# Observations in Shear Wall Strength in Tall Buildings

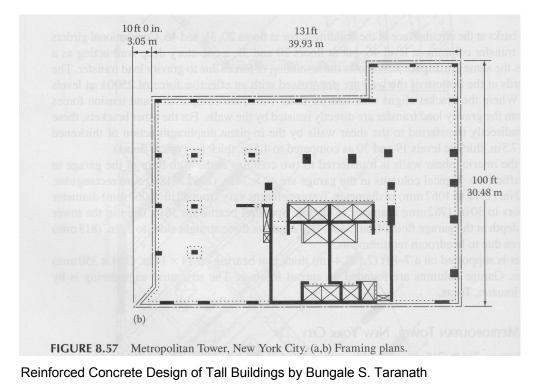


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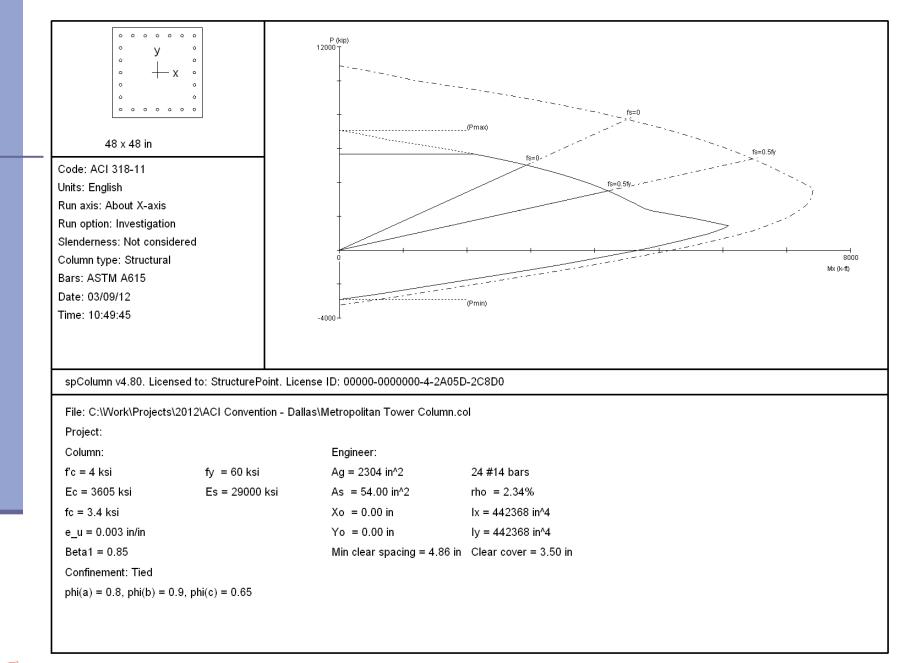
Presented by StructurePoint at ACI Spring 2012 Convention in Dallas, Texas

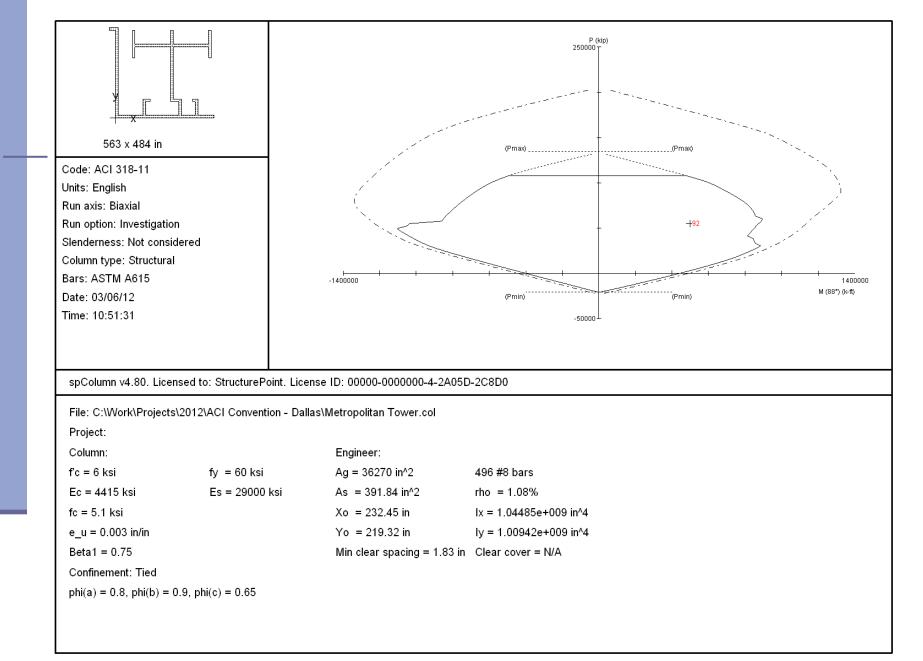
#### Metropolitan Tower, New York City

#### 68-story, 716 ft (218m) skyscraper









# Jin Mao Tower, Shanghai, China

#### 88-story, 1381 ft (421m)

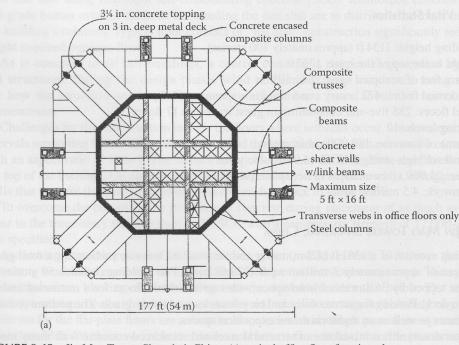
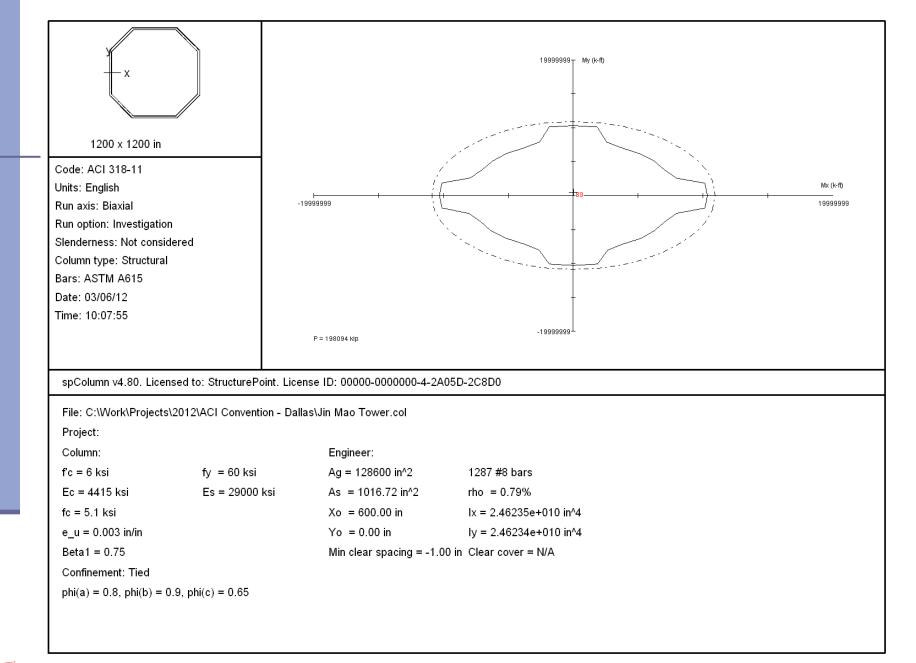
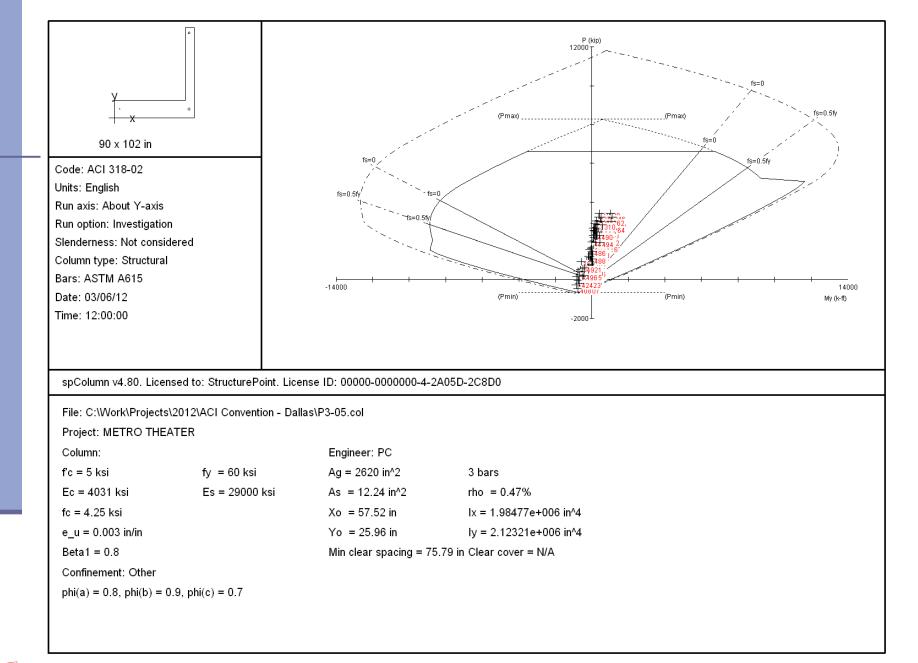


FIGURE 8.45 Jin Mao Tower, Shanghai, China: (a) typical office floor framing plan;









## Motivation

- Sharing insight from detailed analysis and implementation of code provisions
- Sharing insight from members of ACI committees
- Sharing insight from wide base of spColumn users
- Raising awareness of irregularities and their impact on design
- Conclusions apply to all sections, but especially those of irregular shape and loaded with large number of load cases and combinations, e.g. Shear Walls



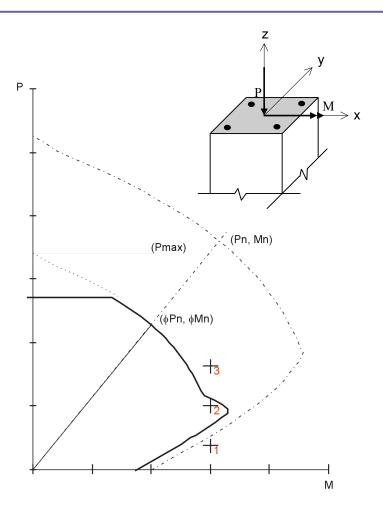
# Outline

#### Observations

- P-M Diagram Irregularities
  - Symmetry/Asymmetry
  - Strength Reduction Factor
  - Uniaxial/Biaxial Bending
- Moment Magnification Irregularities
- Conclusions



## P-M Diagram



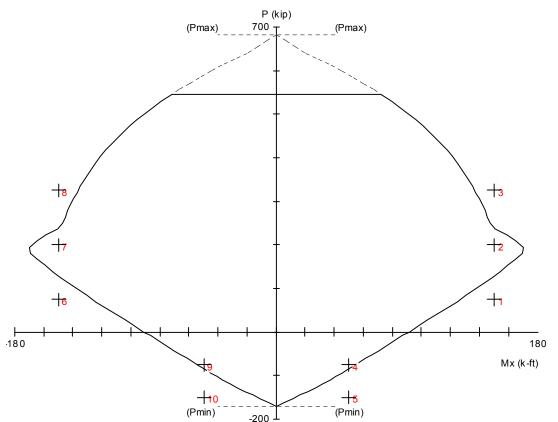
Design

- $(P_{u1}, M_{u1}) \rightarrow NG$
- $(\mathsf{P}_{u2}, \mathsf{M}_{u2}) \rightarrow \mathsf{OK}$
- $(P_{u3}, M_{u3}) \rightarrow NG$
- Notice P<sub>u1</sub> < P<sub>u2</sub> < P<sub>u3</sub> with M<sub>u</sub>=const
- One Quadrant OK if
  - $P_u \ge 0$  and  $M_u \ge 0$
  - Section shape symmetrical
  - Reinforcement symmetrical



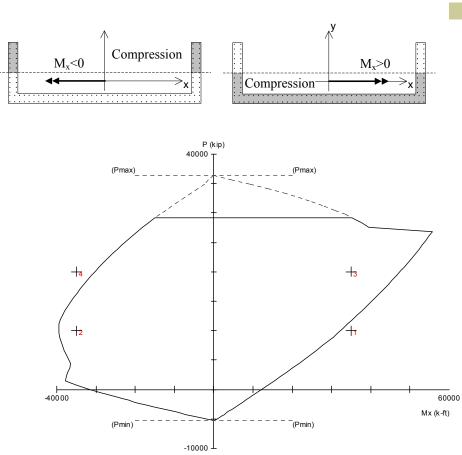
#### P-M Diagram – Pos./Neg. Load Signs

- All four quadrants are needed if loads change sign
  - If section shape and reinforcement are symmetrical then M- side is a mirror of M+ side





#### P-M Diagram – Asymmetric Section



#### Each quadrant different

- $(P_{u1}, M_{u1}) \rightarrow NG$
- $(\mathsf{P}_{\mathsf{u2}}, \mathsf{M}_{\mathsf{u2}}) \to \mathsf{OK}$
- $(\mathsf{P}_{u3}, \mathsf{M}_{u3}) \rightarrow \mathsf{OK}$

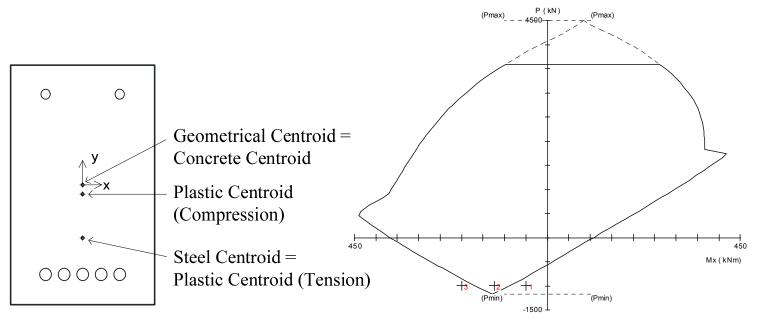
• 
$$(\mathsf{P}_{\mathsf{u4}}, \mathsf{M}_{\mathsf{u4}}) \rightarrow \mathsf{NG}$$

- Notice:
  - Absolute value of moments same on both sides
  - Larger axial force favorable on M+ side but unfavorable on M- side

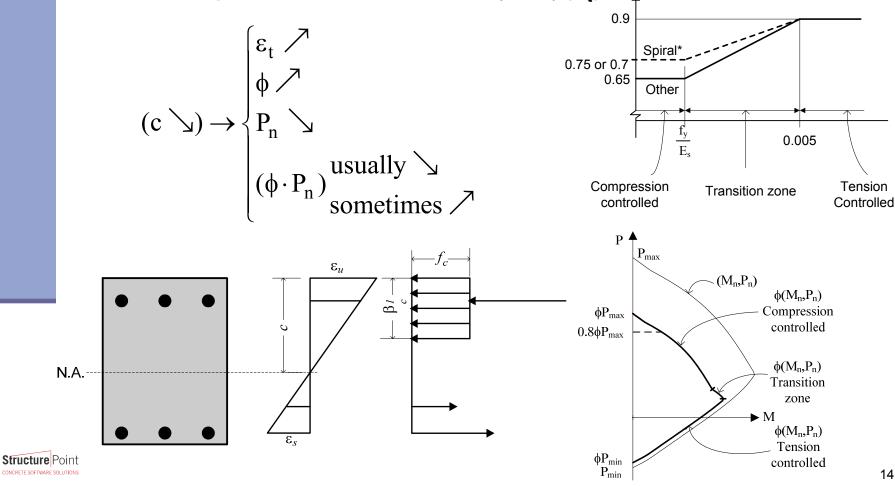
# P-M Diagram – Asymmetric Steel

#### Skewed Diagram

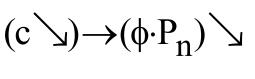
- Plastic Centroid ≠ Geometrical Centroid (Concrete Centroid ≠ Steel Centroid)
- $(P_{u1}, M_{u1}) \rightarrow NG, (P_{u2}, M_{u2}) \rightarrow OK, (P_{u3}, M_{u3}) \rightarrow NG$  $|M_{u1}| < |M_{u2}| < |M_{u3}|$  with  $P_u = const$

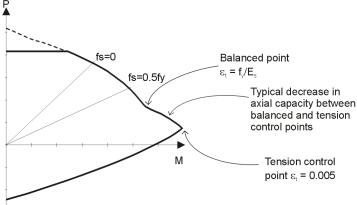


Strength reduction factor  $\phi = \phi(\varepsilon_t) \phi$ 



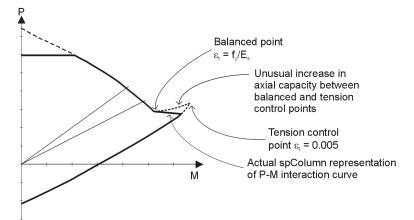
Usually





Sometimes

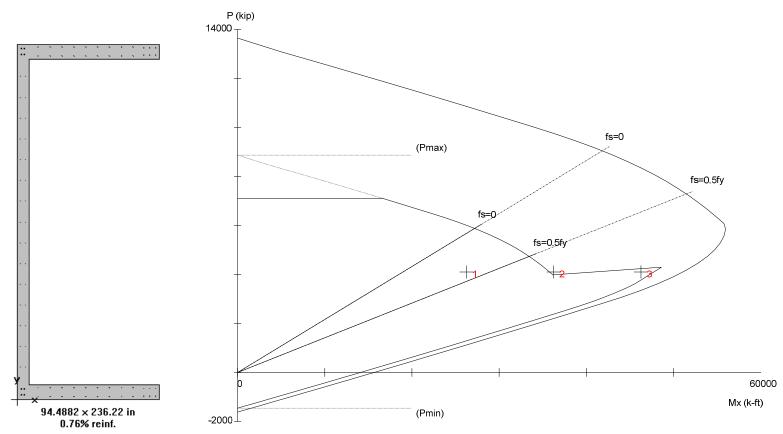
 $(c \searrow) \rightarrow (\phi \cdot P_n) \nearrow$ 



Sections with a narrow portion along height, e.g.: I, L, T, U, Cshaped or irregular sections

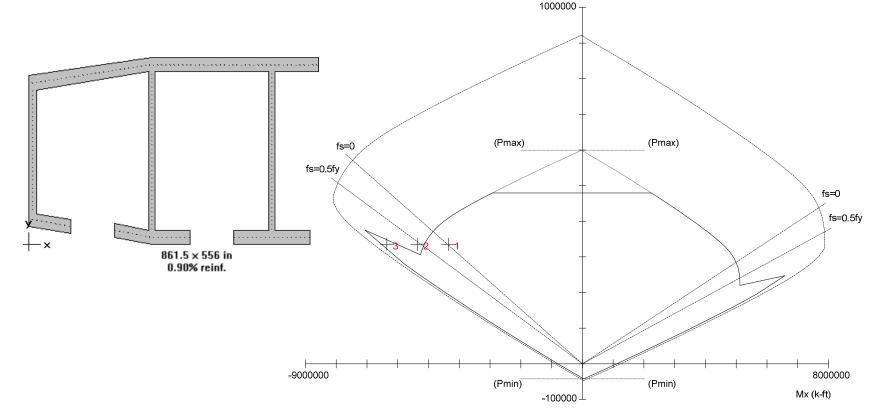


•  $(P_{u1}, M_{u1}) \rightarrow OK, (P_{u2}, M_{u2}) \rightarrow NG, (P_{u3}, M_{u3}) \rightarrow OK$  $M_{u1} < M_{u2} < M_{u3}$  with  $P_u$  = const



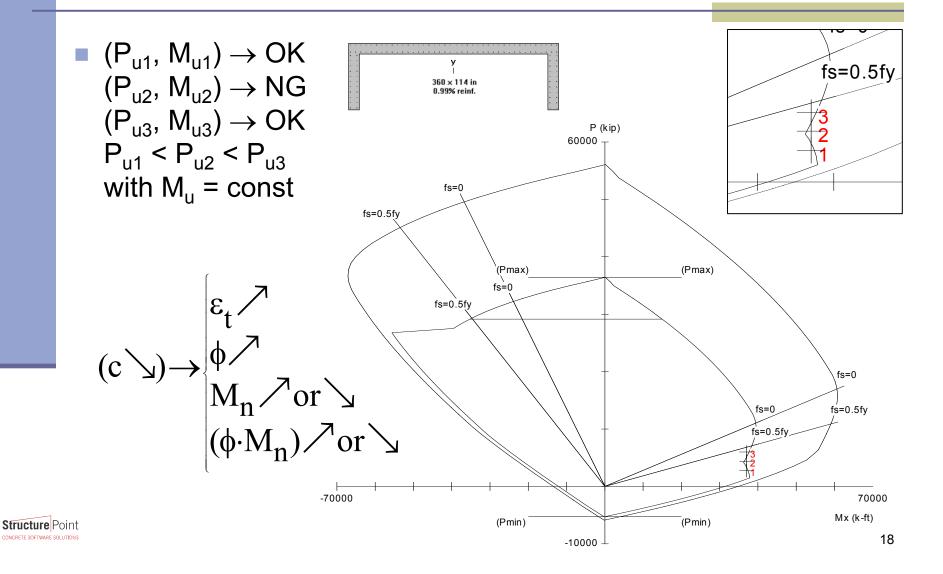


■  $(P_{u1}, M_{u1}) \rightarrow OK, (P_{u2}, M_{u2}) \rightarrow NG, (P_{u3}, M_{u3}) \rightarrow OK$  $|M_{u1}| < |M_{u2}| < |M_{u3}|$  with  $P_u$  = const



P (kip)

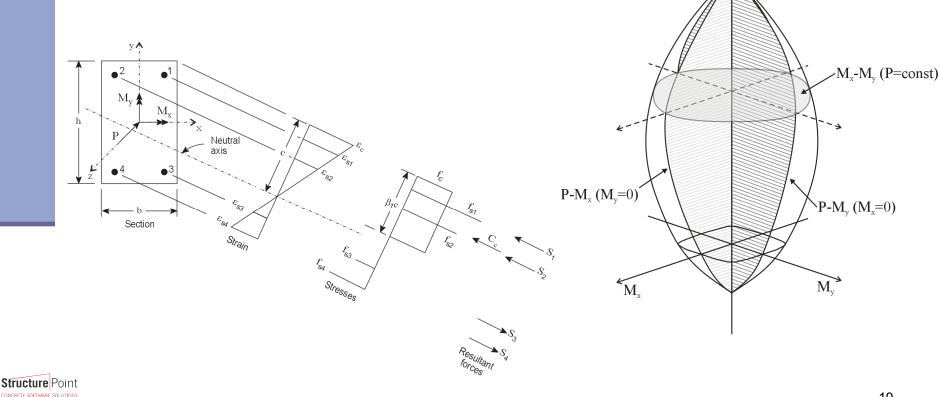




## Uniaxial/Biaxial – Symmetric Case

3D failure surface with tips directly on the P axis

- Uniaxial X = Biaxial P- $M_x$  with  $M_v = 0$
- Uniaxial Y = Biaxial P- $M_v$  with  $M_x = 0$

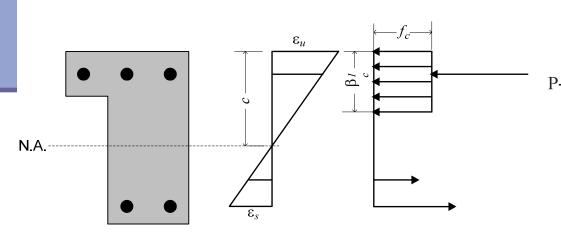


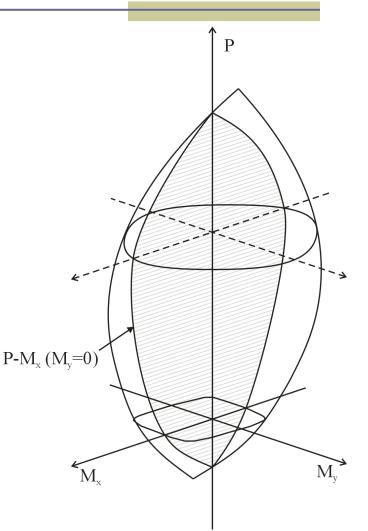
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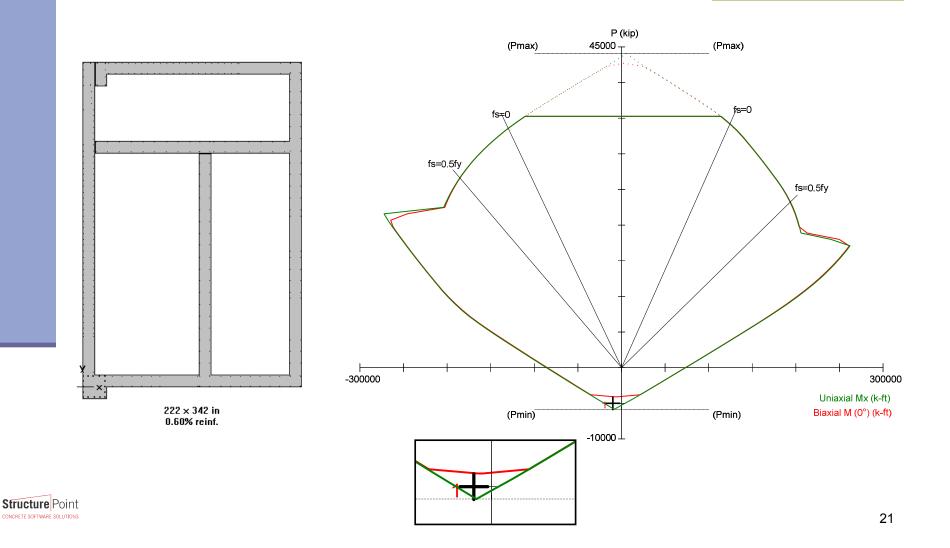
#### Uniaxial/Biaxial – Asymmetric case

- Tips of 3D failure surface may be off the P axis
- Uniaxial X means N.A. parallel to X axis but this produces M<sub>x</sub> ≠ 0 and M<sub>y</sub> ≠ 0
- Uniaxial X may be different than Biaxial P-M<sub>x</sub> with M<sub>y</sub> = 0





#### Uniaxial/Biaxial – Asymmetric Case



#### Moment Magnification – Sway Frames

Magnification at column ends (Sway frames)

$$M_2 = M_{2ns} + \delta_s M_{2s}$$

If sign(M<sub>2ns</sub>) = -sign(M<sub>2s</sub>) then the magnified moment, M<sub>2</sub>, is smaller than first order moment (M<sub>2ns</sub>+M<sub>2s</sub>) or it can even change sign, e.g.:

• 
$$M_{2ns} = 16 \text{ k-ft}, M_{2s} = -10.0 \text{ k-ft}, \delta = 1.2$$
  
 $M_2 = 16 + 1.2 (-10.0) = 4.0 \text{ k-ft}$   
 $(M_{2ns}+M_{2s}) = 6.0 \text{ k-ft}$ 

• 
$$M_{2ns} = 16 \text{ k-ft}, M_{2s} = -14.4 \text{ k-ft}, \delta = 1.2$$
  
 $M_2 = 16 + 1.2 (-14.4) = -1.28 \text{ k-ft}$   
 $(M_{2ns}+M_{2s}) = 1.6 \text{ k-ft}$ 

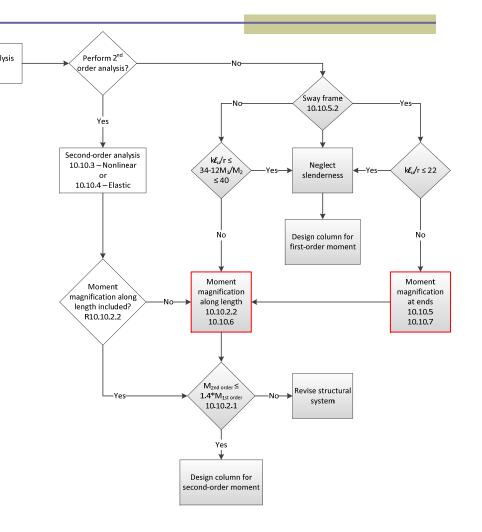
 First-order moment may govern the design rather than second order-moment



#### Moment Magnification – Sway Frames

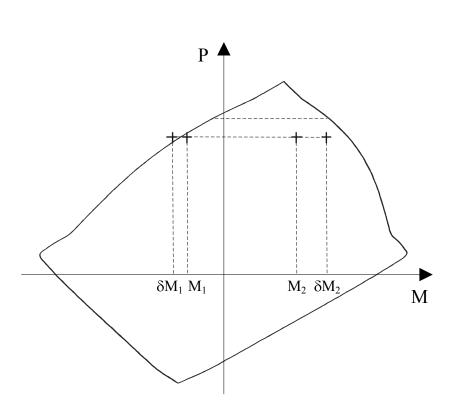
- Since ACI 318-08 International First-order analysis moments in compression members in sway frames are magnified both at ends and along length
  Prior to ACI 318 08
- Prior to ACI 318-08 magnification along length applied only if

$$\frac{\ell_{u}}{r} > \frac{35}{\sqrt{\frac{P_{u}}{f_{c}A_{g}}}}$$



# Moment Magnification – $M_1$

- $M_1$  may govern the design rather than  $M_2$ even though  $|M_2| > |M_1|$ and ACI 318, 10.10.6 provision stipulates that compression members shall be designed for  $M_c = \delta M_2$ . Consider:
  - Double curvature bending (M<sub>1</sub>/M<sub>2</sub> < 0)</li>
  - Asymmetric Section
  - $\delta M_2 \rightarrow OK$  but  $\delta M_1 \rightarrow NG$



# Moment Magnification – $M^{2nd}/M^{1st}$

ACI 318-11, 10.10.2.1 limits ratio of second-order moment to first-order moments

 $M^{2nd}/M^{1st} < 1.4$ 

What if ratio is negative, e.g.:

- $M^{1st} = M_{ns} + M_s = 10.0 + (-9.0) = 1.0 \text{ k-ft}$
- $M^{2nd} = \delta(M_{ns} + \delta_s M_s) = 1.05 (10.0+1.3(-9.0)) = -1.78 \text{ k-ft}$
- $M^{2nd}/M^{1st} = -1.78 \rightarrow OK \text{ or } NG ?$

• Check  $|M^{2nd}/M^{1st}| = 1.78 > 1.4 \rightarrow NG$ 



## Moment Magnification – M<sup>2nd</sup>/M<sup>1st</sup>

■ What if M<sup>1st</sup> is very small, i.e. M<sup>1st</sup> < M<sub>min</sub>, e.g.:

• 
$$M^{1st} = M_2 = 0.1 \text{ k-ft}$$
 (Nonsway frame)

• 
$$M_{min} = P_u(0.6 + 0.03h) = 5 \text{ k-ft}$$

- $M^{2nd} = M_c = \delta M_{min} = 1.1*5 = 5.5 \text{ k-ft}$
- $M^{2nd}/M^{1st} = 5.5/0.1 = 55 \rightarrow OK \text{ or } NG ?$

• Check 
$$M^{2nd}/M_{min} = 1.1 \rightarrow OK$$



#### Conclusions

#### Summary

- Irregular shapes of sections and reinforcement patterns lead to irregular and distorted interaction diagrams
- Large number of load cases and load combinations lead to large number of load points potentially covering entire (P, M<sub>x</sub>, M<sub>y</sub>) space
- Intuition may overlook unusual conditions in tall structures



#### Conclusions

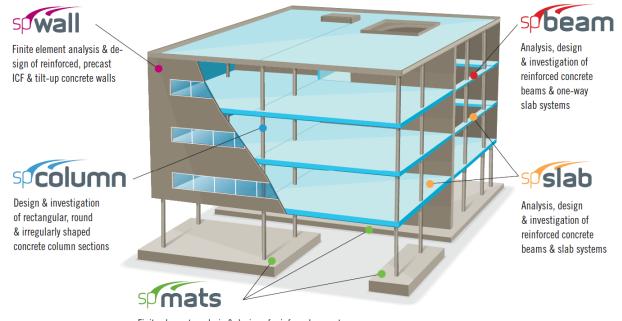
#### Recommendations

- Do not eliminate load cases and combinations based on intuition
- Run biaxial rather than uniaxial analysis for asymmetric sections
- Run both 1<sup>st</sup> order and 2<sup>nd</sup> order analysis
- Apply engineering judgment rather than following general code provisions literally
- Use reliable software and verify its results





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