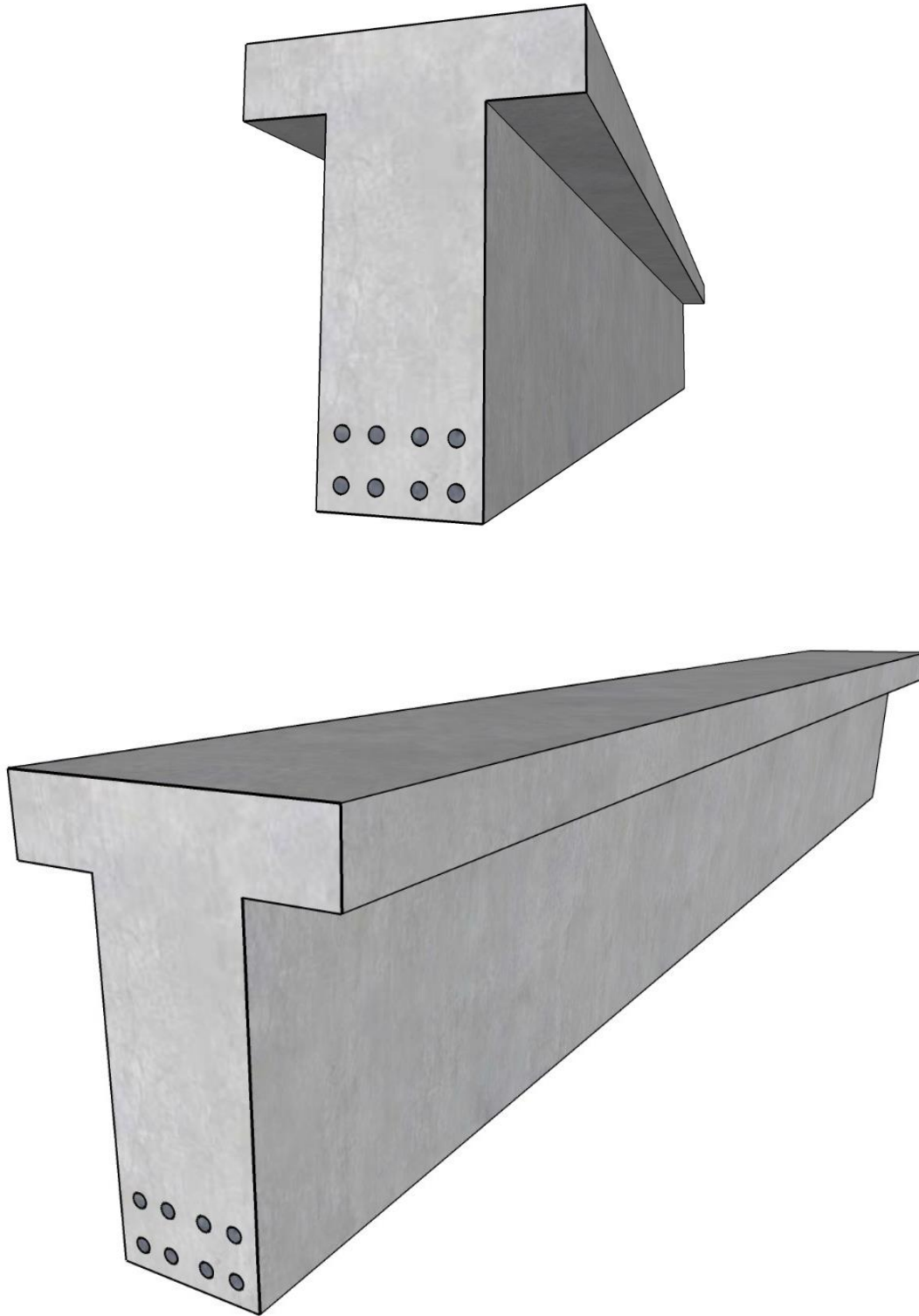


Moment Strength of Flanged Reinforced Concrete Beam (ACI 318-14)



Moment Strength of Flanged Reinforced Concrete Beam (ACI 318-14)

Determining the design moment strength of the isolated T-section shown in Figure 1. Tension reinforcement is 8-#11. Concrete compressive strength f_c' is 4,000 psi and reinforcement yield strength f_y is 60,000 psi. Compare the calculated values in the Reference and the hand calculations with values obtained by [spBeam](#) engineering software program from [StructurePoint](#).

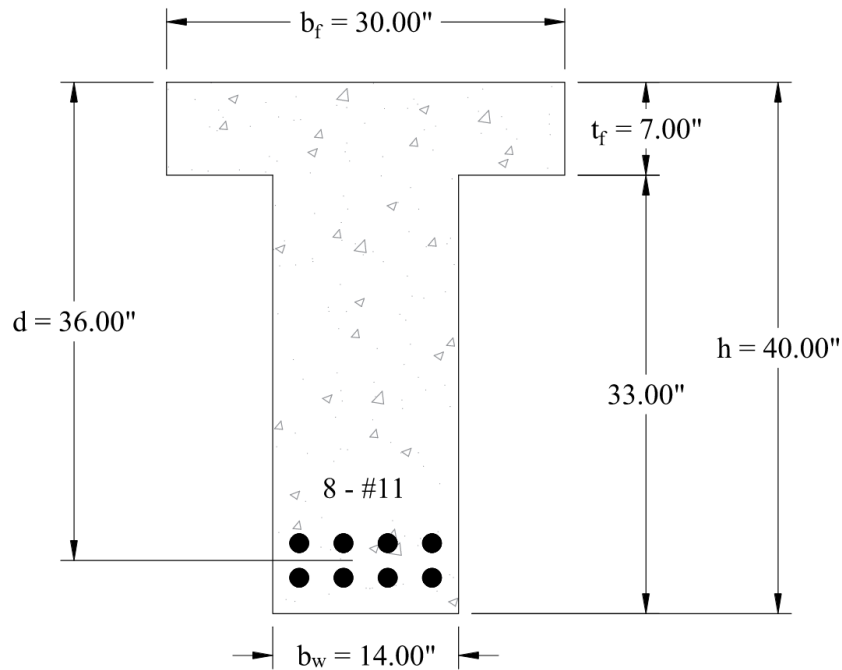


Figure 1 – Flanged Reinforced Concrete Beam Cross-Section

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Code

- Building Code Requirements for Structural Concrete (ACI 318-14) and Commentary (ACI 318R-14)

Reference

[1] Reinforced Concrete Design, 8th Edition, 2017, Chu-Kia Wang, Charles G. Salmon, Jose A. Pincheira, Gustavo J. Parra-Montesinos, Oxford University Press, Example 4.4.2.

[2] [spBeam Engineering Software Program Manual v5.50](#), StructurePoint LLC., 2018.

Design Data

$f_c' = 4,000$ psi normal weight concrete

$f_y = 60,000$ psi

Beam effective depth, $d = 36$ in.

Flange thickness, $t_f = 7$ in.

Clear cover = 1.5 in.

Tension reinforcement (8-#11), $A_s = 8 \times 1.56 \text{ in.}^2 = 12.48 \text{ in.}^2$

Rectangular section behavior is assumed where the stress block depth a is less than the flange thickness ($a < t_f$) and yielding of the reinforcement is expected.

Solution

1. Effective Flange Width

Determining the effective flange width following ACI 318-14 (6.3.2.2), the effective flange width b_f will be:

$$b_f \leq 4b_w \quad \text{ACI 318-14 (6.3.2.2)}$$

$$b_f = 30 \text{ in.} \leq 4b_w = 4 \times 14 \text{ in.} = 56 \text{ in.}$$

$$t_f \geq 0.5b_w \quad \text{ACI 318-14 (6.3.2.2)}$$

$$t_f = 7 \text{ in.} \leq 0.5b_w = 0.5 \times 14 \text{ in.} = 7 \text{ in.}$$

Therefore, flange width and flange thickness are satisfactory to ACI 318-14 (6.3.2.2).

2. Flanged Section Analysis

Calculating stress block depth a assuming rectangular section behavior.

$$a = \frac{A_s f_y}{0.85 f'_c b_f} = \frac{12.48 \text{ in.}^2 \times 60 \text{ ksi}}{0.85 \times 4 \text{ ksi} \times 30 \text{ in.}} = 7.34 \text{ in.} > t_f = 7 \text{ in.}$$

Since the depth of the equivalent block a exceeds the thickness of the flange, assumption of rectangular section behavior is not correct. Therefore, section behaves like a T-section.

3. Design Flexural Strength

The section will be treated as a T-section by the two-coupled method illustrated in Figure 2.

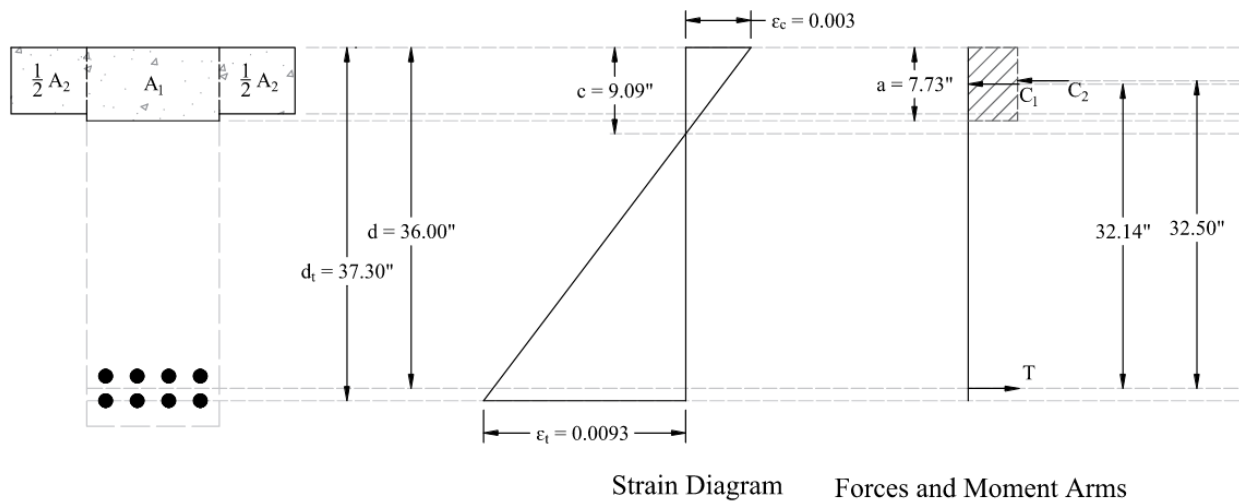


Figure 2 – Flanged Section Analysis

$$T = A_s f_y = 12.48 \text{ in.}^2 \times 60 \text{ ksi} = 749 \text{ kips}$$

From equilibrium $T = C$,

$$C = C_1 + C_2 = 0.85 f'_c A_1 + 0.85 f'_c A_2 \rightarrow 749 \text{ kips} = 3.4 \text{ ksi} \times 14 \text{ in.} \times a + 3.4 \text{ ksi} \times 16 \text{ in.} \times 7 \text{ in.}$$

$$749 \text{ kips} = 3.4 \text{ ksi} \times 14 \text{ in.} \times a + 3.4 \text{ ksi} \times 16 \text{ in.} \times 7 \text{ in.}$$

$$a = 7.73 \text{ in.}$$

$$C_1 = 3.4 \text{ ksi} \times 14 \text{ in.} \times 7.73 \text{ in.} = 368 \text{ kips}$$

$$C_2 = 3.4 \text{ ksi} \times 16 \text{ in.} \times 7.0 \text{ in.} = 381 \text{ kips}$$

$$M_n = C_1 \times [36 \text{ in.} - 0.5 \times 7.73 \text{ in.}] \times \frac{1 \text{ ft}}{12 \text{ in.}} + C_2 \times (36 \text{ in.} - 3.5 \text{ in.}) \times \frac{1 \text{ ft}}{12 \text{ in.}}$$

$$M_n = 985 \text{ ft-kips} + 1032 \text{ ft-kips} = 2017 \text{ ft-kips}$$

$$c = \frac{a}{\beta_1} = \frac{7.73 \text{ in.}}{0.85} = 9.09 \text{ in.}$$

Since $f_c' = 4,000$ psi:

$$\beta_1 = 0.85$$

ACI 318-14 (Table 22.2.2.4.3)

$$d_t = h - \text{clear cover} - d_{\text{stirrup}} - \frac{d_{\text{bar}}}{2} = 40 \text{ in.} - 1.5 \text{ in.} - 0.5 \text{ in.} - \frac{1.41 \text{ in.}}{2} = 37.3 \text{ in.}$$

$$\varepsilon_t = \left(\frac{0.003}{c} \right) d_t - 0.003 = \left(\frac{0.003}{9.09 \text{ in.}} \right) \times 37.3 \text{ in.} - 0.003 = 0.0093 > 0.005$$

Therefore: $\phi = 0.90$ (function of the extreme-tension layer of bars strain)

ACI 318-14 (21.2.1)

$$\phi M_n = 0.9 \times 2017 \text{ ft-kip} = 1815.3 \text{ ft-kip}$$

4. Moment Strength of Flanged Reinforced Concrete Beam – [spBeam](#) Software

[spBeam](#) is widely used for analysis, design and investigation of beams, and one-way slab systems (including standard and wide module joist systems) per latest American (ACI 318) and Canadian (CSA A23.3) codes. [spBeam](#) can be used for new designs or investigation of existing structural members subjected to flexure, shear, and torsion loads. With capacity to integrate up to 20 spans and two cantilevers of wide variety of floor system types, [spBeam](#) is equipped to provide cost-effective, accurate, and fast solutions to engineering challenges.

[spBeam](#) provides top and bottom bar details including development lengths and material quantities, as well as live load patterning and immediate and long-term deflection results. Using the moment redistribution feature engineers can deliver safe designs with savings in materials and labor. Engaging this feature allows up to 20% reduction of negative moments over supports reducing reinforcement congestions in these areas.

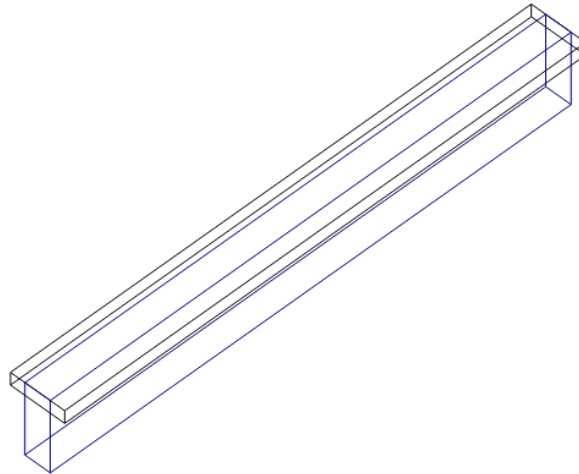
Beam analysis and design requires engineering judgment in most situations to properly simulate the behavior of the targeted beam and take into account important design considerations such as: designing the beam as rectangular or T-shaped sections; using the effective flange width or the center-to-center distance between the beam and the adjacent beams. Regardless which of these options is selected, [spBeam](#) provide users with options and flexibility to:

1. Design the beam as a rectangular cross-section or a T-shaped section.
2. Use the effective or full beam flange width.
3. Include the flanges effects in the deflection calculations.
4. Invoke moment redistribution to lower negative moments
5. Using gross (uncracked) or effective (cracked) moment of inertia
6. Design the beam as singly or doubly reinforced section.

For illustration and comparison purposes, the following figures provide a sample of the results obtained from an [spBeam](#) model created for the beam covered in this design example.



spBeam v5.50
A Computer Program for Analysis, Design, and Investigation of
Reinforced Concrete Beams and One-way Slab Systems
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1. Input Echo

1.1. General Information

File Name	...\Strength of T Section (Investigation) 4.4....
Project	Strength of T Section (Investigation) 4.4.2 - ACI318 -14
Frame	Example 4.4.2
Engineer	SP
Code	ACI 318-14
Reinforcement Database	User Defined
Mode	Investigation
Number of supports =	2
Floor System	One-Way/Beam

1.2. Solve Options

Live load pattern ratio = 0%
Deflections are based on gross section properties.
Long-term deflections are NOT calculated.
Compression reinforcement calculations selected.
Default incremental rebar design selected.
Moment redistribution NOT selected.
Effective flange width calculations selected.
Rigid beam-column joint NOT selected.
Torsion analysis and design NOT selected.

1.3. Material Properties

1.3.1. Concrete: Slabs / Beams

w_c	150 lb/ft ³
f'_c	4 ksi
E_c	3834.3 ksi
f_r	0.47434 ksi

1.3.2. Concrete: Columns

w_c	150 lb/ft ³
f'_c	4 ksi
E_c	3834.3 ksi
f_r	0.47434 ksi

1.3.3. Reinforcing Steel

f_y	60 ksi
f_{yt}	60 ksi
E_s	29000 ksi
Epoxy coated bars	No

1.4. Reinforcement Database

Size	Db	Ab	Wb	Size	Db	Ab	Wb
	in	in ²	lb/ft		in	in ²	lb/ft
#3	0.38	0.11	0.38	#4	0.50	0.20	0.67

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Size	Db	Ab	Wb	Size	Db	Ab	Wb
	in	in ²	lb/ft		in	in ²	lb/ft
#5	0.63	0.31	1.04	#6	0.75	0.44	1.50
#7	0.88	0.60	2.04	#8	1.00	0.79	2.67
#9	1.13	1.00	3.40	#10	1.27	1.27	4.30
#11	1.41	1.56	5.31	#14	1.69	2.25	7.65
#18	2.26	4.00	13.60				

1.5. Span Data

1.5.1. Slabs

Span	Loc	L1	t	wL	wR	bE _{ff}	H _{min}
		ft	in	ft	ft	in	in
1	Int	24.000	7.00	1.250	1.250	30.00	0.00

1.5.2. Ribs and Longitudinal Beams

Span	Ribs			Beams		Span H _{min}
	b	h	Sp	b	h	
	in	in	in	in	in	in
1	0.00	0.00	0.00	14.00	40.00	18.00

1.6. Support Data

1.6.1. Columns

Support	c1a	c2a	Ha	c1b	c2b	Hb	Red %
	in	in	ft	in	in	ft	
1	28.00	28.00	0.000	28.00	28.00	0.000	100
2	28.00	28.00	0.000	28.00	28.00	0.000	100

1.6.2. Boundary Conditions

Support	Spring		Far End	
	K _x	K _y	Above	Below
	kip/in	kip-in/rad		
1	0	0	Pinned	Pinned
2	0	0	Pinned	Pinned

1.7. Load Data

1.7.1. Load Cases and Combinations

Case	Dead	Live
Type	DEAD	LIVE
U1	1.200	1.600

1.7.2. Line Loads

Case/Patt	Span	Wa	La	Wb	Lb
		lb/ft	ft	lb/ft	ft
Live	1	15750.00	0.000	15750.00	24.000

1.8. Reinforcement Criteria

1.8.1. Slabs and Ribs

	Units	Top Bars		Bottom Bars	
		Min.	Max.	Min.	Max.
Bar Size		#3	#4	#3	#4

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	Units	Top Bars		Bottom Bars	
		Min.	Max.	Min.	Max.
Bar spacing	in	1.00	18.00	1.00	18.00
Reinf ratio	%	0.14	5.00	0.14	5.00
Clear Cover	in	3.00		3.00	

There is NOT more than 12 in of concrete below top bars.

1.8.2. Beams

	Units	Top Bars		Bottom Bars		Stirrups	
		Min.	Max.	Min.	Max.	Min.	Max.
Bar Size		#3	#3	#4	#4	#3	#4
Bar spacing	in	1.00	18.00	1.00	18.00	6.00	18.00
Reinf ratio	%	0.14	5.00	0.14	5.00		
Clear Cover	in	3.00		3.00			
Layer dist.	in	1.00		1.00			
No. of legs						2	6
Side cover	in					1.50	
1st Stirrup	in					3.00	

There is NOT more than 12 in of concrete below top bars.

1.9. Reinforcing Bars

1.9.1. Top Bars

Top Bars: --- NONE ---

1.9.2. Bottom Bars

Span	Continuous		Discontinuous			
	Bars	Cover in	Bars	Length ft	Start ft	Cover in
1	4-#11	2.00				
	4-#11	4.59				

1.9.3. Transverse Reinforcement

Span	Stirrups (2 legs each unless otherwise noted)
1	14-#4 @ 5.9 + 9-#4 @ 10.6 + 14-#4 @ 5.9

2. Design Results

2.1. Flexural Capacity

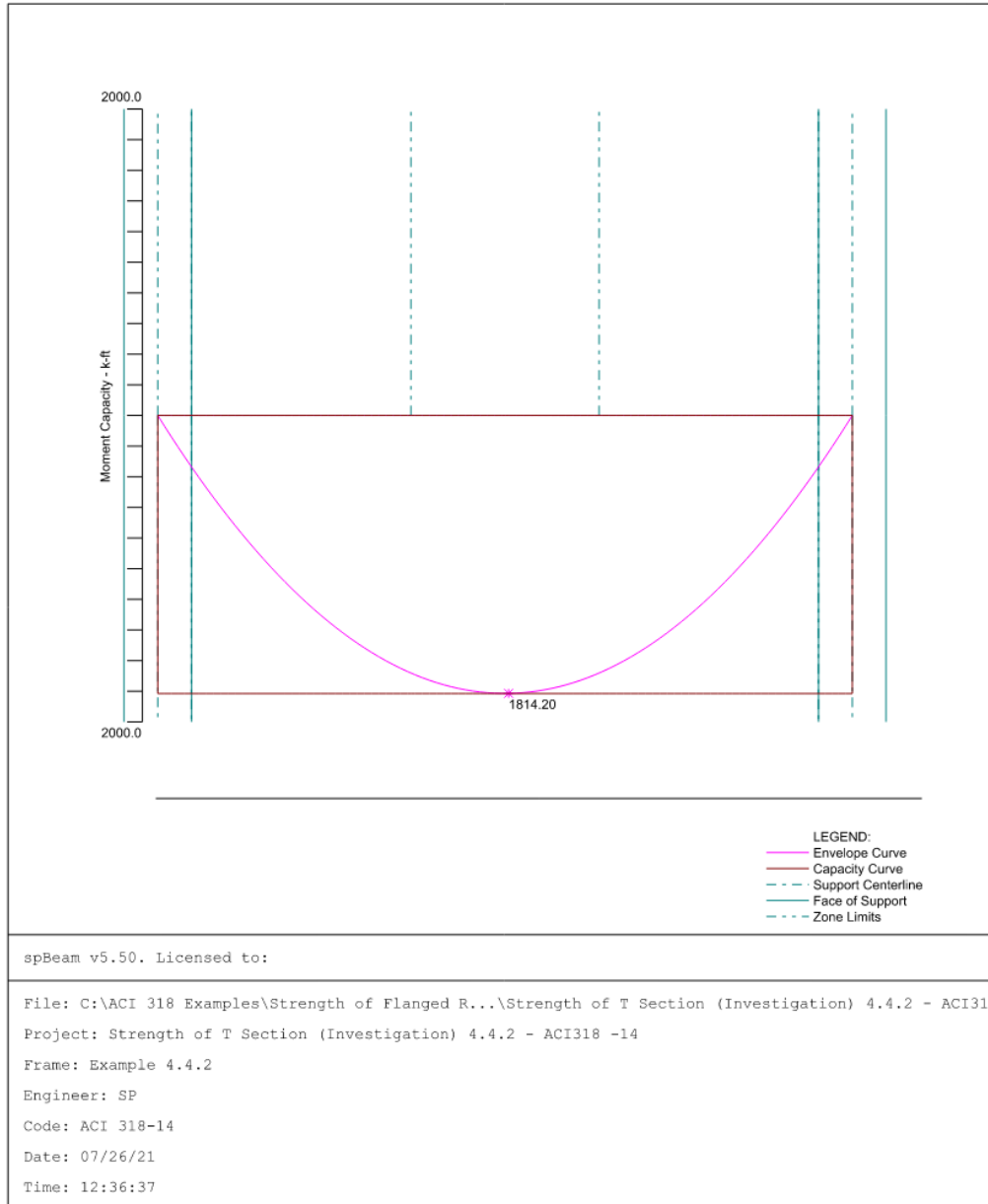
Span	x ft	Top					Bottom				
		A _{s,top} in ²	ΦM _n ⁻ k-ft	M _u ⁻ k-ft	Comb Pat	Status	A _{s,bot} in ²	ΦM _n ⁺ k-ft	M _u ⁺ k-ft	Comb Pat	Status
1	0.000	0.00	0.00	0.00	U1 All	---	12.48	1815.11	0.00	U1 All	---
	1.167	0.00	0.00	0.00	U1 All	OK	12.48	1815.11	335.65	U1 All	OK
	8.750	0.00	0.00	0.00	U1 All	OK	12.48	1815.11	1681.12	U1 All	OK
	12.000	0.00	0.00	0.00	U1 All	OK	12.48	1815.11	1814.20	U1 All	OK
	12.125	0.00	0.00	0.00	U1 All	OK	12.48	1815.11	1814.20	U1 All	OK
	15.250	0.00	0.00	0.00	U1 All	OK	12.48	1815.11	1681.12	U1 All	OK
	22.833	0.00	0.00	0.00	U1 All	OK	12.48	1815.11	335.66	U1 All	OK
	24.000	0.00	0.00	0.00	U1 All	---	12.48	1815.11	0.00	U1 All	---

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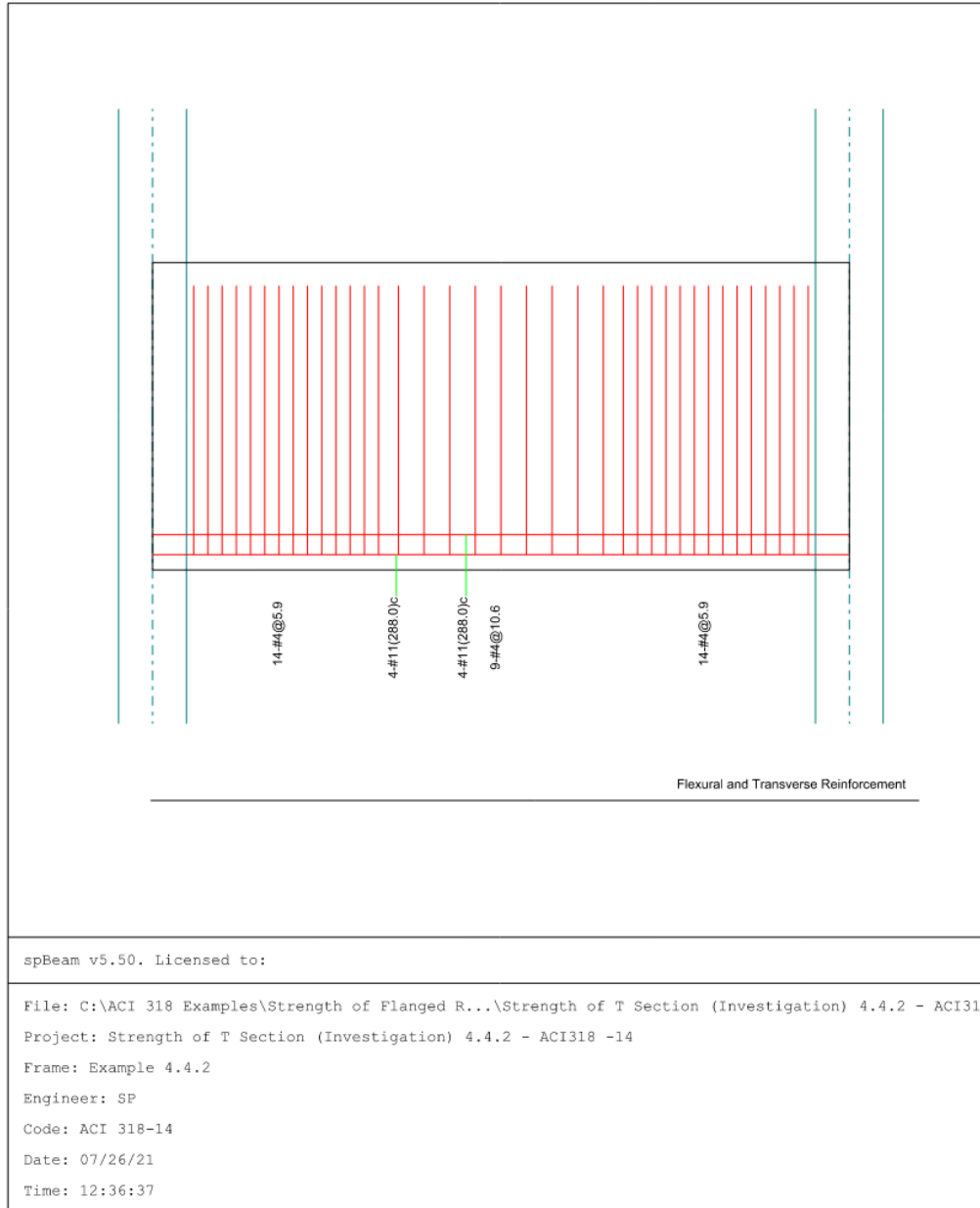
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3. Diagrams

3.1. Moment Capacity



3.2. Reinforcement



5. Comparison of Analysis Results

Table 1 - Comparison of Results				
Method	Reinforcement	$A_{s,provided}$, in.²	b_f, in.	ϕM_n, kip-ft
Reference	8 #11	12.48	30	1815.3
Hand	8 #11	12.48	30	1815.3
spBeam	8 #11	12.48	30	1815.1

In all of the hand calculations and the reference used illustrated above, the results are in precise agreement with the automated exact results obtained from the [spBeam](#) program. The reference example displayed the nominal flexural capacity without having the strength reduction factor applied. A value of 0.9 for the flexural reduction factor is applied in Table 1.