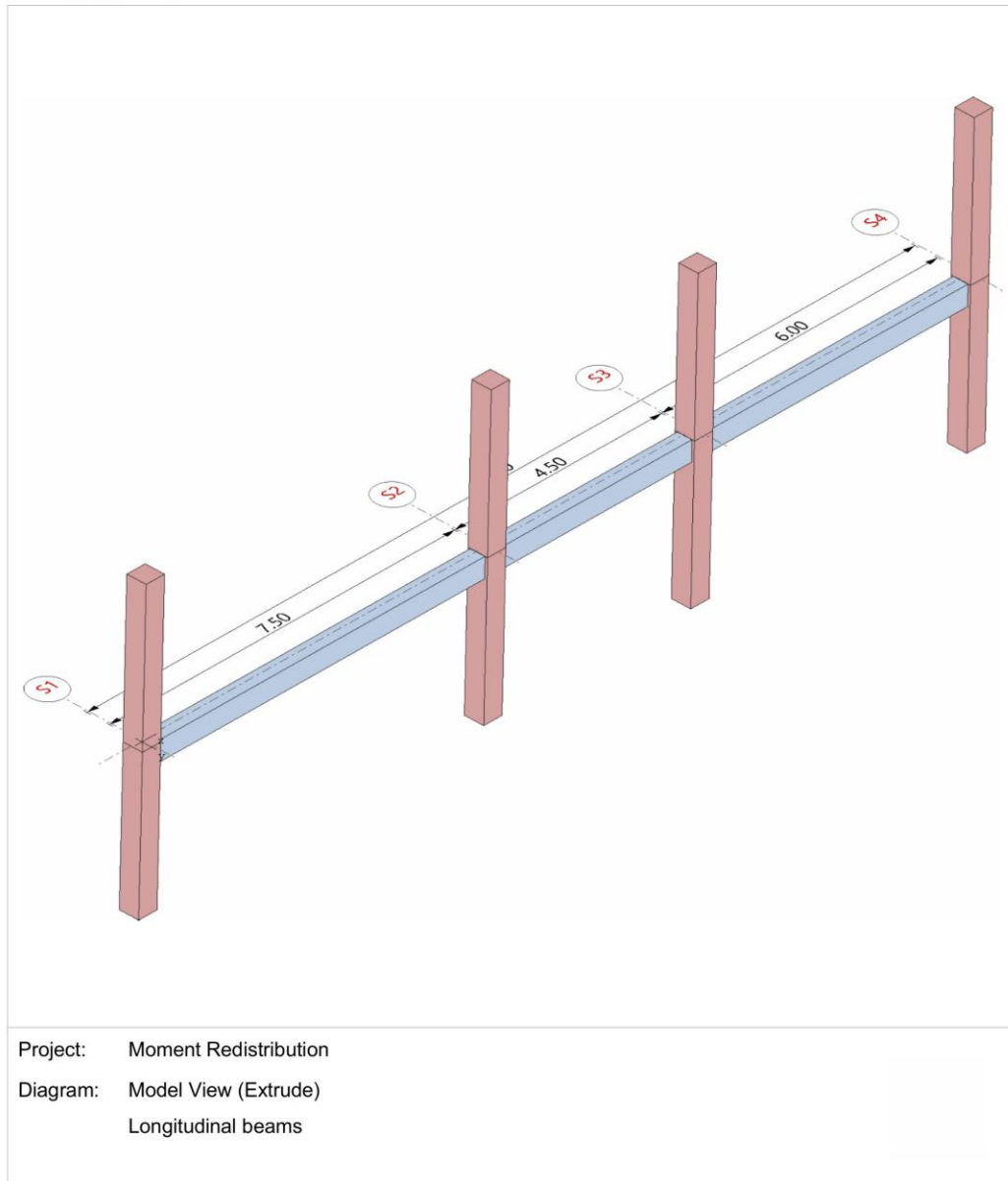
| | | | | | |
|-------------|--------------------|-----|------------------------|-----|--------------------------------------|
| Top Bars | 78.6 kg | <=> | 4.37 kg/m | <=> | 14.556 kg/m ² |
| Bottom Bars | 197.8 kg | <=> | 10.99 kg/m | <=> | 36.633 kg/m ² |
| Stirrups | 40.1 kg | <=> | 2.23 kg/m | <=> | 7.420 kg/m ² |
| Total Steel | 316.5 kg | <=> | 17.58 kg/m | <=> | 58.609 kg/m ² |
| Concrete | 2.2 m ³ | <=> | 0.12 m ³ /m | <=> | 0.400 m ³ /m ² |

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3. Screenshots

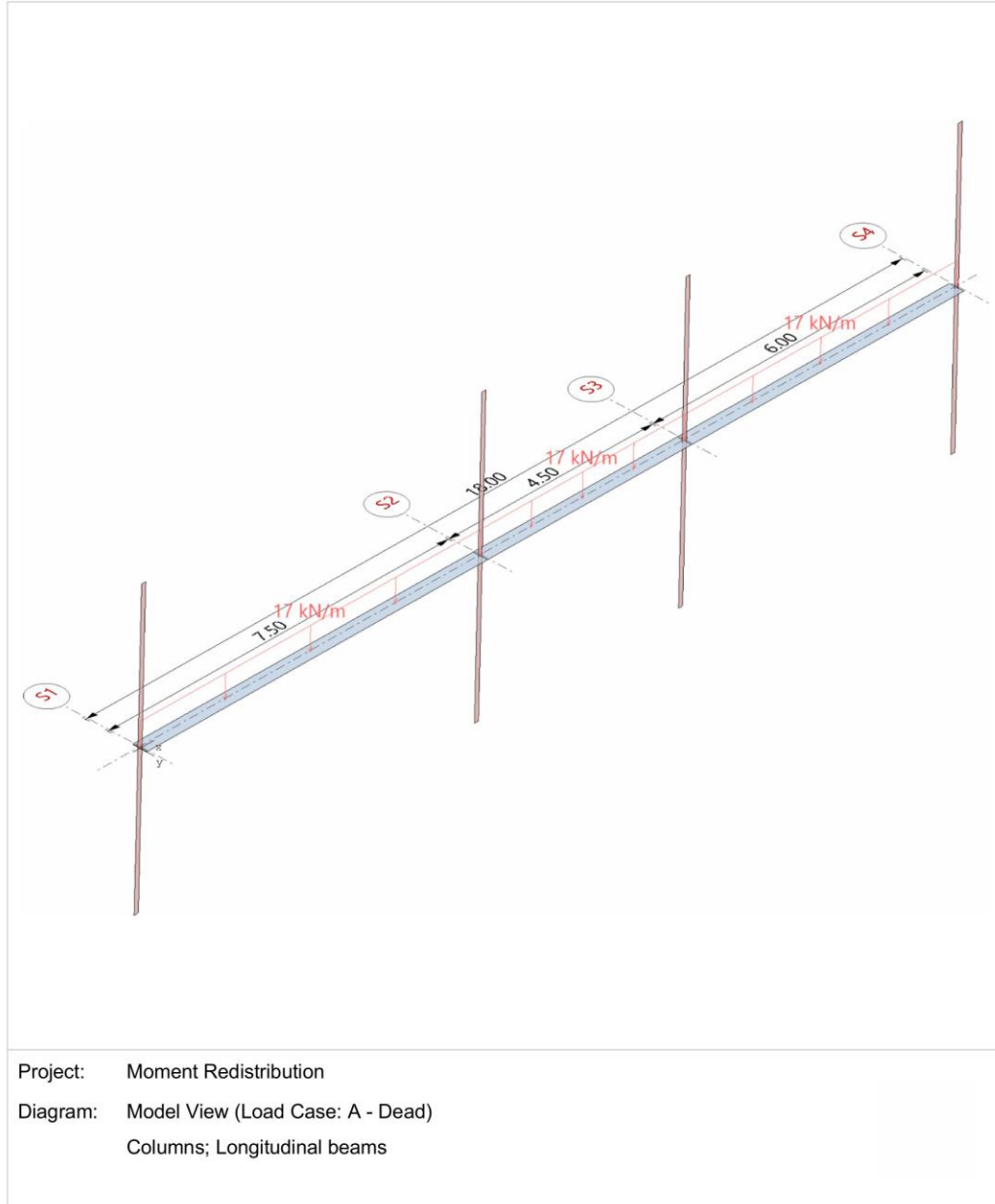
3.1. Extrude 3D view



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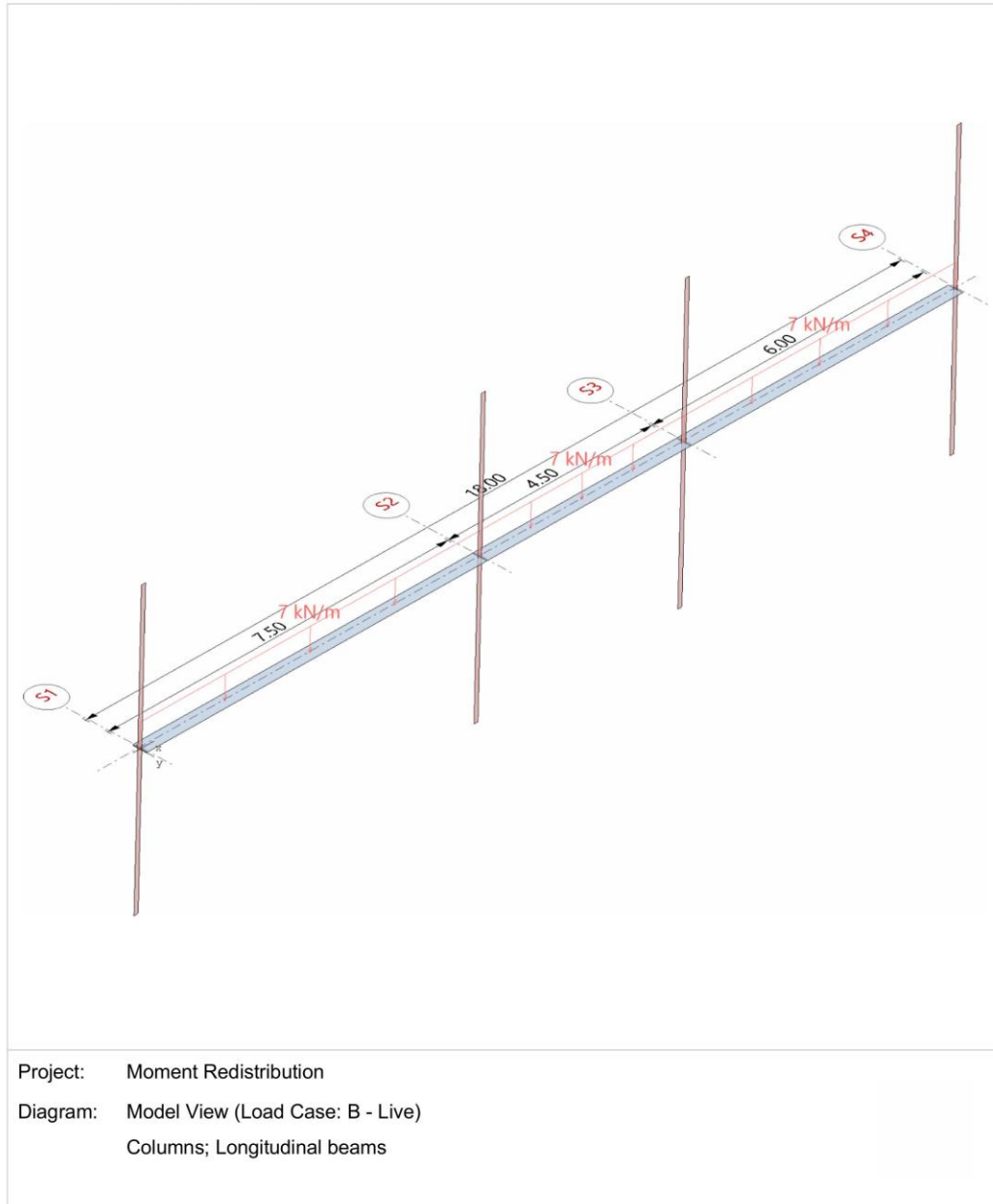
3.2. Loads - Case A - Dead



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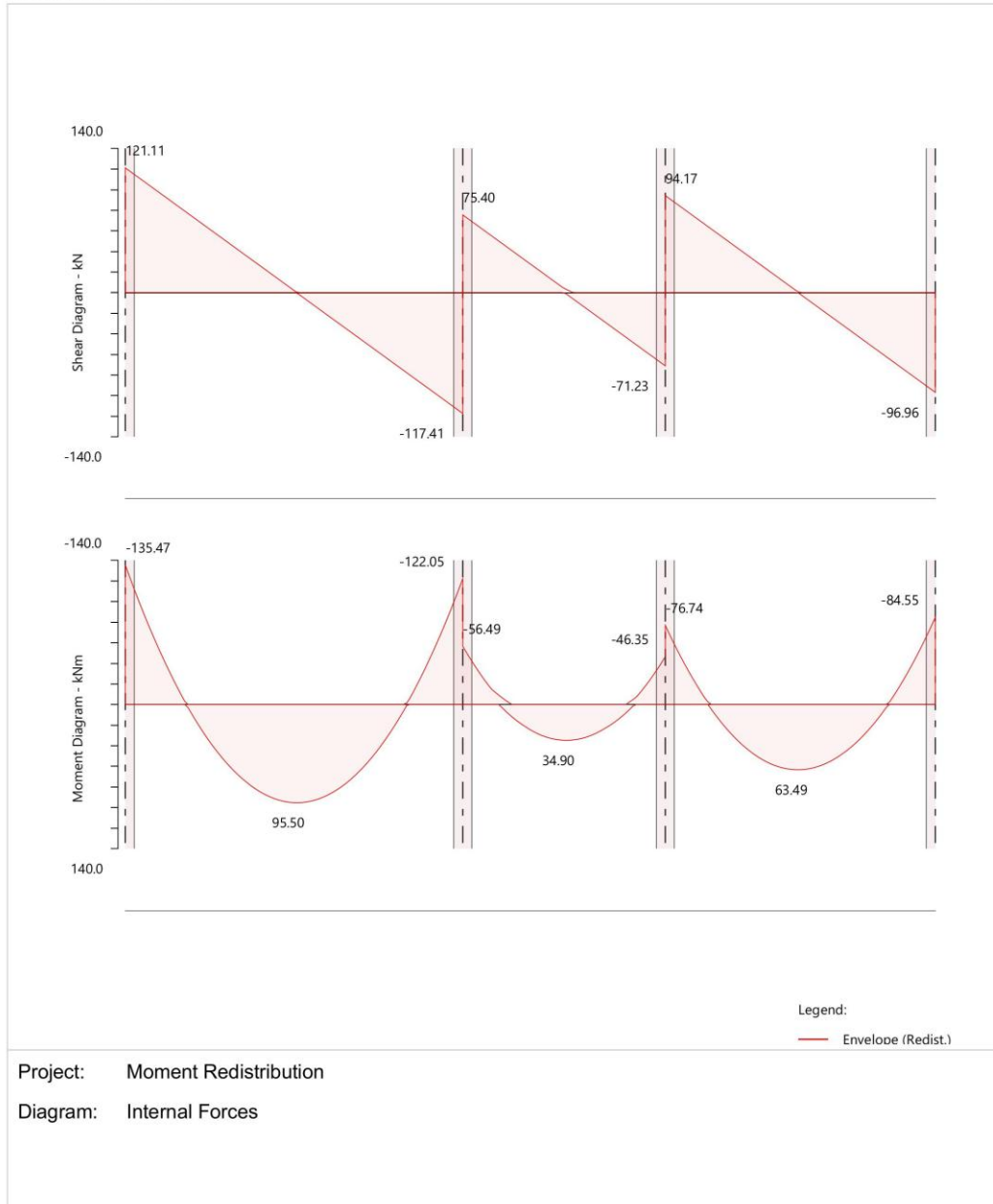
3.3. Loads - Case B - Live



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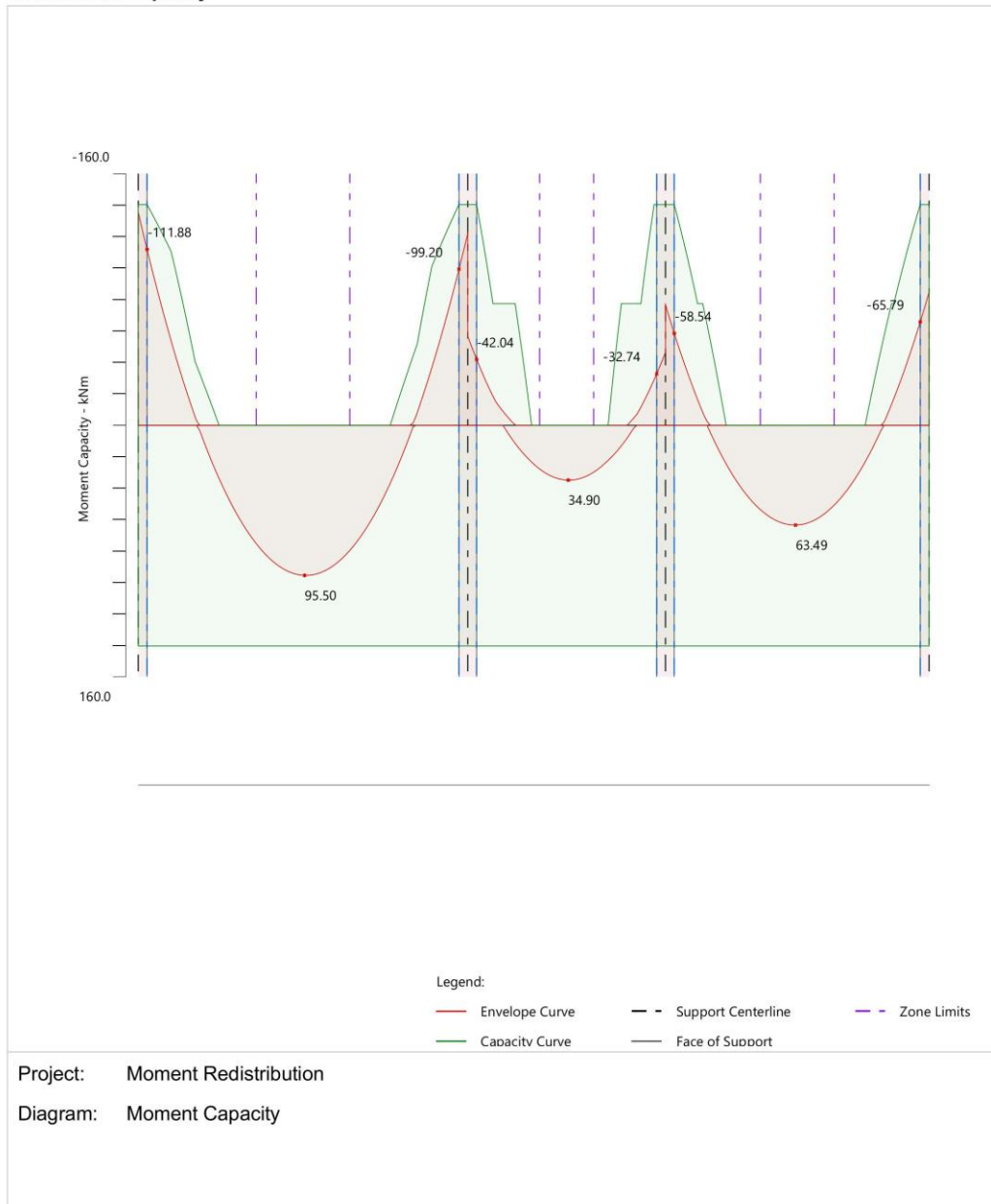
3.4. Internal Forces



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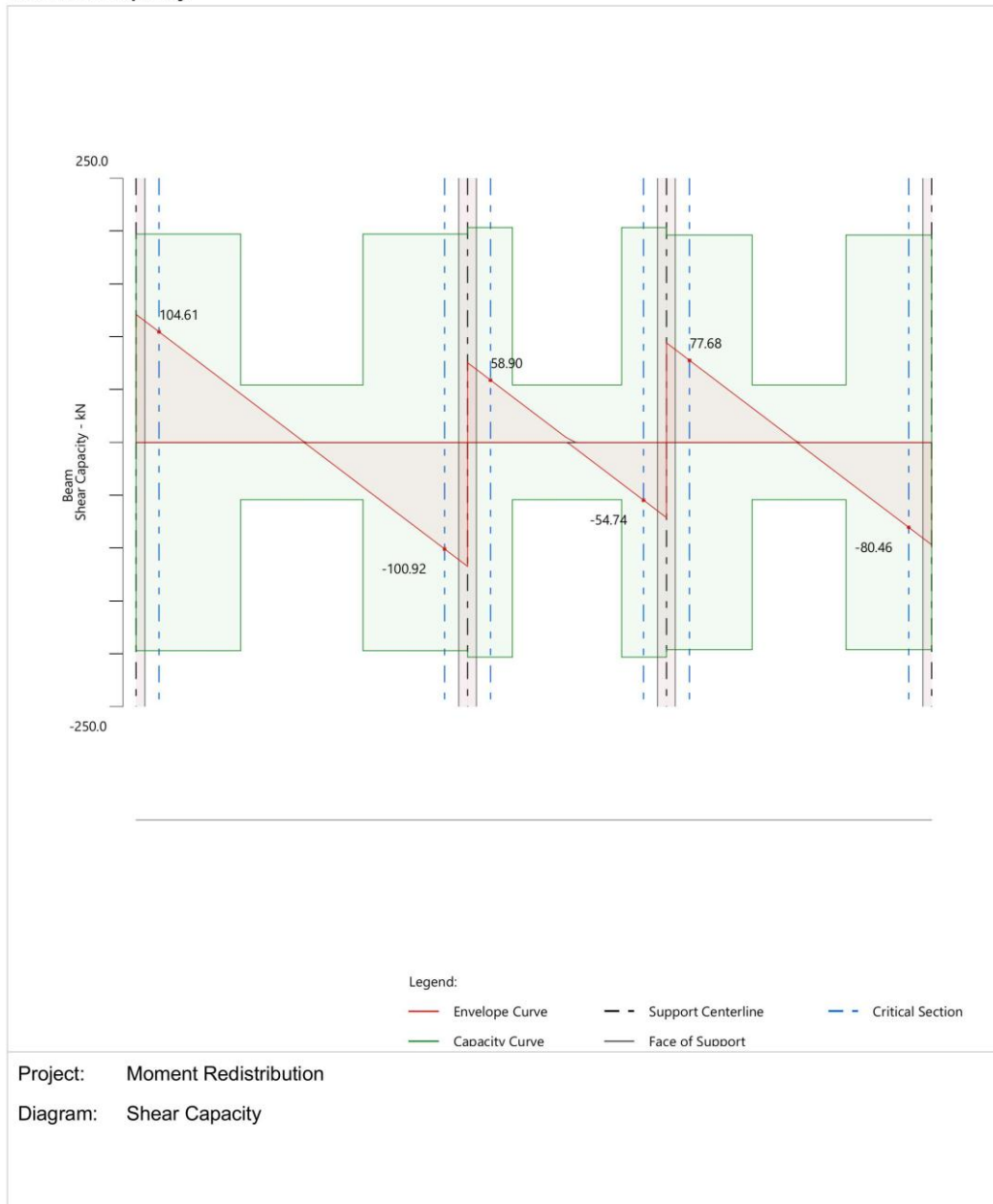
3.5. Moment Capacity



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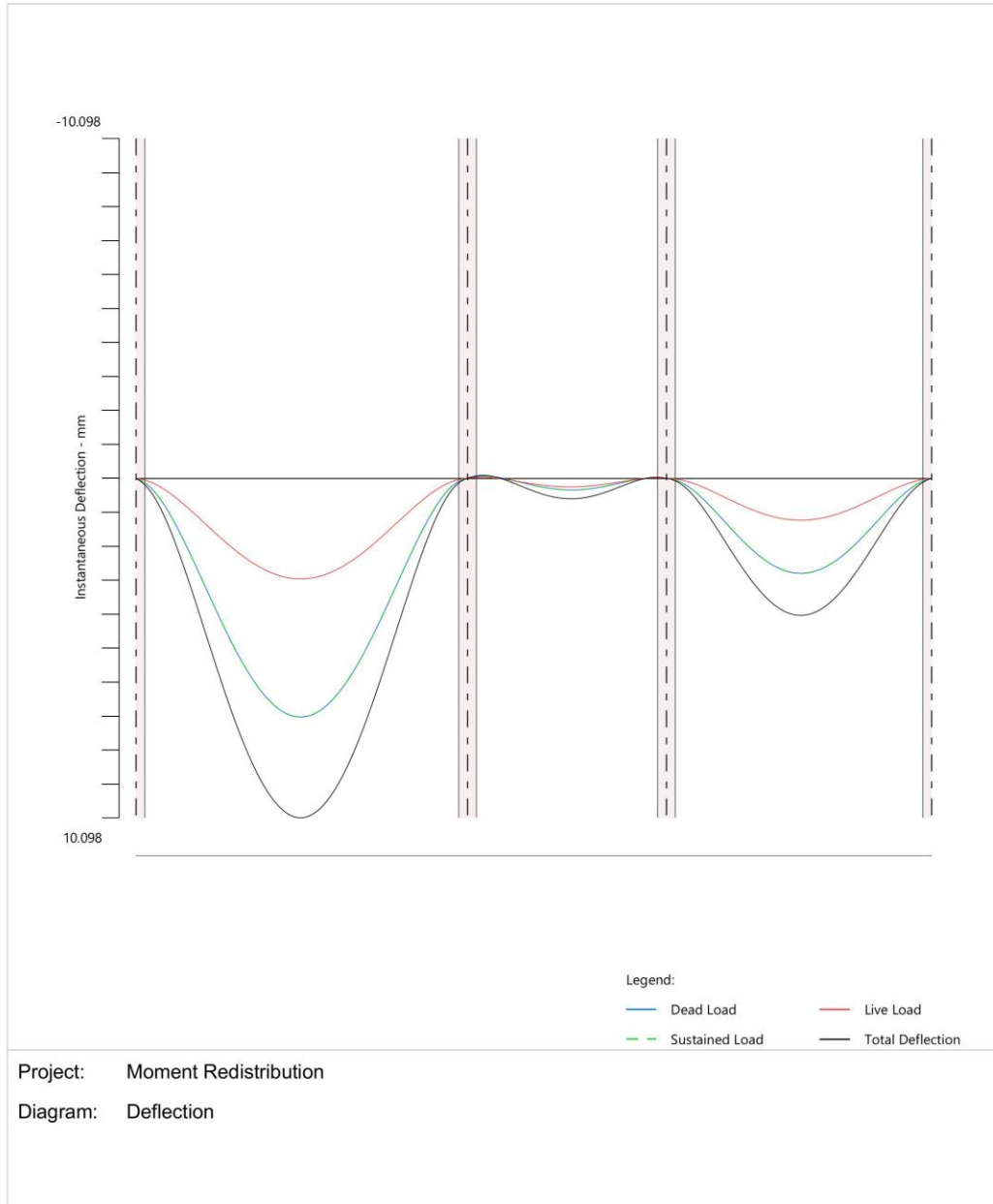
3.6. Shear Capacity



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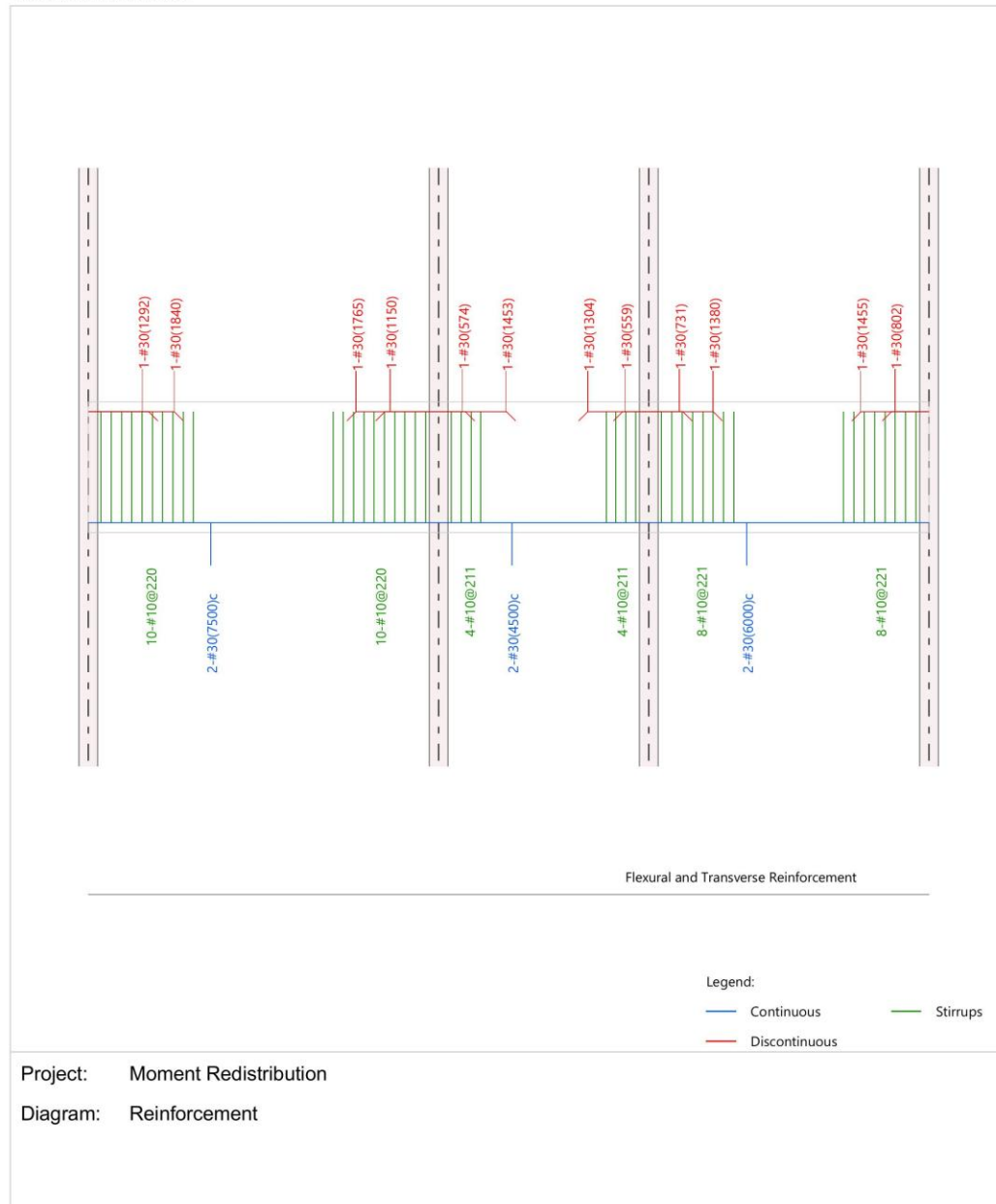
3.7. Deflection



STRUCTUREPOINT - spBeam v10.00 (TM)
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C:\StructurePoint\spBeam\DE-Moment-Redistribution-CSA-14.slbx

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3.8. Reinforcement



4. Design Results Comparison and Conclusions

The [following table](#) shows the comparison between hand results and [spBeam](#) model results.

| Table 5 – Comparison of the Continuous Beam Analysis and Design Results | | | | | | | |
|---|------------|---------------------------------------|------------------------|--------------------------------------|------------------------|--------------------------------|------------------------|
| Location | | M_f (kN-m) Before Redistribution | | M_f (kN-m) After Redistribution | | $A_{s,req}$ (mm ²) | |
| | | Hand | spBeam | Hand | spBeam | Hand | spBeam |
| Support A | Right Face | -112.55 | -112.55 | -111.88 | -111.88 | 1,064 | 1,064 |
| Midspan A-B | | 83.00 | 83.00 | 95.51 | 95.50 | 886 | 886 |
| Support B | Left Face | -123.87 | -123.87 | -99.21 | -99.20 | 926 | 925 |
| | Right Face | -55.96 | -55.96 | -42.04 | -42.04 | 364 | 364 |
| Midspan B-C | | 23.55 | 23.54 | 34.90 | 34.90 | 300* | 300* |
| Support C | Left Face | -44.34 | -44.34 | -32.74 | -32.74 | 300* | 300* |
| | Right Face | -77.09 | -77.09 | -58.54 | -58.54 | 517 | 517 |
| Midspan C-D | | 54.19 | 54.19 | 63.50 | 63.49 | 565 | 564 |
| Support D | Left Face | -66.41 | -66.41 | -65.79 | -65.79 | 587 | 587 |
| * $A_{s,min}$ governs | | | | | | | |

The results of all the hand calculations used illustrated above are in precise agreement with the automated exact results obtained from the [spBeam](#) program.

The moment redistribution is often utilized for the investigation of existing structures for conditions such as change of use, additional loading, or verifying adequacy for the latest design code. In these conditions, any reserve capacity from existing reinforcement layout at mid-span (or support) of a span may be utilized to compensate for the inadequacy of the support (or mid-span) of the same span.

The moment redistribution can also be utilized in the design of a new structure. One such example of its application may help reduce the negative moment at an interior support and corresponding top reinforcement while increasing the positive moment at mid-span. The advantage of this may be the alleviation of the congestion of rebar at support top regions.

The calculation of moment redistribution is a tedious process especially while considering live load patterning as presented in this example. The procedure gets far more complicated if point loads or partial line loads are present. The [spBeam](#) software program performs the moment redistribution calculations with speed and accuracy.