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Slenderness Effects for Concrete Columns in Sway Frame - Moment Magnification Method (CSA A23.3-94)











Slender Concrete Column Design in Sway Frame Buildings

Evaluate slenderness effect for columns in a sway frame multistory reinforced concrete building by designing the first story exterior column. The clear height of the first story is 4.75 m, and is 2.75 m for all of the other stories. Lateral load effects on the building are governed by wind forces. Compare the calculated results with the values presented in the Reference and with exact values from <u>spColumn</u> engineering software program from <u>StructurePoint</u>.



Figure 1 – Slender Reinforced Concrete Column Cross-Section



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Design of Concrete Structures (CSA A23.3-94) Explanatory Notes on CSA Standard A23.3-94

Reference

Reinforced Concrete Mechanics and Design, First Canadian Edition, 2000, James MacGregor and Michael Bartlett, Prentice Hall, Example 12-3, 4 and 5.

Design Data

 f_c ' = 25 MPa for columns

 $f_y = 400 \text{ MPa}$

Slab thickness = 180 mm

Exterior Columns = $500 \text{ mm} \times 500 \text{ mm}$

Interior Columns = $500 \text{ mm} \times 500 \text{ mm}$

Interior Beams = $450 \text{ mm} \times 750 \text{ mm} \times 9 \text{ m}$

Exterior Beams = $450 \text{ mm} \times 750 \text{ mm} \times 9.5 \text{ m}$

Total building loads in the first story from the reference:

Table 1 – Total building factored loads						
CSA A23.3-94 Reference	No.	Load Combination	$\sum P_{f}$, kN			
	1	1.25D	59,500			
	2	1.25D + 1.5L	77,500			
	3	1.25D + 1.5W	59,500			
8.3.2	4	1.25D - 1.5W	59,500			
	5	1.25D + 1.05L + 1.05W	72,100			
	6	1.25D + 1.05L - 1.05W	72,100			
	7	0.85D + 1.5W	40,460			
	8	0.85D - 1.5W	40,460			



1. Factored Axial Loads and Bending Moments

1.1. Service loads

Table 2 - Exterior column service loads						
Load Case	Axial Load,	Bending Moment, kN.m				
Load Case	kN	Тор	Bottom			
Dead, D	1,615.2	-107.36	-118			
Live, L	362.86	-67.43	-72.86			
Wind, W	0	-90.19	-105.33			

1.2. Load Combinations – Factored Loads

CSA A23.3-94 (8.3)

	Table 3 - Exterior column factored loads								
CSA A23.3-94 Reference	No.	Load Combination	Axial Load, kN	Load, kN.m		M _{Top,ns} kN.m	M _{Bottom,ns} kN.m	M _{Top,s} kN.m	M _{Bottom,s} kN.m
	1	1.25D	2,019	134.2	147.5	134.2	147.5	0	0
	2	1.25D + 1.5L	2,563	235.3	256.8	235.3	256.8	0	0
	3	1.25D + 1.5W	2,019	269.5	305.5	134.2	147.5	135.3	158
022	4	1.25D - 1.5W	2,019	-1.1	-10.5	134.2	147.5	-135.3	-158
8.3.2	5	1.25D + 1.05L + 1.05W	2,400	299.7	334.6	205	224	94.7	110.6
	6	1.25D + 1.05L - 1.05W	2,400	110.3	113.4	205	224	-94.7	-110.6
	7	0.85D + 1.5W	1,373	226.5	258.3	91.3	100.3	135.3	157.8
	8	0.85D – 1.5W	1,373	-44	-57.7	91.3	100.3	-135.3	-157.8

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Structure Point



2. Slenderness Effects and Sway or Nonsway Frame Designation

Columns and stories in structures are considered as nonsway frames if the stability index for the story (Q) does not exceed 0.05. <u>CSA A.23.3-94 (10.14.4)</u>

 $\sum P_f$ is the total factored vertical load in the first story corresponding to the lateral loading case for which $\sum P_f$ is greatest (without the wind loads, which would cause compression in some columns and tension in others and thus would cancel out). CSA A23.3-94 (10.14.4)

 V_{fs} is the total factored shear in the first story corresponding to the wind loads, and Δ_o is the first-order relative deflection between the top and bottom of the first story due to V_{f} . CSA A.23.3-94 (10.14.4)

From Table 1, load combination (1.25D + 1.5L) provides the greatest value of $\sum P_{f}$.

$$\Sigma P_f = 1.25 \times D + 1.5 \times L = 77,500 \text{ kN}$$

CSA A.23.3-94 (8.3.2)

Since there is no lateral load in this load combination, the reference applied an arbitrary lateral load as 1.05W representing (V_f) since the deflection calculated for this loading and calculated the resulting story lateral deflection (Δ_o).

 $V_f = 1,105 \text{ kN} \text{ (given)}$ $\Delta_o = 7.58 \text{ mm} \text{ (given)}$

$$Q = \frac{\Sigma P_f \times \Delta_o}{V_f \times I_c} = \frac{77,500 \times 7.58}{1,105 \times 5,500} = 0.0967 > 0.05$$

CSA A.23.3-94 (Eq. 10-14)

Thus, the frame at the first story level is considered sway.

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3. Determine Slenderness Effects

$$I_{column} = 0.7 \times \frac{c^4}{12} = 0.7 \times \frac{500^4}{12} = 3.65 \times 10^9 \text{ mm}^4$$
$$E_c = \left(3,300 \times \sqrt{f_c} + 6,900\right) \left(\frac{\gamma_c}{2,300}\right)^{1.5}$$
$$E_c = \left(3,300 \times \sqrt{25} + 6,900\right) \left(\frac{2,400}{2,300}\right)^{1.5} = 24,942.2 \text{ MPa}$$

For the column below level 2:

$$\frac{E_c \times I_{column}}{l_c} = \frac{24,942.2 \times 3.65 \times 10^9}{5,500} = 1.65 \times 10^{10} \text{ N.mm}$$

For the column above level 2:

$$\frac{E_c \times I_{column}}{l_c} = \frac{24,942.2 \times 3.65 \times 10^9}{3,500} = 2.6 \times 10^{10} \text{ N.mm}$$

For beams framing into the columns:

$$\frac{E_b \times I_{beam}}{l_b} = \frac{24,942.2 \times 5.54 \times 10^9}{9,500} = 1.45 \times 10^{10} \text{ N.mm}$$

Where:

$$E_{c} = \left(3,300 \times \sqrt{f_{c}} + 6,900\right) \left(\frac{\gamma_{c}}{2,300}\right)^{1.5}$$

$$E_{c} = \left(3,300 \times \sqrt{25} + 6,900\right) \left(\frac{2,400}{2,300}\right)^{1.5} = 24,942.2 \text{ MPa}$$

$$I_{beam} = 0.35 \times \frac{b \times h^{3}}{12} = 0.35 \times \frac{450 \times 750^{3}}{12} = 5.54 \times 10^{9} \text{ mm}^{4}$$

$$\Psi_{A} = \frac{\left(\sum \frac{EI}{l_{c}}\right)_{columns}}{\left(\sum \frac{EI}{l}\right)_{beams}} = \frac{1.65 + 2.6}{1.45} = 2.92$$

$$CSA A.23.3-94 (Eq. 8-6)$$

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$$CSA A.23.3-94 (Eq. 8-6)$$

$$CSA A.23.3-94 (Figure N.10.15.1)$$

 $\Psi_{B} = 1.0$ (Column considered fixed at the base)

Using Figure N10.15.1 from CSA A23.3-94 $\rightarrow k = 1.51$ as shown in the figure below for the exterior column.

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CSA A.23.3-94 (Figure N.10.15.1)







Figure 2 – Effective Length Factor (k) for Exterior Column (Sway Frame)

Note: CSA A23.3-94 (Cl. 10.15.2) allows to neglect the slenderness in a non-sway frame. However, there is no such clause in for sway frames. The CSA A23.3-94 committee intended that all columns in sway frames should be designed for slenderness.

4. Moment Magnification at Ends of Compression Member

A detailed calculation for load combinations 2 and 5 is shown below to illustrate the slender column moment magnification procedure. Table 4 summarizes the magnified moment computations for the exterior columns.

4.1. Gravity Load Combination #2 (Gravity Loads Only)

$$M_2 = M_{2ns} + \delta_s M_2$$

Where:

$$M_{Top s} = M_{Bottom s} = M_2 s = 0 \text{ kN.m}$$

$$\therefore M_2 = M_{2ns}$$

 $M_{Top_2^{nd}} = M_{Top,ns} = -235 \text{ kN.m}$

 $M_{Bottom 2^{nd}} = M_{Bottom,ns} = -257 \text{ kN.m}$

CSA A23.3-94 (Eq. 10-22)



$$M_{2_{2}2^{nd}} = max \left(M_{Top_{2}2^{nd}}, M_{Bottom_{2}2^{nd}} \right) = M_{Bottom_{2}2^{nd}} = -257 \text{ kN.m} \rightarrow M_{2_{2}1^{st}} = M_{Bottom_{1}1^{st}} = -257 \text{ kN.m}$$
$$M_{1_{2}2^{nd}} = min \left(M_{Top_{2}2^{nd}}, M_{Bottom_{2}2^{nd}} \right) = M_{Top_{2}2^{nd}} = -235 \text{ kN.m} \rightarrow M_{1_{1}1^{st}} = M_{Top_{1}1^{st}} = -235 \text{ kN.m}$$

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 $P_f = 2,563 \text{ kN}$

4.2. Lateral Load Combination #5 (Gravity Plus Wind Loads)

$$M_2 = M_{2ns} + \delta_s M_{2s}$$
 CSA A23.3-94 (Eq. 10-22)

Where:

$$\delta_{s} = \text{ moment magnifier} = \begin{cases} (1) \text{ Second-order analysis} \\ (2) \frac{1}{1 - \frac{\Sigma P_{f}}{\phi_{m} \Sigma P_{c}}} \\ (3) \frac{1}{1 - Q}, \text{ if } Q < 1/3 \end{cases}$$

$$\underbrace{CSA \ A23.3-94 \ (10.16.3)}_{CSA \ A23.3-94 \ (10.16.3)}$$

There are three options for calculating δ_s . CSA A23.3-94 (10.16.3.2) will be used since it does not require a detailed structural analysis model results to proceed and is also used by the solver engine in spColumn.

 $\sum P_f$ is the summation of all the factored vertical loads in the first story, and $\sum P_c$ is the summation of the critical buckling load for all sway-resisting columns in the first story.

$$P_{c} = \frac{\pi^{2} EI}{\left(kl_{u}\right)^{2}}$$
 CSA A23.3-94 (Eq. 10-17)

Where:

$$EI = \begin{cases} (a) \frac{0.2E_c I_g + E_s I_{st}}{1 + \beta_d} \\ (b) \ 0.25 \ E_c I_g \end{cases}$$
 (b) 0.25 $E_c I_g$

There are two options for calculating the flexural stiffness of slender concrete columns EI. The first equation provides accurate representation of the reinforcement in the section and will be used in this example and is also used by the solver in spColumn. Further comparison of the available options is provided in "Effective Flexural Stiffness for Critical Buckling Load of Concrete Columns" technical note.

$$I_{column} = \frac{c^4}{12} = \frac{500^4}{12} = 5.21 \times 10^9 \text{ mm}^4$$

$$E_c = \left(3,300 \times \sqrt{f_c} + 6,900\right) \left(\frac{\gamma_c}{2,300}\right)^{1.5}$$

$$CSA A.23.3-94 (Eq. 8-6)$$



$$E_c = (3,300 \times \sqrt{25} + 6,900) \left(\frac{2,400}{2,300}\right)^{1.5} = 24,942.2 \text{ MPa}$$

 β_d in sway frames, is the ratio of maximum factored sustained shear within a story to the maximum factored shear in that story associated with the same load combination. The maximum factored sustained shear in this example is equal to zero leading to $\beta_d = 0$. **CSA A.23.3-94 (10.0)**

For exterior columns with one beam framing into them in the direction of analysis (14 columns):

With 12 - 25M reinforcement equally distributed on all sides $I_{st} = 1.62 \times 10^8$ mm⁴

$$EI = \frac{0.2E_c I_g + E_s I_{st}}{1 + \beta_d}$$

$$EI = \frac{0.2 \times 24,942.2 \times (5.21 \times 10^9) + 200,000 \times (1.62 \times 10^8)}{1 + 0} = 5.85 \times 10^{13} \text{ N.mm}^2$$

k = 1.51 (calculated previously).

$$P_{c1} = \frac{\pi^2 \times 5.85 \times 10^{13}}{(1.51 \times 4,750)^2} = 1.12 \times 10^7 \text{ N} = 11,213.9 \text{ kN}$$

For exterior columns with two beams framing into them in the direction of analysis (4 columns):

$$\Psi_{A} = \frac{\left(\sum \frac{EI}{l_{c}}\right)_{columns}}{\left(\sum \frac{EI}{l}\right)_{beams}} = \frac{1.65 + 2.6}{1.45 + 1.53} = 1.42$$
CSA A.23.3-94 (Figure N.10.15.1)

 $\Psi_{B} = 1$ (Column considered fixed at the base)

CSA A.23.3-94 (Figure N.10.15.1)

Using Figure N10.15.1 from CSA A23.3-94 $\rightarrow k = 1.38$ as shown in the figure below for the exterior columns with two beams framing into them in the directions of analysis.







Figure 3 – Effective Length Factor (k) for Exterior Columns with Two Beams Framing into them in the Direction of Analysis

$$P_{c2} = \frac{\pi^2 \times 5.85 \times 10^{13}}{(1.38 \times 4,750)^2} = 1.34 \times 10^7 \text{ N} = 13,426.2 \text{ kN}$$

For interior columns (10 columns):

$$\Psi_{A} = \frac{\left(\sum \frac{EI}{l_{c}}\right)_{columns}}{\left(\sum \frac{EI}{l}\right)_{beams}} = \frac{1.65 + 2.6}{1.45 + 1.53} = 1.42$$

 $\Psi_{B} = 1.0$ (Column essentially fixed at base)

<u>CSA A.23.3-94 (Figure N.10.15.1)</u>

CSA A.23.3-94 (Figure N.10.15.1)

Using Figure N10.15.1 from CSA A23.3-94 $\rightarrow k = 1.38$ as shown in the figure below for the interior columns.







Figure 4 – Effective Length Factor (k) Calculations for Interior Columns

With 12 - 25M reinforcement equally distributed on all sides $I_{st} = 1.62 \times 10^8$ mm⁴

$$EI = \frac{0.2E_c I_s + E_s I_{st}}{1 + \beta_d}$$

$$EI = \frac{0.2 \times 24,942.2 \times (5.21 \times 10^3) + 200,000 \times (1.62 \times 10^8)}{1 + 0} = 5.85 \times 10^{13} \text{ N.mm}^2$$

$$P_{c2} = \frac{\pi^2 \times 5.85 \times 10^{13}}{(1.38 \times 4,750)^2} = 1.34 \times 10^7 \text{ N} = 13,426.2 \text{ kN}$$

$$\Sigma P_c = n_1 \times P_{c1} + n_2 \times P_{c2} + n_3 \times P_{c3}$$

$$\Sigma P_c = 10 \times 13,426.2 + 4 \times 13,426.2 + 14 \times 11,213.9 = 344,960 \text{ kN}$$

$$\Sigma P_f = 72,100 \text{ kN (Table 1)}$$

$$\delta_s = \frac{1}{1 - \frac{\Sigma P_f}{\phi_m \times \Sigma P_c}}$$

$$CSA A23.3-94 (Eq. 10-18)$$

$$CSA A23.3-94 (Eq. 10-23)$$



$\delta_s M_{T_{op,s}} = 1.39 \times 94.7 = 131.25 \text{ kN.m}$	
$M_{Top_2^{nd}} = M_{Top,ns} + \delta_s M_{Top,s} = 205 + 131.3 = 336.3 \text{ kN.m}$	<u>CSA A.23.3-94 (10.16.2)</u>
$\delta_s M_{Bottom,s} = 1.39 \times 224 = 310.5 \text{ kN.m}$	
$\delta_s M_{Bottom,s} = 1.39 \times 110.6 = 153.3 \text{ kN.m}$	
$M_{Bottom_2^{nd}} = M_{Bottom,ns} + \delta_s M_{Bottom,s} = 224 + 153.3 = 377.3 \text{ kN.m}$	<u>CSA A.23.3-94 (10.16.2)</u>
$M_{2_2^{nd}} = max \left(M_{Top_2^{nd}}, M_{Bottom_2^{nd}} \right) = M_{Bottom_2^{nd}} = 377.3 \text{ kN.m} \rightarrow M_{2_1^{st}} = M_{Bottom_1^{st}}$, = 334.6
$M_{2_2^{nd}} = max \left(M_{Top_2^{nd}}, M_{Bottom_2^{nd}} \right) = M_{Bottom_2^{nd}} = 377.3 \text{ kN.m} \rightarrow M_{2_1^{nd}} = M_{Bottom_1^{nd}}$, = 334.6 kN.m
$M_{1_2^{nd}} = min(M_{Top_2^{nd}}, M_{Bottom_2^{nd}}) = M_{Top_2^{nd}} = 336.3 \text{ kN.m} \rightarrow M_{1_1^{st}} = M_{Top_1^{st}} = 2$	999.7 kN.m
$P_f = 2,400 \text{ kN}$	

A summary of the moment magnification factors and magnified moments for the exterior column for all load combinations using both equation options CSA A23.3 (Eq. 10-23) and (Eq. 10-24) to calculate δ_s is provided in the table below for illustration and comparison purposes. Note: The designation of M_1 and M_2 is made based on the second-order (magnified) moments and not based on the first-order (unmagnified) moments.

	Table 4 - Factored Axial loa	ds and Ma	gnified M	loments at	the Ends of	Exterior	Column		
		Axial Load	Usin	g CSA Eq.	.10-24	Using CSA Eq.10-23			
No.	Load Combination	kN	δ_{s}	M ₁ , kN.m	M2, kN.m	δ_{s}	M ₁ , kN.m	M ₂ , kN.m	
1	1.25D	2,019	*	*	*		134	148	
2	1.25D + 1.5L	2,563		235	257		235	257	
3	1.25D + 1.5W	2,019	*	*	*	1.30	309.9	352.7	
4	1.25D - 1.5W	2,019	*	*	*	1.30	-41.5	-57.7	
5	1.25D + 1.05L + 1.05W	2,400	1.11	310	346	1.39	336.3	377.3	
6	1.25D + 1.05L - 1.05W	2,400	*	*	*	1.39	70.7	73.7	
7	0.85D + 1.5W	1,373	*	*	*	1.24	259.5	296.7	
8	0.85D - 1.5W	1,373	*	*	*	1.24	-76.9	-96.1	
* Not cov	vered by the reference								



CSA A23.3-94 (10.15.3)

5. Moment Magnification along Length of Compression Member

In sway frames, if an individual compression member has:

$$\frac{l_u}{r} > \frac{35}{\sqrt{P_f / (f_c A_g)}}$$
CSA A23.3-94 (Eq. 10-25)

It shall be designed for the factored axial load, P_f and moment, M_c , computed using Clause 10.15.3 (Nonsway frame procedure), in which M_1 and M_2 are computed in accordance with Clause 10.16.2. *CSA A23.3-94 (10.16.4)*

$$M_{c} = \frac{C_{m}M_{2}}{1 - \frac{P_{f}}{\phi_{m}P_{c}}} \ge M_{2}$$
CSA A23.3-94 (10.15.3)

Where:

$$C_m = 0.6 + 0.4 \frac{M_1}{M_2} \ge 0.4$$

CSA A23.3-94 (10.15.3.1)

 M_2 = the second-order factored moment (magnified sway moment)

And, the member resistance factor would be $\phi_m = 0.75$

$$P_{c} = \frac{\pi^{2} EI}{\left(kl_{u}\right)^{2}}$$
CSA A23.3-94 (Eq. 10-17)

Where:

$$EI = \begin{cases} (a) \frac{0.2E_c I_g + E_s I_{st}}{1 + \beta_d} \\ (b) \ 0.25 \ E_c I_g \end{cases}$$
 (b) 0.25 $E_c I_g$

There are two options for calculating the effective flexural stiffness of slender concrete columns *EI*. The first equation provides accurate representation of the reinforcement in the section and will be used in this example and is also used by the solver in <u>spColumn</u>. Further comparison of the available options is provided in "<u>Effective Flexural</u> <u>Stiffness for Critical Buckling Load of Concrete Columns</u>" technical note.

5.1. Gravity Load Combination #2 (Gravity Loads Only)

$$r = \sqrt{\frac{I_g}{A_g}} = \sqrt{\frac{500^4 / 12}{500^2}} = 144.34 \text{ mm}$$

$$\frac{CSA A23.3-94 (10.14.4)}{r}$$

$$\frac{l_u}{r} = \frac{4750}{144.34} = 32.91$$

$$\frac{35}{\sqrt{P_f} / (f_c A_g)} = \frac{35}{\sqrt{\frac{2,564 \times 1,000}{25 \times 2.5 \times 10^5}}} = 54.63$$

$$\frac{CSA A23.3-94 (Eq. 10-25)}{\sqrt{\frac{2}{25 \times 2.5 \times 10^5}}}$$



Since 32.94 < 54.63, calculating the moments along the column length is not required.

Check minimum moment:

CSA A23.3-94 (10.15.3)

CSA A23.3-94 does not require to design columns in sway frames for a minimum moment. However, the reference decided conservatively to design the column for the larger of computed moments and the minimum value of $C_m M_2$.

$$(C_m M_2)_{\min} = P_f (15 + 0.03h)$$

 $(C_m M_2)_{\min} = 2,563 \times (15 + 0.03 \times 500) / 1,000 = 76.9 \text{ kN.m}$

5.2. Load Combination #5 (Gravity Plus Wind Loads)

$$\frac{35}{\sqrt{P_f / (f_c A_g)}} = \frac{35}{\sqrt{\frac{2,400 \times 1,000}{25 \times 2.5 \times 10^5}}} = 56.48$$
CSA A23.3-94 (Eq. 10-25)

Since 32.94 < 56.48, calculating the moments along the column length is not required.

Check minimum moment:

CSA A23.3-94 (10.15.3)

$$(C_m M_2)_{\min} = P_f (15 + 0.03h)$$

 $(C_m M_2)_{\min} = 2,400 \times (15 + 0.03 \times 500) / 1,000 = 72 \text{ kN.m}$

 M_{c1} and M_{c2} will be considered separately to ensure proper comparison of resulting magnified moments against negative and positive moment capacities of unsymmetrical sections as can be seen in the following figure.



Figure 5 - Column Interaction Diagram for Unsymmetrical Section

A summary of the moment magnification factors and magnified moments for the exterior column for all load combinations using both equation options CSA A23.3 (Eq. 10-23) and (Eq. 10-24) to calculate δ_s is provided in the table below for illustration and comparison purposes.

	Table 5 - Factored A	Axial loads and M	Magr	nified Momen	ts along Exter	ior (Column Lengt	h	
No.	Load Combination	Axial Load,		Using CSA E	Eq. 10-24		Using CSA Eq. 10-23		
NO.	Load Combination	kN	δ	M _{c1} , kN.m	M _{c2} , kN.m	δ	M _{c1} , kN.m	M _{c2} , kN.m	
1	1.25D	2,019	*	*	*	1	134	14	
2	1.25D + 1.5L	2,563	1	235	257	1	235	25	
3	1.25D + 1.5W	2,019	*	*	*	1	309.9	352	
4	1.25D - 1.5W	2,019	*	*	*	1	-41.5	-57	
5	1.25D + 1.05L + 1.05W	2,400	1	310	346	1	336.3	377	
6	1.25D + 1.05L - 1.05W	2,400	*	*	*	1	73.7	70	
7	0.85D + 1.5W	1,373	*	*	*	1	259.5	296	
8	0.85D – 1.5W	1,373	*	*	*	1	-76.9	-96	

For column design, CSA A23.3 requires that δ_s to be computed from Clause 10.16.3.2 using $\sum P_f$ and $\sum P_c$ corresponding to 1.25 dead load and 1.5 live load shall be positive and shall not exceed 2.5. β_d shall be taken as the ratio of the factored sustained axial dead load to the total axial load. For values of δ_s above the limit, the frame would be very susceptible to variations in EI, foundation rotations and the like. If this value is exceeded, the frame must be stiffened to reduce δ_s .

$\beta_{d} = \frac{\text{Total factored sustained axial load}}{\text{Total factored axial load}}$

$$\beta_d = \frac{59,500}{77,500} = 0.768$$

$$P_c = \frac{\pi^2 \text{EI}}{(\text{kl}_u)^2}$$

Where:

$$EI = \frac{0.2E_c I_g + E_s I_{st}}{1 + \beta_d}$$

$$EI = \frac{0.2 \times 24,942.2 \times (5.21 \times 10^9) + 200,000 \times (1.62 \times 10^8)}{1 + 0.768} = 3.31 \times 10^{13} \text{ N.mm}^2$$

For exterior columns with two beams framing into them in the direction of analysis:

$$P_c = \frac{\pi^2 \times 3.31 \times 10^{13}}{(1.51 \times 4,750)^2} = 6,343.62 \text{ kN}$$

For interior columns and exterior columns with two beams framing into them in the direction of analysis:

$$P_c = \frac{\pi^2 \times 3.31 \times 10^{13}}{(1.38 \times 4,750)^2} = 7,595.09 \text{ kN}$$
$$\Sigma P_c = (10+4) \times 7,595.09 + 14 \times 6,343.62 = 195,142 \text{ kN}$$

CSA A23.3-94 (10.16.5)

CSA A23.3-94 (Eq. 10-17)





Where the member resistance factor is $\phi_m = 0.75$

CSA A23.3-94 (10.15.3)

CSA A23.3-94 (Eq. 10-23)

$$\delta_s = \frac{1}{1 - \frac{\Sigma P_f}{\phi_m \times \Sigma P_c}}$$
$$\delta_s = \frac{1}{77.500} = 2.13 < 2.5$$

$$1 - \frac{77,500}{0.75 \times 195,142}$$

Thus, the frame is stable.

6. Column Design

Based on the factored axial loads and magnified moments considering slenderness effects, the capacity of the assumed column section (500 mm \times 500 mm with 12 – 25M bars distributed all sides equal) will be checked and confirmed to finalize the design. A column interaction diagram will be generated using strain compatibility analysis, the detailed procedure to develop column interaction diagram can be found in "Interaction Diagram - Tied Reinforced Concrete Column" example.

The factored axial load resistance P_r for all load combinations will be set equals to P_f , then the factored moment resistance M_r associated to P_r will be compared with the magnified applied moment M_f . The design check for load combination #5 is shown below for illustration. The rest of the checks for the other load combinations are shown in the following Table.





The following procedure is used to determine the nominal moment capacity by setting the factored axial load resistance, P_r , equal to the factored axial load, P_f and iterating on the location of the neutral axis.

6.1. c, a, and strains in the reinforcement

Try
$$c = 335 \text{ mm}$$

Where c is the distance from extreme compression fiber to the neutral axis. **CSA A.23.3-94 (10.0)**

$$a = \beta_1 \times c = 0.908 \times 335 = 304 \text{ mm}$$

<u>CSA A.23.3-94 (10.1.7a)</u>

Where:



$$\begin{aligned} \beta_1 &= 0.97 - 0.0025 f_c^{-1} = 0.908 \ge 0.67 \\ \hline CSA \ A.23.3 - 94 \ (Eq. \ 10 - 2) \\ \hline \varepsilon_{cu} &= 0.0035 \\ \hline \varepsilon_y &= \frac{f_y}{E_s} = \frac{400}{200,000} = 0.002 \\ \hline \varepsilon_y &= \frac{f_y}{E_s} = \frac{400}{200,000} = 0.002 \\ \hline \varepsilon_s &= (d_1 - c) \times \frac{0.0035}{c} = (446 - 335) \times \frac{0.0035}{335} = 0.00116 \ (\text{Tension}) < \varepsilon_y \\ \therefore \text{ tension reinforcement has not yielded} \\ \phi_c &= 0.60 \\ \hline \phi_s &= 0.85 \\ \hline \varepsilon_{s4}^{-1} &= (c - d_4) \times \frac{0.0035}{c} = (335 - 54) \times \frac{0.0035}{335} = 0.00294 \ (\text{Compression}) > \varepsilon_y \\ \hline \varepsilon_{s3}^{-1} &= (c - d_3) \times \frac{0.0035}{c} = (335 - 185) \times \frac{0.0035}{335} = 0.00157 \ (\text{Compression}) < \varepsilon_y \\ \hline \varepsilon_{s2}^{-1} &= (c - d_2) \times \frac{0.0035}{c} = (335 - 315) \times \frac{0.0035}{335} = 0.00021 \ (\text{Compression}) < \varepsilon_y \end{aligned}$$

6.2. Forces in the concrete and steel

$$C_{rc} = \alpha_1 \times \phi_c \times f_c \times a \times b = 0.812 \times 0.6 \times 25 \times 304 \times 500 = 1,852.6 \text{ kN}$$
CSA A.23.3-94 (10.1.7a)

Where:

$$\alpha_{1} = 0.85 - 0.0015 f_{c}^{'} = 0.812 \ge 0.67$$

$$f_{s} = \varepsilon_{s} \times E_{s} = 0.00116 \times 200,000 = 231.94 \text{ MPa}$$

$$T_{rs} = \phi_{s} \times f_{s} \times A_{s1} = 0.85 \times 231.94 \times (4 \times 500) = 394 \text{ kN}$$
Since $\varepsilon_{s4}^{'} > \varepsilon_{y} \rightarrow$ compression reinforcement has yielded

$$\therefore f_{s4} = f_v = 400 \text{ MPa}$$

Since $\varepsilon_{s_3} < \varepsilon_y \rightarrow$ compression reinforcement has not yielded

 $\therefore f_{s3} = \varepsilon_{s3} \times E_s = 0.00157 \times 200,000 = 313$ MPa

Since $\dot{\varepsilon_{s2}} < \varepsilon_y \rightarrow$ compression reinforcement has not yielded



 $\therefore f_{s2} = \varepsilon_{s2} \times E_s = 0.00021 \times 200,000 = 42$ MPa

The area of the reinforcement in third and fourth layers has been included in the area (*ab*) used to compute C_{rc} . As a result, it is necessary to subtract $\alpha_1 f_c$ ' from f_s ' before computing C_{rs} :

$$C_{rs4} = (\phi_s f_{s4}^{'} - \alpha_1 \phi_c f_c^{'}) \times A_{s4}^{'} = (0.85 \times 400 - 0.812 \times 0.6 \times 25) \times (4 \times 500) / 1,000 = 655.6 \text{ kN}$$

$$C_{rs3} = (\phi_s f_{s3}^{'} - \alpha_1 \phi_c f_c^{'}) \times A_{s3}^{'} = (0.85 \times 313 - 0.812 \times 0.6 \times 25) \times (2 \times 500) / 1,000 = 254.2 \text{ kN}$$

$$C_{rs2} = (\phi_s f_{s2}^{'}) \times A_{s2}^{'} = (0.85 \times 42) \times (2 \times 500) / 1,000 = 35.52 \text{ kN}$$

6.3. P_r and M_r

$$P_r = C_{rc} + C_{rs2} + C_{rs3} + C_{rs4} - T_{rs} = 1,852.6 + 35.52 + 254.2 + 655.6 - 394.3 = 2,403.66 \text{ kN}$$
$$P_r = 2,403.66 \text{ kN} \approx 2,400 \text{ kN} = P_f$$

The assumed value of c = 335 mm is correct.

$$M_{r} = C_{rc} \times \left(\frac{h}{2} - \frac{a}{2}\right) + C_{rs4} \times \left(\frac{h}{2} - d_{4}\right) + C_{rs3} \times \left(\frac{h}{2} - d_{3}\right) - C_{rs2} \times \left(d_{2} - \frac{h}{2}\right) + T_{rs} \times \left(d_{1} - \frac{h}{2}\right)$$
$$M_{r} = 1,852.6 \times \left(\frac{500}{2} - \frac{304}{2}\right) + 655.6 \times \left(\frac{500}{2} - 54\right) + 254.2 \times \left(\frac{500}{2} - 185\right) - 35.52 \times \left(315 - \frac{500}{2}\right) + 394 \times \left(446 - \frac{500}{2}\right)$$

	Table 6 – Exterior Column Axial and Moment Capacities								
No.	P _f , kN	$\begin{array}{c} M_u = M_{2(2nd)},\\ kN.m \end{array}$	c, mm	$\varepsilon_t = \varepsilon_s$	P _r , kN	M _r , kN.m			
1	2,019	148	307	0.00158	2,023.3	437.6			
2	2,563	257	349	0.00097	2,568.1	390.5			
3	2,019	352.7	307	0.00158	2,023.3	437.6			
4	2,019	-57.7	307	0.00158	2,023.3	437.6			
5	2,400	377.3	335	0.00116	2,403.7	402			
6	2,400	70.7	335	0.00116	2,403.7	402			
7	1,373	296.7	253	0.00267	1,376.7	470			
8	1,373	-96.1	253	0.00267	1,376.7	470			

 $M_r = 401,541$ N.m = 401.54 kN.m > $M_f = 337.3$ kN.m

Since $M_r > M_f$ for all $P_r = P_f$, use 500×500 mm column with 12 - 25 M bars.



7. Column Interaction Diagram - spColumn Software

<u>spColumn</u> program performs the analysis of the reinforced concrete section conforming to the provisions of the Strength Design Method and Unified Design Provisions with all conditions of strength satisfying the applicable conditions of equilibrium and strain compatibility and includes slenderness effects using moment magnification method for sway and nonsway frames. For this column section, we ran in investigation mode with control points using the CSA A23.3-94. In lieu of using program shortcuts, spSection (Figure 7) was used to place the reinforcement and define the cover to illustrate handling of irregular shapes and unusual bar arrangement.



Figure 7 – spColumn Model Editor (spSection)



Figure 8 -spColumn Model Input Wizard Windows

spcolumn







Figure 5 - Column Section Interaction Diagram about X-Axis - Design Check for Load Combination 5 (spColumn)







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1. General Information

File Name	C:\TSDA\Slenderness\CSA \1.25D+1.05L+1.05W.col
Project	MacGreger
Column	Exterior
Engineer	SP
Code	CSA A23.3-94
Bar Set	CSA G30.18
Units	Metric
Run Option	Investigation
Run Axis	X - axis
Slenderness	Considered
Column Type	Structural

2. Material Properties

2.1. Concrete

Туре	Standard
f'c	25 MPa
E _c	24942.4 MPa
f _c	20.3125 MPa
ε _u	0.0035 mm/mm
β1	0.9075

2.2. Steel

Туре	Standard	
f _y	400	MPa
E₅	200000	MPa
ε _{yt}	0.002	mm/mm

3. Section

3.1. Shape and Properties

Туре	Rectangular	
Width	500	mm
Depth	500	mm
Ag	250000	mm ²
I _x	5.20833e+009	mm ⁴
l _y	5.20833e+009	mm ⁴
۲ _x	144.338	mm
r _y	144.338	mm
r _y X _o Y _o	0	mm
Yo	0	mm



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3.2. Section Figure



Figure 1: Column section

4. Reinforcement

4.1. Bar Set: CSA G30.18

Bar	Diameter	Area	Bar	Diameter	Area	Bar	Diameter	Area
	mm	mm ²		mm	mm ²		mm	mm ²
#10	11.30	100.00	#15	16.00	200.00	#20	19.50	300.00
#25	25.20	500.00	#30	29.90	700.00	#35	35.70	1000.00
#45	43.70	1500.00	#55	56.40	2500.00			

4.2. Confinement and Factors

Confinement type	Tied
For #55 bars or less	#10 ties
For larger bars	#15 ties
Material Resistance Factors	
Axial compression, (a)	0.8
Steel (∮₅)	0.85
Concrete (¢c)	0.6

4.3. Arrangement

Pattern	All sides equal		
Bar layout	Rectangular		
Cover to	Transverse bars		
Clear cover	30 mm		
Bars	12 #25		





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Total steel area, As	6000	mm ²
Rho	2.40	%
Minimum clear spacing	106	mm

5. Loading 5.1. Load Combinations

Combination	Dead	Live	Wind	EQ	Snow
U1	1.250	1.050	1.050	0.000	0.000

5.2. Service Loads

No.	Load Case	Axial Load	Мх @ Тор	Mx @ Bottom	Му @ Тор	My @ Bottom
		kN	kNm	kNm	kNm	kNm
1	Dead	1615.20	107.36	118.00	0.00	0.00
1	Live	362.86	67.43	72.86	0.00	0.00
1	Wind	0.00	90.19	105.33	0.00	0.00
1	EQ	0.00	0.00	0.00	0.00	0.00
1	Snow	0.00	0.00	0.00	0.00	0.00

5.3. Sustained Load Factors

Load Case	Factor
	%
Dead	100
Live	0
Wind	0
EQ	0
Snow	0

6. Slenderness

6.1. Sway Criteria

X-Axis	Sway column
ΣPc	30.76 x P _c
ΣPu	30.04 x P _u

6.2. Columns

Column	Axis	Height	Width	Depth	I	f'c	Ec
		m	mm	mm	mm⁴	MPa	MPa
Design	Х	4.75	500	500	5.20833e+009	25	24942.4
Above	Х	(no column specified)					
Below	Х	(no column specified)					

6.3. X - Beams

Beam	Length	Width	Depth	I.	f'c	Ec
	m	mm	mm	mm⁴	MPa	MPa
Above Left	(no beam specified)					
Above Right	(no beam specified)					
Below Left	(no beam specified)					
Below Right	(no beam specified)					

7. Moment Magnification

7.1. General Parameters

Factors

Code defaults



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Stiffness reduction factor, ϕ_K	0.75
Cracked section coefficients, cl(beams)	0.35
Cracked section coefficients, cl(columns)	0.7
$0.2 E_c I_g + E_s I_{se}$ (X-axis)	5.85e+010 kNmm ²
Minimum eccentricity, e _{x min}	30.00 mm
k'	(P _f / (f' _c *A _g)) ^{0.5}

7.2. Effective Length Factors

Axis	Ψ_{top}	Ψ_{bottom}	k (Nonsway)	k (Sway)	kl _u /r
Х	0.000	0.000	1.000	1.5 <mark>1</mark> 0	49.69

7.3. Magnification Factors: X - axis

Load		At	Ends			Α	long Leng	jth			
Combo	∑P _f	Pc	∑P₀	β _{ds}	ō₅	Pf	k'l _u /r	Pc	β_{dns}	Cm	δ
	kN	kN	kN			kN		kN			
1 U1	72100.89	11214.50	344980.50	0.000	1.386	2400.00	20.39	(N/A)	(N/A)	(N/A)	(N/A)

8. Factored Moments

NOTE: Each loading combination includes the following cases: Top - At column top Bot - At column bottom

8.1. X - axis

Load					2 nd Order			Ratio		
Comb	0		M _{ns}	Ms	Mf	M _{min}		Mi	Mc	2 nd /1 st
			kNm	kNm	kNm	kNm		kNm	kNm	
1	U1	Тор	205.00	94.70	299.70	(N/A)	M ₁ =	336.29	(N/A)	(N/A)
1	U1	Bot	-224.00	-110.60	-334.60	(N/A)	M ₂ =	-377.33	(N/A)	(N/A)

9. Factored Loads and Moments with Corresponding Capacity Ratios

NOTE: Capacity Ratios are based on "Moment Capacity" method. Each loading combination includes the following cases: Ton - At column ton

Top - At column top Bot - At column bottom

N	No. Load				Demand			Capacity			
	C	Comb	0		Pf	Mfx	Pr	Mrx	NA Depth	εt	Ratio
					kN	kNm	kN	kNm	mm		
	1	1	U1	Тор	2400.00	336.29	2400.00	402.21	335	0.00116	0.84
	2	1	U1	Bot	2400.00	-377.33	2400.00	-402.21	335	0.00116	0.94





8. Summary and Comparison of Design Results

Analysis and design results from the hand calculations above are compared for the one load combination used in the reference (Example 12-3,4 and 5) and exact values obtained from spColumn model.

	Table 7 – Parameters for Moment Magnification at Column Ends												
	Q	k	EI, N.mm ²	P _c , kN	M _{1(2nd)} , kN.m	M _{2(2nd)} , kN.m							
Hand	0.0.97	1.51*	5.85×10 ¹³ ‡	11,214	336.3	377.3							
Reference	0.0.97	1.43†	5.31×10 ^{13†}	11,360	330.0	370.0							
spColumn		1.51*	5.85×10 ^{13‡}	11,214	336.3	377.3							
	* From nomographs (CSA A23.3 charts) [†] Conservatively estimated not using exact formulae without major impact on the final results in this special case												

In this table, a detailed comparison for all considered load combinations are presented for comparison.

	Table 8 - Factored Axial loads and Magnified Moments at Column Ends														
No.	P _f ,	kN	δ	δs	M _{1(2nd)} ,	kN.m	M _{2(2nd)} , kN.m								
INO.	Hand	spColumn	Hand	spColumn	Hand	spColumn	Hand	spColumn							
1	2,019	2,019.0	N/A	N/A	134.2	134.2	147.5	147.5							
2	2,563	2,563.3	N/A	N/A	235.3	235.3	256.8	256.8							
3	2,019	2,019.0	1.30	1.30	309.9	309.9	352.7	352.6							
4	2,019	2,019.0	1.30	1.30	-41.5	-41.5	-57.7	-57.6							
5	2,400	2,400.0	1.39	1.39	336.3	336.3	377.3	377.3							
6	2,400	2,400.0	1.39	1.39	73.7	73.7	70.7	70.7							
7	1,373	1,372.9	1.24	1.24	259.4	259.4	296.7	296.7							
8	1,373	1,372.9	1.24	1.24	-76.9	-76.9	-96.1	-96.1							





	Table 9 - Design Parameters Comparison													
No.		c, mm		$\varepsilon_t = \varepsilon_s$	P _f , k	N	M _r , 1	M _r , kN.m						
INO.	Hand	spColumn	Hand	spColumn	Hand	spColumn	Hand	spColumn						
1	307	307	0.00158	0.00159	2,023.3	2,019.0	437.6	438.4						
2	349	349	0.00097	0.00098	2,568.1	2,563.6	390.5	385.4						
3	307	307	0.00158	0.00159	2,023.3	2,019.0	437.6	438.4						
4	307	307	0.00158	0.00159	2,023.3	2,019.0	437.6	438.4						
5	335	335	0.00116	0.00116	2,403.7	2,400.0	401.5	402.2						
6	335	335	0.00116	0.00116	2,403.7	2,400.0	401.5	402.2						
7	253	253	0.00268	0.00268	1,376.7	1,373.0	470.0	470.4						
8	253	253	0.00268	0.00268	1,376.7	1,373.0	470.0	470.4						

All the results of the hand calculations illustrated above are in precise agreement with the automated exact results obtained from the <u>spColumn</u> program.

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9. Conclusions & Observations

The analysis of the reinforced concrete section performed by <u>spColumn</u> conforms to the provisions of the Strength Design Method and Unified Design Provisions with all conditions of strength satisfying the applicable conditions of equilibrium and strain compatibility and includes slenderness effects using moment magnification method for sway and nonsway frames.

CSA A23-3 provides multiple options for calculating values of *EI* and δ_s leading to variability in the determination of the adequacy of a column section. Engineers must exercise judgment in selecting suitable options to match their design condition as is the case in the reference where the author conservatively made assumptions to simplify and speed the calculation effort. The <u>spColumn</u> program utilizes the exact methods whenever possible and allows user to override the calculated values with direct input based on their engineering judgment wherever it is permissible.

It was concluded in the CSA A23.3-94 that the probability of stability failure increases rapidly when the stability index Q exceeds 0.2 and a more rigid structure may be required to provide stability. <u>CSA A23.3-94 (10.14.6)</u>

If a frame undergoes appreciable lateral deflections under gravity loads, serious consideration should be given to rearranging the frame to make it more symmetrical because with time, creep will amplify these deflections leading to both serviceability and strength problems. One of these limitations is to limit the second-order lateral deflections to first-order lateral deflections to 2.5 (the ratio should not exceed 2.5) for loads applied to the structure with 1.25 dead load and 1.5 live load plus a lateral load applied to each story equal to 0.0005 multiplied by factored gravity load in that story.

The limitation on δ_s is intended to prevent instability under gravity loads alone. For values of δ_s above the limit, the frame would be very susceptible to variations in EI, foundation rotations and the like. If δ_s exceeds 2.5 the frame must be stiffened to reduce δ_s . CSA A23.3-94 (N10.16.5)

Exploring the impact of other code permissible equation options provides the engineer added flexibility in decision making regarding design. In some cases resolving the stability concern may be viable through a frame analysis providing values for V_f and Δ_o to calculate magnification factor δ_s . Creating a complete model with detailed lateral loads and load combinations to account for second order effects may not be warranted for all cases of slender column design nor is it disadvantageous to have a higher margin of safety when it comes to column slenderness and frame stability considerations.