Multi-Story Tilt-Up Wall Panel with Openings Analysis and Design (ACI 551)
Reinforced Concrete Multi-Story Tilt-Up Wall Panel with Openings Analysis and Design (ACI 551)

Tilt-up is a form of construction with increasing popularity owing to its flexibility and economics. Tilt-up concrete is essentially a precast concrete that is site cast instead of traditional factory cast concrete members. A structural reinforced concrete multi-story tilt-up wall panel with openings in a building provides gravity and lateral load resistance for the applied loads from roof and floor joists.

The existing tilt-up wall panel in the following figure will be investigated to evaluate the as-built design to resist the applied gravity and lateral loads. The results, from ACI 318 procedure, will then be compared with numerical finite element analysis results obtained from spWall engineering software program from StructurePoint. Additionally, different modeling and analysis techniques using spWall software to investigate and design multi-story tilt-up wall panels with openings are discussed.

![Figure 1 – Reinforced Concrete Multi-Story Tilt-Up Wall Panel Geometry](image-url)
Contents

1. Method of Solution .................................................................................................................. 2
   1.1. Background .................................................................................................................... 2
   1.2. Tilt-Up Wall Panel Design Strips .................................................................................... 2
2. Tilt-Up Wall Structural Analysis ............................................................................................. 4
   2.1. Loads and Load Combinations ....................................................................................... 4
   2.2. Wall First Order Structural Analysis .............................................................................. 5
   2.3. Wall Second Order Structural Analysis ......................................................................... 6
3. Tilt-Up Wall Flexural Strength ................................................................................................. 7
   3.1. Wall Cracking Moment Capacity (Mcr) .......................................................................... 7
   3.2. Wall Flexural Moment Capacity (ϕMn) ........................................................................... 7
   3.3. Tilt-Up Wall Flexural Reinforcement ............................................................................. 8
4. Tilt-Up Wall Vertical Strength Check ..................................................................................... 8
5. Tilt-Up Wall Shear Strength Check ......................................................................................... 8
6. Tilt-Up Wall Panel Design Strip Analysis – spWall Software .................................................. 9
7. Design Results Comparison and Conclusions ......................................................................... 18
8. Comparison of Design Strip with Complete Wall Panel Analysis .......................................... 19
9. Complete Wall Panel Analysis – spWall Software .................................................................. 19
Code

Building Code Requirements for Structural Concrete (ACI 318-11) and Commentary (ACI 318R-11)

Reference


spWall Engineering Software Program Manual v5.01, STRUCTUREPOINT, 2016

Design Data

$f_{c'} = 4,000$ psi normal weight concrete ($w_c = 150$ pcf)

$f_y = 60,000$ psi

As-built wall thickness = 8.75 in.

Load eccentricity = $e_{cc} = 6.75$ in.

As-built vertical reinforcement: 4 #5 per layer (double layer) for the left leg (design strip)

4 #5 per layer (double layer) for the right leg (design strip)
1. Method of Solution

1.1. Background

According to ACI 551, continuous wall panels may be analyzed and designed using the alternative design method in ACI 318. The effect of openings on out-of-plane bending in tilt-up panels can be approximated in hand calculations by a simplified, one-dimensional strip analysis. Where openings occur, the entire lateral and axial load, including self-weight above the critical section, is distributed to supporting legs or design strips at each side of the opening (sometimes referred to as wall piers).

ACI 551.2R-15 (7.2)

The effective width of the strip should be limited to approximately 12 times the panel thickness to avoid localized stress concentrations along the edge of the opening. This limit is not mandated by ACI 318, but is included as a practical guideline where the opening width is less than one-half the clear vertical span. In most cases the tributary width for loads can be taken as the width of the strip plus one-half the width of adjacent openings. Tilt-up design strips should have constant properties for the full height and the reinforcement should not be cut off just above or below the opening. Thickened vertical or horizontal sections can be introduced within the panel where openings are large or where there are deep recesses on the exterior face. Some conditions may require ties around all vertical reinforcement bars in a vertical pilaster (wall pier) for the full height of the tilt-up panel. ACI 551.2R-15 (7.2)

No minimum limits are provided in ACI 551 on the width or thickness of the wall piers in panels with openings. Similarly, no limits are provided on horizontal sections (header beams) where openings are large. Therefore, slenderness effects and reinforcement size and confinement must be optimized to achieve adequate strength and stability. Slender column and deep beam provisions of ACI 318 can quickly become applicable in such circumstances. A detailed investigation of slenderness effects on the stability of the design strips is provided at the end of this example.

1.2. Tilt-Up Wall Panel Design Strips

Using ACI 551 guidance, the wall panel can be idealized as two design strips with constant section as shown. The left strip analysis and design will be carried out in details.
Figure 2 – Tilt-Up Design Strips Tributary Widths – Selfweight & Wind Loads
2. Tilt-Up Wall Structural Analysis

2.1. Loads and Load Combinations

Roof dead load \( (P_{DL}^{\text{roof}}) \) = 2.5 kip
Roof live load \( (P_{LL}^{\text{roof}}) \) = 2.0 kip
Floor dead load \( (P_{DL}^{\text{floor}}) \) = 17.6 kip
Floor live load \( (P_{LL}^{\text{floor}}) \) = 10.0 kip
Wind load = 27.2 psf (out of plane)
            = 0.00 psf (in plane)

The tributary width for loads can be taken as the width of the strip plus one-half the width of adjacent openings. Joists loads at each floor level including the roof are divided between the individual strips assuming an equivalent simply supported beams with the supports at the centerline of each strip.

Figure 3 – Tilt-Up Design Strips Tributary Widths – Dead & Live Loads
### Table 1 - Joists Loads at Each Floor Level

<table>
<thead>
<tr>
<th>Floor Level</th>
<th>Left Strip (L)</th>
<th>Right Strip (R)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>P&lt;sub&gt;DL&lt;/sub&gt;, kip</td>
<td>P&lt;sub&gt;LL&lt;/sub&gt;, kip</td>
</tr>
<tr>
<td>First</td>
<td>14.89</td>
<td>8.46</td>
</tr>
<tr>
<td>Second</td>
<td>14.89</td>
<td>8.46</td>
</tr>
<tr>
<td>Third</td>
<td>14.89</td>
<td>8.46</td>
</tr>
<tr>
<td>Roof</td>
<td>3.75</td>
<td>3.00</td>
</tr>
</tbody>
</table>

For maximum positive 1<sup>st</sup> order moment section (43 ft):

\[
\text{Wall self-weight} = \frac{8.75}{12} \times 150 \times \left[ 2 \times (5 + 14 + 2) + \frac{11}{2} \times (5 + 14 + 2 - 9) \right] \times \frac{1 \text{ kip}}{1000 \text{ lb}} = 11.8 \text{ kip}
\]

For maximum negative 1<sup>st</sup> order moment section (17 ft):

\[
\text{Wall self-weight} = \frac{8.75}{12} \times 150 \times \left[ 2 \times (64 - 17) + \frac{11}{2} \times (64 - 17 - 3 \times 9) \right] \times \frac{1 \text{ kip}}{1000 \text{ lb}} = 22.3 \text{ kip}
\]

Self-weight is calculated at the critical sections based on the 1<sup>st</sup> order moment diagram shown in the next section.

The load combination considered for structural analysis and design is 1.2D + 0.5L<sub>r</sub> + 1.0L + 1.0W.

#### 2.2. Wall First Order Structural Analysis

Using the loads and load combination calculated in the previous section, the moment diagram of 1<sup>st</sup> order moment can be obtained as shown in the following figure using the method illustrated later in this example.
Figure 4 – 1st Order Moment Diagram for Left Strip

2.3. Wall Second Order Structural Analysis

For maximum positive 1st order moment section (43 ft):

The maximum factored wall forces including moment magnification due to second order (P-Δ) effects can be calculated as follows:

\[
P_{\text{factored}} = 1.2 \times (3.75 + 14.89 + 11.80) + 0.5 \times 3.00 + 1.0 \times 8.46 = 46.51 \text{ kip}
\]

Calculate the effective area of longitudinal reinforcement in a slender wall for obtaining an approximate cracked moment of inertia.

\[
A_{se} = A_s + \frac{P_{\text{factored}} \times h}{2 \times f_y \times d} = 1.24 + \frac{46.51 \times 8.75}{2 \times 60 \times (8.75 - 1.69)} = 1.72 \text{ in.}^2
\]

\[
\text{ACI 318-11 (R14.8.3)}
\]

The following calculation are performed with the effective area of steel in lieu of the actual area of steel.

\[
a = \frac{A_{se} \times f_y}{0.85 \times f_y \times b} = \frac{1.72 \times 60}{0.85 \times 4 \times (2 \times 12)} = 1.27 \text{ in.}
\]

\[
c = \frac{a}{\beta} = \frac{1.27}{0.85} = 1.49 \text{ in.}
\]

\[
\phi = 0.9
\]

\[
\text{ACI 318-11 (9.3.2)}
\]

\[
I_{cr} = n \times A_{se} \times (d - c)^2 + \frac{E_s \times c^3}{3}
\]

\[
E_s = 57,000 \times \sqrt{f_y} = 57,000 \times \sqrt{4,000} = 3,605,000 \text{ psi}
\]

\[
n = \frac{E_s}{E_c} = \frac{29,000}{3,605} = 8.0 > 6.0 \text{ (o.k.)}
\]

\[
\text{ACI 318-11 (14.8.3)}
\]

\[
I_{cr} = 8.0 \times 1.72 \times (7.06 - 1.49)^2 + \frac{(2 \times 12) \times 1.49^3}{3} = 456 \text{ in.}^4
\]

\[
M_s = \frac{M_{\text{factored}}}{1 - \frac{P_{\text{factored}}}{0.75 \times K_b}}
\]

\[
\text{ACI 318-11 (Eq. 14-6)}
\]

Where \(M_{\text{factored}}\) is the maximum factored moment along the wall due to lateral and eccentric vertical loads, not including PΔ (second order) effects. This value can be seen in the previous figure.

\[
\text{ACI 318-11 (14.8.3)}
\]
\[ K_b = \frac{48 \times E_e \times I_{cr}}{5 \times l_e^2} = \frac{48 \times 3605 \times 456}{5 \times (14 \times 12)^2} = 559 \text{ kip} \]

\[ M_u = \frac{5.84}{1 - \frac{46.51}{0.75 \times 559}} = 6.57 \text{ ft-kip} \]

3. Tilt-Up Wall Flexural Strength

3.1. Wall Cracking Moment Capacity (\(M_{cr}\))

Determine \(f_c\) = Modulus of rupture of concrete and \(I_g\) = Moment of inertia of the gross uncracked concrete section to calculate \(M_{cr}\)

\[ f_c = 7.55 \sqrt{f_e} = 7.5 \times 1.0 \times \sqrt{4,000} = 474.3 \text{ psi} \quad \text{ACI 318-11 (Eq. 9-10)} \]

\[ I_g = \frac{l \times h^3}{12} = \frac{(2 \times 12) \times 8.75^3}{12} = 1340 \text{ in.}^4 \]

\[ y_e = \frac{h}{2} = \frac{8.75}{2} = 4.38 \text{ in.} \]

\[ M_{cr} = \frac{f_c I_g}{y_e} = \frac{474.3 \times 1340 \times 1000 \times 1}{4.38 \times 12} = 12.1 \text{ ft-kip} \quad \text{ACI 318-11 (Eq. 9-9)} \]

3.2. Wall Flexural Moment Capacity (\(\phi M_u\))

\[ M_u = A_w \times f_c \times \left( d - \frac{a}{2} \right) = 1.72 \times 60 \times \left( 7.06 - \frac{1.27}{2} \right) = 55.3 \text{ ft-kip} \]

It was shown previously that the section is tension controlled \(\Rightarrow \phi = 0.9\)

\[ \phi M_u = \phi \times M_u = 0.9 \times 55.30 = 49.80 \text{ ft-kip} > M_{cr} = 6.57 \text{ ft-kip} \quad \text{(o.k.)} \quad \text{ACI 318-11 (14.8.3)} \]

\[ \phi M_u = 49.80 \text{ ft-kip} > M_{cr} = 12.10 \text{ ft-kip} \quad \text{(o.k.)} \quad \text{ACI 318-11 (14.8.2.4)} \]

\[ \Delta_s = \frac{M_u}{0.75 \times K_b} = \frac{6.57 \times 12}{0.75 \times 559} = 0.188 \text{ in.} \quad \text{ACI 318-11 (Eq. 14-5)} \]

The same procedure was repeated for positive moment section at 8 ft height and negative moment section at 17 ft height (see the following table).

<table>
<thead>
<tr>
<th>Location</th>
<th>(M_{in}) (kip-ft)</th>
<th>(M_u) (kip-ft)</th>
<th>Magnifier</th>
<th>(D_{ult}) (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(y = 8 \text{ ft (Span 1)})</td>
<td>+5.63</td>
<td>+7.15</td>
<td>1.270</td>
<td>0.284</td>
</tr>
<tr>
<td>(y = 43 \text{ ft (Span 3)})</td>
<td>+5.84</td>
<td>+6.57</td>
<td>1.125</td>
<td>0.188</td>
</tr>
<tr>
<td>(y = 17 \text{ ft (Span 2)})</td>
<td>-14.71</td>
<td>-17.94</td>
<td>1.220</td>
<td>0.000</td>
</tr>
</tbody>
</table>
3.3. Tilt-Up Wall Flexural Reinforcement

At the maximum positive moment location in span 3, \( I_r \) equals 456 in.\(^4\) corresponding to 4 #5 bars. At this location, the wall capacity far exceeds the maximum moment (\( \phi M_u = 49.8 \text{ ft-kip} \gg M_u = 6.57 \text{ ft-kip} \)), the corresponding cracking coefficient (\( 0.75I_r/I_g \)) = 0.255. If this is used in a FEA like spWall, the resulting design flexural reinforcement will be far less than provided in this example. While this example uses a conservative As, a lower value may be possibly obtained for strength calculations by the optimization procedure as illustrated in section 13 of “Reinforced Concrete Tilt-Up Wall Panel with Opening Analysis and Design (ACI 551)” example in StructurePoint’s Design Examples Library.

4. Tilt-Up Wall Vertical Strength Check

\[
P_{sw} = \frac{46.51 \times 1000}{8.75 \times (2 \times 12)} = 221.5 \text{ psi} < 0.06 \times f'_c = 0.06 \times 4,000 = 240 \text{ psi (o.k.)}
\]

\( ACI 318-11 (14.8.2.6) \)

5. Tilt-Up Wall Shear Strength Check

In-plane shear is not evaluated since in-plane shear forces are not applied in this example. Out-of-plane shear due to lateral load should be checked against the shear capacity of the wall. By inspection of the maximum second order shear forces, it can be determined that the maximum shear force is under 3 kips. The wall has a shear capacity approximately 26.5 kips and no detailed calculations are required by engineering judgement. (See figure 9 for detailed shear force diagram).

Repeating the same process for the right leg (design strip) leads to the following results:

<table>
<thead>
<tr>
<th>Location</th>
<th>( M_{ua} ) (kip-ft)</th>
<th>( M_{u} ) (kip-ft)</th>
<th>Magnifier</th>
<th>( D_{z,\text{ultimate}} ) (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( y = 8 \text{ ft (Span 1)} )</td>
<td>+5.06</td>
<td>+6.30</td>
<td>1.245</td>
<td>0.255</td>
</tr>
<tr>
<td>( y = 43 \text{ ft (Span 3)} )</td>
<td>+4.27</td>
<td>+4.74</td>
<td>1.110</td>
<td>0.139</td>
</tr>
<tr>
<td>( y = 17 \text{ ft (Span 2)} )</td>
<td>-12.38</td>
<td>-14.74</td>
<td>1.191</td>
<td>0.000</td>
</tr>
</tbody>
</table>
6. Tilt-Up Wall Panel Design Strip Analysis – spWall Software

spWall is a program for the analysis and design of reinforced concrete shear walls, tilt-up walls, precast walls and Insulate Concrete Form (ICF) walls. It uses a graphical interface that enables the user to easily generate complex wall models. Graphical user interface is provided for:

- Wall geometry (including any number of openings and stiffeners)
- Material properties including cracking coefficients
- Wall loads (point, line, and area),
- Support conditions (including translational and rotational spring supports)

spWall uses the Finite Element Method for the structural modeling, analysis, and design of slender and non-slender reinforced concrete walls subject to static loading conditions. The wall is idealized as a mesh of rectangular plate elements and straight line stiffener elements. Walls of any geometry are idealized to conform to geometry with rectangular boundaries. Plate and stiffener properties can vary from one element to another but are assumed by the program to be uniform within each element.

Six degrees of freedom exist at each node: three translations and three rotations relating to the three Cartesian axes. An external load can exist in the direction of each of the degrees of freedom. Sufficient number of nodal degrees of freedom should be restrained in order to achieve stability of the model. The program assembles the global stiffness matrix and load vectors for the finite element model. Then, it solves the equilibrium equations to obtain deflections and rotations at each node. Finally, the program calculates the internal forces and internal moments in each element. At the user’s option, the program can perform second order analysis. In this case, the program takes into account the effect of in-plane forces on the out-of-plane deflection with any number of openings and stiffeners.

In spWall, the required flexural reinforcement is computed based on the selected design standard (ACI 318-11 is used in this example), and the user can specify one or two layers of wall reinforcement. In stiffeners and boundary elements, spWall calculates the required shear and torsion steel reinforcement. Wall concrete strength (in-plane and out-of-plane) is calculated for the applied loads and compared with the code permissible shear capacity.

For illustration and comparison purposes, the following figures provide a sample of the input modules and results obtained from an spWall model created for the reinforced concrete wall in this example. No in-plane forces were specified for this model.

In this example, ultimate load combination #1 is used in conjunction with one service load combination to report service and ultimate level displacements

Ultimate load combination #1: $1.2D + 0.5L_t + 1.0L + 1.0W$
Service load combination #1: $1.0D + 0.5L + 0.5W$
Special loading provisions are made to incorporate the self-weight and wind pressure from windows into the model. Care must be used in determining proper load application points based on windows and door anchorage to the wall. No in-plane lateral forces were specified for this model.

Figure 5 – Defining Loads (spWall)
Figure 6 – Tilt-Up Design Strip Service Displacements (in.) (spWall)
Figure 7 – Tilt-Up Design Strip Ultimate Displacements (in.) (spWall)
Figure 8 – Axial Force Diagram (kips) (spWall)
Figure 9 – Out-of-Plane Shear Force Diagram (kips) (spWall)
Figure 10 – First Order Bending Moment Diagram (kip-ft) (spWall)
Figure 11 – Second Order Bending Moment Diagram (kip-ft) (spWall)
**Figure 12 – Ultimate Displacement at Critical Sections (spWall)**

<table>
<thead>
<tr>
<th>Left Leg</th>
<th>8 ft</th>
</tr>
</thead>
<tbody>
<tr>
<td>25</td>
<td>-3.71e-004</td>
</tr>
<tr>
<td>26</td>
<td>-1.60e-013</td>
</tr>
<tr>
<td>27</td>
<td>3.71e-004</td>
</tr>
<tr>
<td>53</td>
<td>-7.00e-013</td>
</tr>
<tr>
<td>54</td>
<td>3.13e-004</td>
</tr>
<tr>
<td>130</td>
<td>-1.50e-004</td>
</tr>
<tr>
<td>131</td>
<td>-1.98e-012</td>
</tr>
<tr>
<td>132</td>
<td>1.98e-004</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Right Leg</th>
<th>9 ft</th>
</tr>
</thead>
<tbody>
<tr>
<td>28</td>
<td>-3.13e-004</td>
</tr>
<tr>
<td>29</td>
<td>-1.73e-013</td>
</tr>
<tr>
<td>30</td>
<td>3.13e-004</td>
</tr>
<tr>
<td>52</td>
<td>-2.65e-004</td>
</tr>
<tr>
<td>53</td>
<td>-6.01e-013</td>
</tr>
<tr>
<td>54</td>
<td>2.65e-004</td>
</tr>
<tr>
<td>130</td>
<td>-1.30e-004</td>
</tr>
<tr>
<td>131</td>
<td>-3.41e-012</td>
</tr>
<tr>
<td>132</td>
<td>1.30e-004</td>
</tr>
</tbody>
</table>
7. Design Results Comparison and Conclusions

The model shown above was created in spWall taking into account the ACI 318-11 provisions (alternative design method) and ACI 551 recommendations regarding the analysis and design of tilt-up wall panels with openings. In this model the left and right design strips are modeled such that the entire lateral and axial load, including self-weight above the critical section, are distributed to the two strips as idealized in Section 1. The following table shows the comparison between hand results with spWall model results.

<table>
<thead>
<tr>
<th>Output</th>
<th>Location (ft)</th>
<th>Design Strip</th>
<th>Hand</th>
<th>spWall</th>
</tr>
</thead>
<tbody>
<tr>
<td>M_u (kip-ft)</td>
<td>8 (+ve)</td>
<td>Left</td>
<td>7.15</td>
<td>8.25</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Right*</td>
<td>6.30</td>
<td>7.03</td>
</tr>
<tr>
<td></td>
<td>17 (-ve)</td>
<td>Left</td>
<td>-17.94</td>
<td>-16.32</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Right</td>
<td>-14.74</td>
<td>-13.56</td>
</tr>
<tr>
<td></td>
<td>43 (+ve)</td>
<td>Left</td>
<td>6.57</td>
<td>5.92</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Right</td>
<td>4.74</td>
<td>4.32</td>
</tr>
<tr>
<td>D_{uz} (kip-ft)</td>
<td>8 (+ve)</td>
<td>Left</td>
<td>0.284</td>
<td>0.357</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Right*</td>
<td>0.255</td>
<td>0.309</td>
</tr>
<tr>
<td></td>
<td>17 (-ve)</td>
<td>Left</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Right</td>
<td>0.000</td>
<td>0.000</td>
</tr>
<tr>
<td></td>
<td>43 (+ve)</td>
<td>Left</td>
<td>0.188</td>
<td>0.055</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Right</td>
<td>0.139</td>
<td>0.044</td>
</tr>
</tbody>
</table>

* Maximum positive moment occurs at 9 ft height for the right strip

The results of all the hand calculations used illustrated above are in agreement with the automated exact results obtained from the spWall program with observations, comments and recommendations discussed later in this section.
8. Comparison of Design Strip with Complete Wall Panel Analysis

ACI 318 provides the alternative design method as a simple and accurate option for analysis and design of simple walls meeting the method conditions. ACI 551 allows the use of this method for some cases were some of the method limitation do not meet where the results obtained are still within acceptable range. However, the combination of a multi-span continuous wall with the presence of openings brings a lot of challenges accompanied with the use of the alternative design method. To understand the wall behavior and adequately address strength and stability requirement, other methods such as finite element analysis can be used with panels similar to the one in this example that do not meet alternative design method conditions where continuous supports provides negative moments and maximum positive moment don’t occur at midspan. Many other issues arise with panels not meeting the method limitations (continuous and cantilevered walls, variable thickness and width, walls with openings, non-standard boundary conditions, walls with high compressive loads, in-plane lateral loads, non-standard concentrated load position from attachments of piping, racking etc., concentrated out of plane loads).

In the following section, the complete tilt-up wall panel geometry and loads are employed for illustration and comparison.

9. Complete Wall Panel Analysis – spWall Software

The exact wall geometry and applied loads were modeled using spWall engineering software to investigate the differences between the simplified approximate method using design strips and the finite element method for the complete panel with openings. For illustration and comparison purposes, the following figures provide a sample of the results obtained from an spWall model created for the complete panel.

It is very important to consider the wind load applied to the windows openings and how it must be considered and applied in the model based on the windows boundary condition. In this example, the windows support reactions are applied along the top and bottom of the windows openings. Load is modeled as an equivalent uniform line load applied along the top and bottom opening grids. The magnitude of this load is calculated as follows:

\[ W_{\text{door}} = 27.2 \times \frac{10}{2} \times \frac{1}{1000} = 0.136 \text{ kip/ft} \text{ for the 10’ long window} \]

\[ W_{\text{door}} = 27.2 \times \frac{9}{2} \times \frac{1}{1000} = 0.122 \text{ kip/ft} \text{ for the 9’ long windows} \]
Δ\text{allowable} = \frac{L}{150} = 1.12 \text{ in.}

Δ\text{allowable} = \frac{L}{150} = 1.12 \text{ in.}

Δ\text{allowable} = \frac{L}{150} = 1.12 \text{ in.}

Δ\text{allowable} = \frac{L}{150} = 1.36 \text{ in.}

Figure 13 – Complete Wall Service Displacements (in.) (spWall)
Figure 14 – Complete Wall Ultimate Displacements (in.) (spWall)
Figure 15 – Axial Force Diagram (kips) (spWall)
Figure 16 – Complete Wall Shear Force Diagram (kips) (spWall)
Figure 17 – Complete Wall First Order Moment Diagram (kip-ft) (spWall)
Figure 18 – Complete Wall Second Order Moment Diagram (kip-ft) (spWall)
From the table above, it can be observed that the complete wall deflections compare closely with the approximate design strips. However, the complete wall model requires fewer assumptions and approximations providing more reliable displacement estimates and better representation of the actual panel behavior.
10. Comments, Observations and Recommendations on the Current ACI 551 Procedure

The ACI 551 design guide illustrates tilt-up concrete walls analysis using the provisions of Chapter 14 of the ACI 318-11. Most walls, and especially slender walls, are widely evaluated using provisions from the “Alternative design of slender walls” in Section 14.8. The same provisions are presented in ACI 318-14 but reorganized in different chapters with slightly revised terminology. The provisions (or method) are applicable when the following conditions are met:

- The wall can be designed as simply supported  
  \( \text{ACI 318-11 (14.8.2.1)} \)
- The maximum moments and deflections occurring at midspan  
  \( \text{ACI 318-11 (14.8.2.1)} \)
- The wall must be axially loaded  
  \( \text{ACI 318-11 (14.8.2.1)} \)
- The wall must be subjected to an out-of-plane uniform lateral load  
  \( \text{ACI 318-11 (14.8.2.1)} \)
- The cross section shall be constant over the height of the wall  
  \( \text{ACI 318-11 (14.8.2.2)} \)
- The wall shall be tension-controlled  
  \( \text{ACI 318-11 (14.8.2.3)} \)
- The reinforcement shall provide design strength greater than cracking strength  
  \( \text{ACI 318-11 (14.8.2.4)} \)
- The concentrated loads application limits shall be met  
  \( \text{ACI 318-11 (14.8.2.5)} \)
- The vertical stress limit at midheight shall be met  
  \( \text{ACI 318-11 (14.8.2.6)} \)

For multi-story panels with openings, ACI 551 utilized the alternative design method even though several of the conditions above are not met. This example identified important issues (related to the utilization of ACI 551 approach with multi-story panels with/without openings) summarized in the following figure. A detailed discussion of these issues can found in “Commentary on Multi-Story Tilt-Up Panel Design Using ACI 551.2R-15” technical article in StructurePoint’s technical articles page.

![Figure 20 – First and Second Order Analyses (spWall)](image)